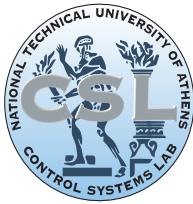


# OBSIdian

## On-Board System Identification for Uncertainty Modelling & Characterization

AO/1-9509/18/NL/GLC

Final Presentation



# Agenda

- 09.30 – 09.35 Welcome
- 09.35 – 09.48 Introduction
- 09.48 – 10.48 Benchmark Problems
- 10.48 – 10.58 Break
- 10.58 – 11.26 Study Cases
- 11.26 – 11.35 SYSID Detailed Design – 3D SC1
- 11.35 – 11.45 Sensitivity, Robustness, Sampling Considerations
- 11.45 – 11.48 Project Output Exploitation
- 11.48 – 11.51 Conclusions
- 11.51 – 11.53 Managerial
- 11.53 – 12.30 Discussion

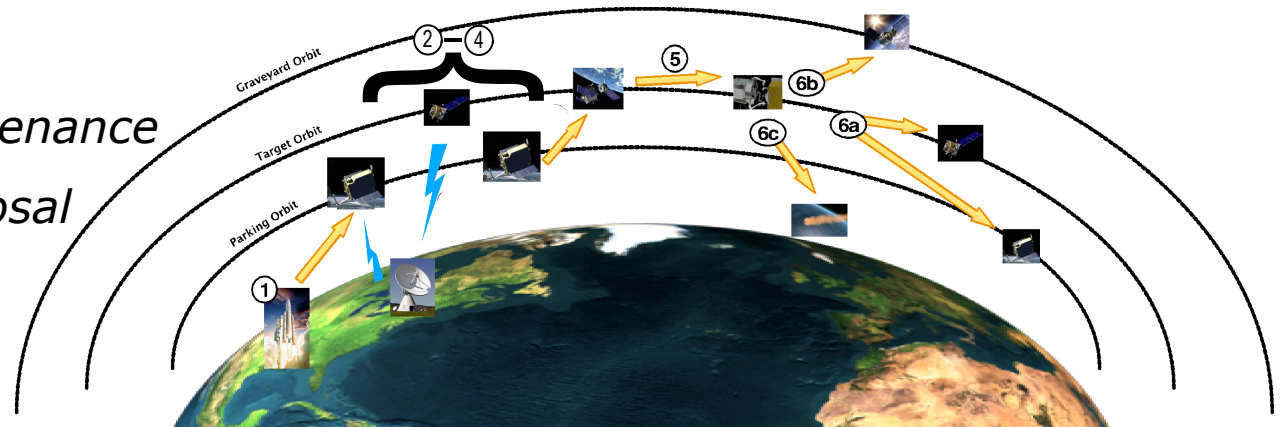
# Introduction

# Problem Statement (1/5)

## ❑ OOS Chaser-Target berthing-type mission

- ❑ *Launch of Servicing satellite (Chaser)*
- ❑ *Phasing with Client (Target)*
- ❑ *Far Rendezvous sequence/ Homing*
- ❑ *Forced Motion/ Closing and Inspection*
- ❑ *Final Approach – Capture – Stabilisation – Docking*
- ❑ *OOS tasks*

- *Orbital assembly*
- *Satellite repair/ maintenance*
- *Debris handling/ disposal*





# Problem Statement (2/5)

□ *Chaser and/ or Target parameters may be **unknown or uncertain***

- Fuel consumption changes the **sloshing** model parameters
- Temperature changes affects the flexible appendages **modal** parameters
- Grasping of Target may result in uncertain change of system **inertial** parameters
- Completely **unknown** Target parameters

# Problem Statement (3/5)

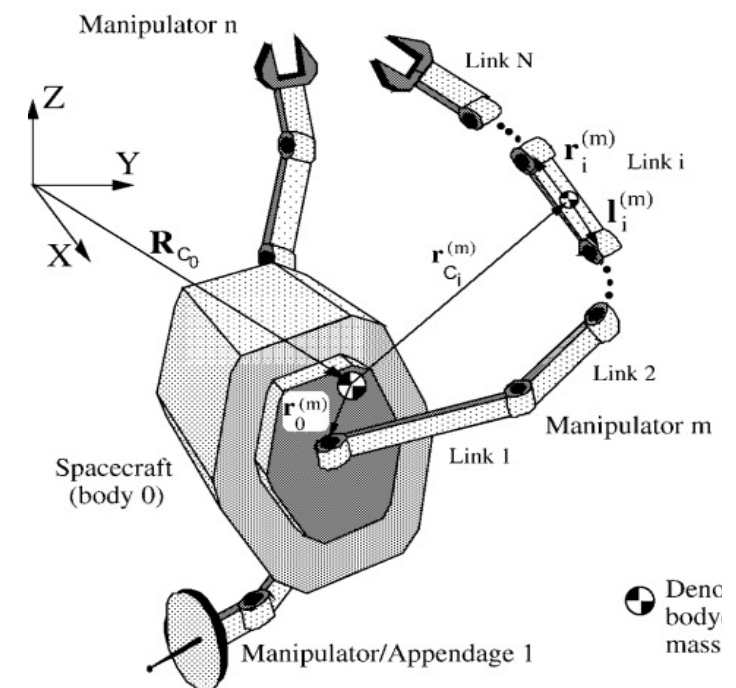
□ *Parameter change/ uncertainty may be beyond the capabilities of a robust controller to cope with*

- Recalibration of the controller parameters
- Updated parameter estimates by means of a **System Identification (SYSID)** process

# Problem Statement (4/5)

□ *Berthing-type OOS mission can be achieved using a **Space Manipulator System (SMS)***

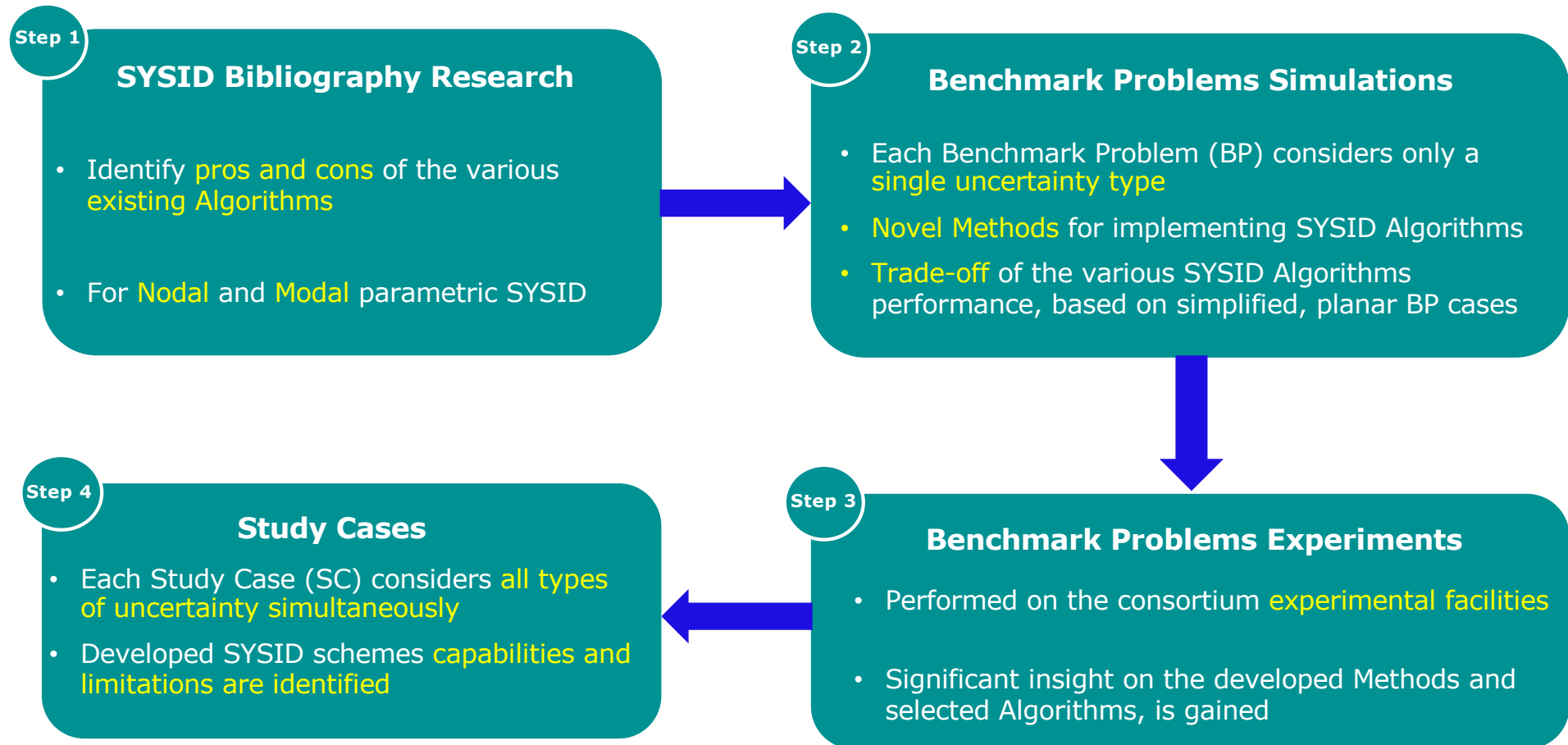
- **Accurate control** of the berthing fixture and the captured Target
- **Complex system**
- We opted to work with an SMS, but **results are general**
- **Uncertainty** types considered:
  - ❖ System **inertial** parameters
  - ❖ Fuel **sloshing** model parameters
  - ❖ Flexible appendage **modal** parameters



# Problem Statement (5/5)

- *Inspection and Forced Motion stage (off-line PI)*
  - Chaser subsystems parameters (inertial/ flexible)
  - Chaser fuel sloshing
  
- *Capture – Mating/ OOS tasks stage (on-/ off-line PI)*
  - Target subsystems parameters (inertial/ flexible)
  - Target fuel sloshing
  
- *Level of realism vs. Complexity*
  
- *Not everything can be “unknown”*

# OBSIdian Framework



# Benchmark Problems Considered

Benchmark Problem 1 (BP1A)	Benchmark Problem 1 (BP1B)	Benchmark Problem 2 (BP2)	Benchmark Problem 3A (BP3A)	Benchmark Problem 3B (BP3B)
<b>Identification of inertial parameters</b>  (no sloshing, no flexibilities)	<b>Identification of inertial parameters</b>  (no sloshing, no flexibilities)	<b>Identification of sloshing model parameters</b>  (known satellite, no flexibilities)	<b>Identification of appendages modal parameters</b>  (known satellite, no sloshing)	<b>Identification of appendages modal parameters</b>  (known satellite, no sloshing)
<b>Experimental Identification</b>  Excitation is user's choice	<b>Experimental Identification</b>  Excitation is user's choice	<b>Experimental Identification</b>  Excitation is user's choice	<b>Experimental Identification</b>  Excitation is user's choice	<b>Operational Identification</b>  Excitation by the task
<b>Non-recursive SYSID</b>  (Parametric Identification Algorithm)	<b>Non-recursive SYSID</b>  (Parametric Identification Algorithm)	<b>Non-recursive SYSID</b>  (Parametric Identification Algorithm)	<b>Non-recursive SYSID</b>  (EMA)	<b>Recursive SYSID</b>  (OMA)
<b>Model</b>  2D free-floating space robot (manipulator joints actuated only)	<b>Model</b>  2D free-flying space robot (active manipulator, thrusters and RWs)	<b>Model</b>  2D satellite and 2D sloshing models	<b>Model</b>  2D flexible appendage on hub	<b>Model</b>  2D flexible appendage on hub

# Study Cases Considered

Study Case 1 (SC1)		Study Case 2 (SC2)	
<b>Full System Identification</b> i.e., identification of inertial parameters, sloshing parameters, and modal parameters of flexible appendages simultaneously (to the extent possible)			
<b>Phase 1</b> Motion before capture		<b>Phase 2</b> Motion after rigid capture-during berthing	
<b>Experimental Identification</b> Excitation is user's choice		<b>Operational Identification</b> Excitation by the task	
<b>Non-recursive SYSID</b> (Parametric Identification Method for lumped models + EMA for continuous models)		<b>Recursive SYSID</b> (Parametric Identification Method for lumped models + OMA for continuous models)	
3D Simulation	2D Experiments	3D Simulation	2D Experiments

# SYSID Algorithms (1/5)

## □ Types of SYSID approaches

### ❖ **White-box** Models and SYSID

- Both *Physical Laws and Model Structure are known*
- e.g., system dynamics equations of motion

### ❖ **Grey-box** Models and SYSID

- *Physical Laws are known, while Model Structure is partially unknown*
- e.g., linear models, LPV models etc. of a nonlinear system

### ❖ **Black-box** SYSID

- Both *Physical Laws and Model Structure are unknown*
- More a “curve-fitting” describing the input-output system behaviour



# SYSID Algorithms (2/5)

- ❑ More than 50 Parametric, Non-parametric and Modal SYSID Algorithms were considered
  - Based on their basic characteristics, many were discarded outright
  
- ❑ 15 Parametric, 2 Non-Parametric and 19 Modal SYSID Algorithms were considered further
  - Trade-off analysis, based on a detailed study of each algorithm's characteristics

# SYSID Algorithms (3/5)

- 4 Parametric and 5 Modal SYSID Algorithms chosen as appropriate candidates for a final trade-off
  - Parametric SYSID Algorithms: UKF, IV, PEM, TLS
  - Modal Analysis Algorithms: FSDD, RFP, LSCE, SSI-COV, SSI-DATA

# SYSID Algorithms (4/5)

## ❑ Trade-off to be based on Performance Metrics

- **Computational Effort:** FLOPS and Big-O Notation
- **Relative % error:** Parametric error with respect to “true” value
- Convergence rate also was initially considered but is valid for recursive SYSID only

# SYSID Algorithms (5/5)

- ❑ SYSID Parametric Algorithms must be applied on equations that characterize the system
  - Equations of motion
  - Energy balance
  - Angular momentum conservation (when applicable)
  - Transfer function (when applicable)
  
- ❑ Choice of appropriate equation is not trivial
  - Constitutes the SYSID scheme **Method**
  - Results in the required Regressor Formulation
  
- ❑ Different SYSID Algorithms (regressor-based or not)
  - Constitutes the SYSID scheme **Algorithm**

# Benchmark Problems

# Basic Considerations (1/4)

## ☐ Sensors

- IMU
- Motor encoders
- Flexible appendage accelerometers
- Sun- Star-trackers (for full scale system) or PhaseSpace MoCap system (for SRE)
- Realistic noise models employed

## ☐ Actuators

- Joint motors
- Reaction wheels
- Thrusters

# Basic Considerations (2/4)

## □ Signal Conditioning

- **Low – pass filters** applied: ‘designfilt’ MATLAB function
  - Pass dominant system dynamics, & filter noise, to the extent possible
  - First order low-pass Infinite Impulse Response (IIR)
  - Filter cut-off frequencies chosen using signal FFT’s
  - Cut-off frequencies values depend on sensor

# Basic Considerations (3/4)

## Planar Full-scale System Models (simulations)

- ❑ Final trade-off of the chosen SYSID Algorithms
- ❑ Insight on the SYSID Algorithms requirements
- ❑ Develop appropriate Methods to apply the chosen Algorithms

## Planar Experiments (scaled-down consortium facilities)

- ❑ Significant insight on the SYSID Algorithms and developed Methods requirements, capabilities and limitations



# Basic Considerations (4/4)

## Experimental Setups Models (simulated experiments)

*Simulated experiments* performed with the aim to:

- Validate the developed Analytical Models
- Design of excitation signal to be used for the h/w experiment
- Gain knowledge on the behaviour of the experimental set-up (limitations, sources of error, etc.) and on the SYSID algorithm
- Validate the Experimentally Identified Models, using Analytical and/ or SimScape models

# BP1: Full-scale planar system (1/3)

## Model

2D Space Manipulator System (SMS) with a single manipulator

## Modelling Assumptions

- Rigid S/C and manipulator

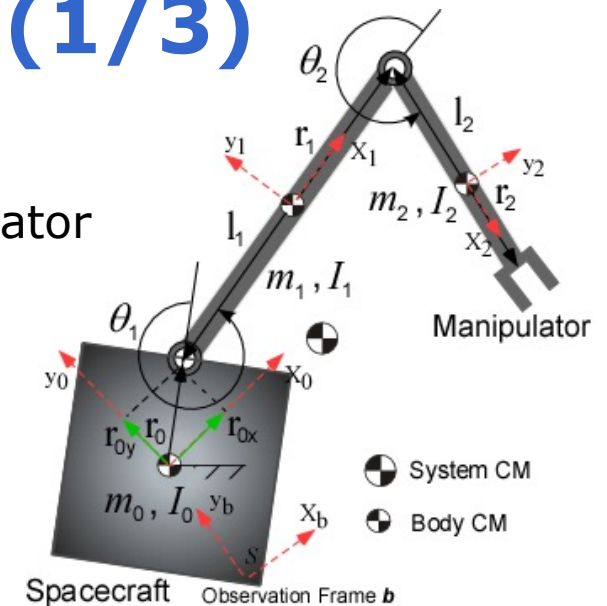
## SMS operational modes

- Free-floating mode (**BP1A**): Only manipulator joints actuated
- Free-flying mode (**BP1B**): Manipulator joints actuated, S/C thrusters and reaction wheels active

## Goal

Estimation of SMS inertial parameters (combination sets)

- Full reconstruction of free-floating dynamics (BP1A) or of free-flying dynamics (BP1B)



# BP1: Full-scale planar system (2/3)

## BP1A Methods and Algorithms

- TLS on regressor formulation of angular momentum conservation (M1-TLS)
- TLS on regressor formulation of equations of motion (M2-TLS)
- IV on regressor formulation of angular momentum conservation (M1-IV)
- IV on regressor formulation of equations of motion (M2-IV)
- PEM
- UKF

## Trade-off Analysis Result

The best algorithm and method combination for **BP1A** is **M1-TLS**.

- Max Rel. Error: 1.19%
- RMS Rel. Error: 0.48%

# BP1: Full-scale planar system (3/3)

## BP1B Methods and Algorithms

- TLS on regressor formulation of equations of motion (M1-TLS)
- TLS on regressor formulation of energy balance equation (M2-TLS)
- IV on regressor formulation of equations of motion (M1-IV)
- IV on regressor formulation of angular momentum conservation (M2-IV)
- PEM
- UKF

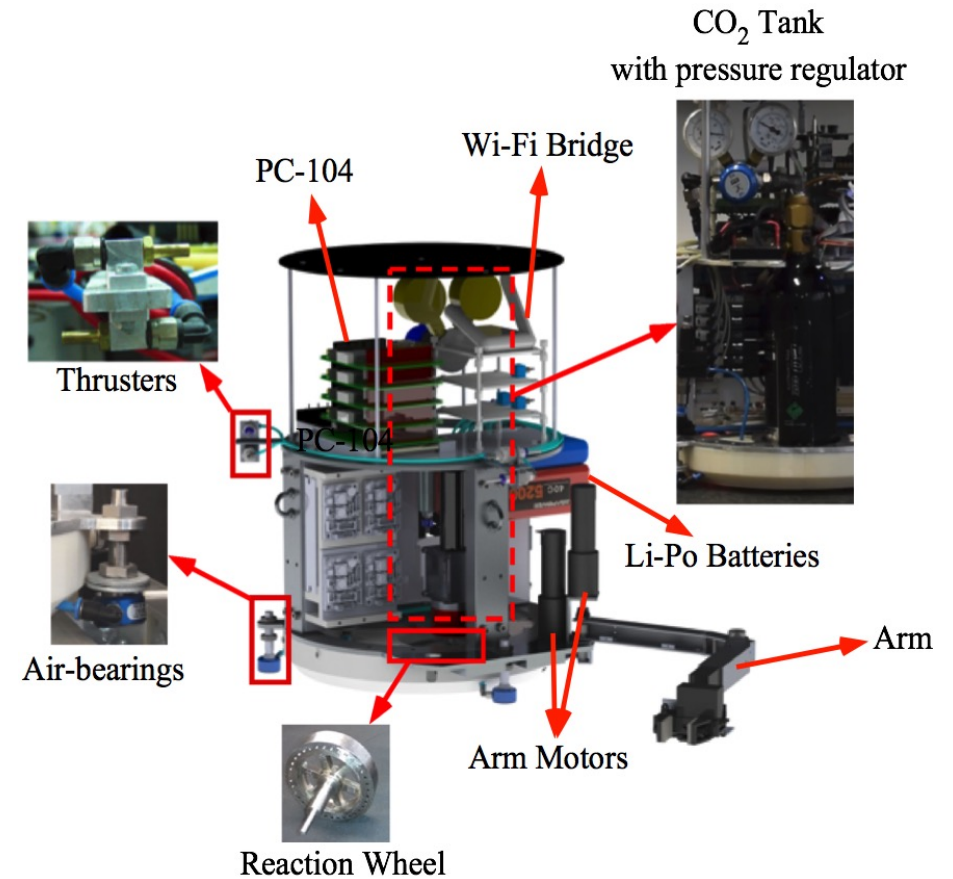
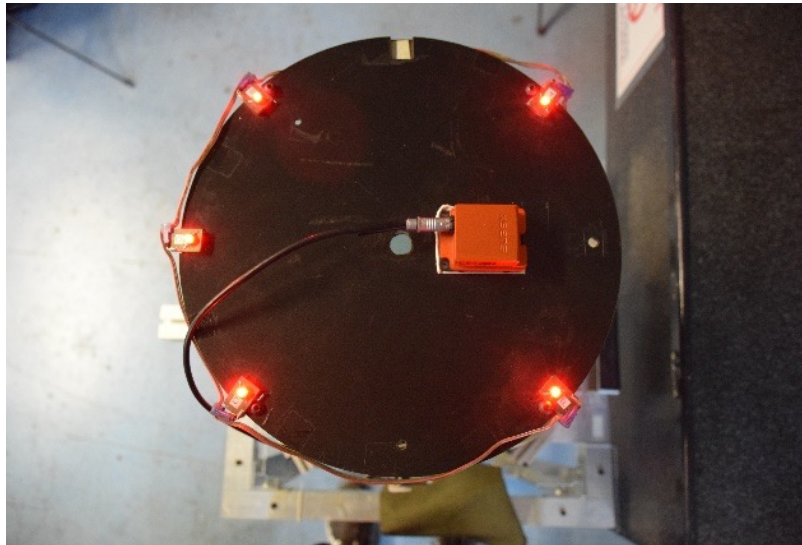
## Trade-off Analysis Results

The best algorithm and method combination for BP1B is [M2-TLS](#).

- Max Rel. Error: 2.63%
- RMS Rel. Error: 1.10%

Thus, the best algorithm **for both BP1A and BP1B** is [TLS](#).

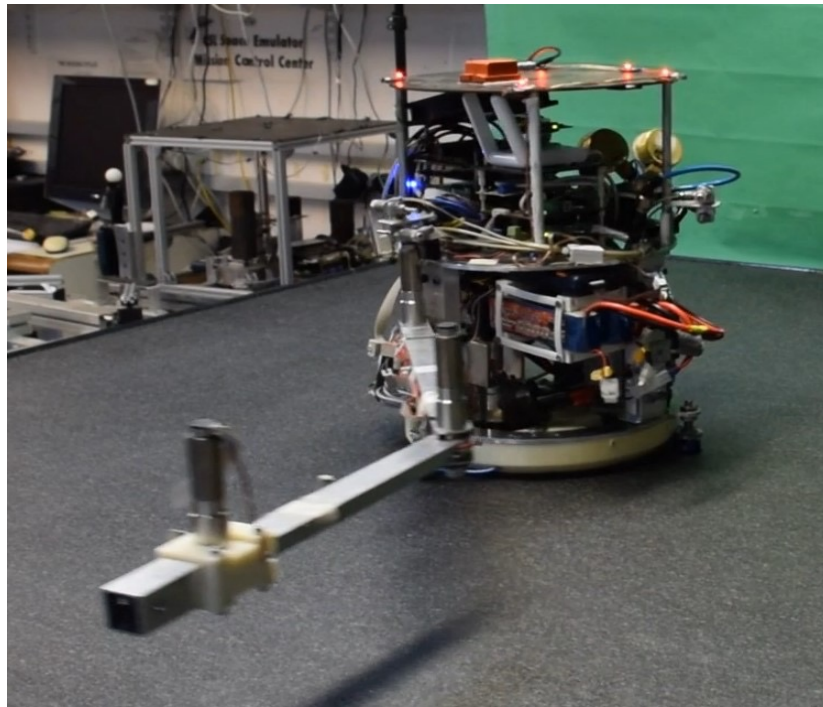
# BP1: Experimental Facility & Model (1/4)



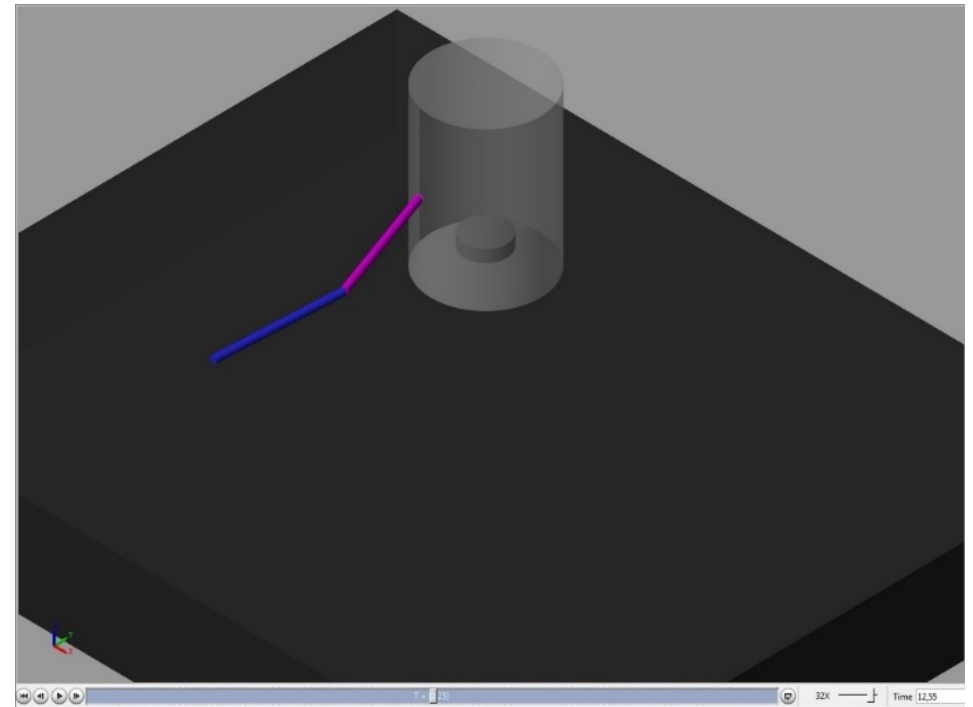
Component	Mass	Notes
Robotic System w/o Manipulator	14 kg	N/A
Robotic System w/t Manipulator	15 kg	N/A
Empty plastic Tank	500 g	N/A
Solar Panel	440 g	N/A
CO <sub>2</sub> Tank (empty) CO <sub>2</sub> Tank (full)	800 g 1500 g	Pressure: 7 bar

# BP1: Experimental Facility & Model (2/4)

- Inertial parameters in accordance with those of Cepheus
- Sensors and actuators in accordance with Cepheus



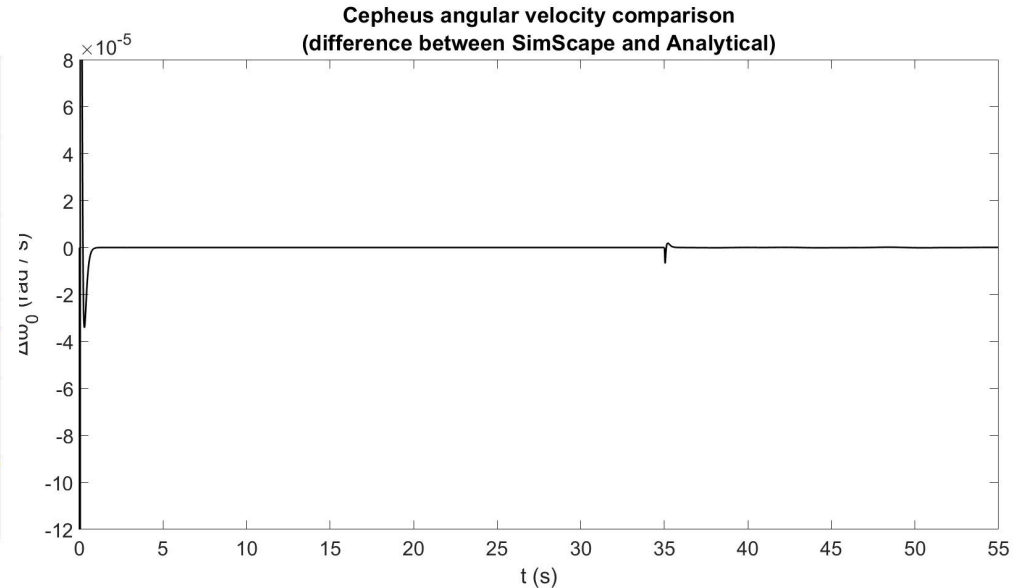
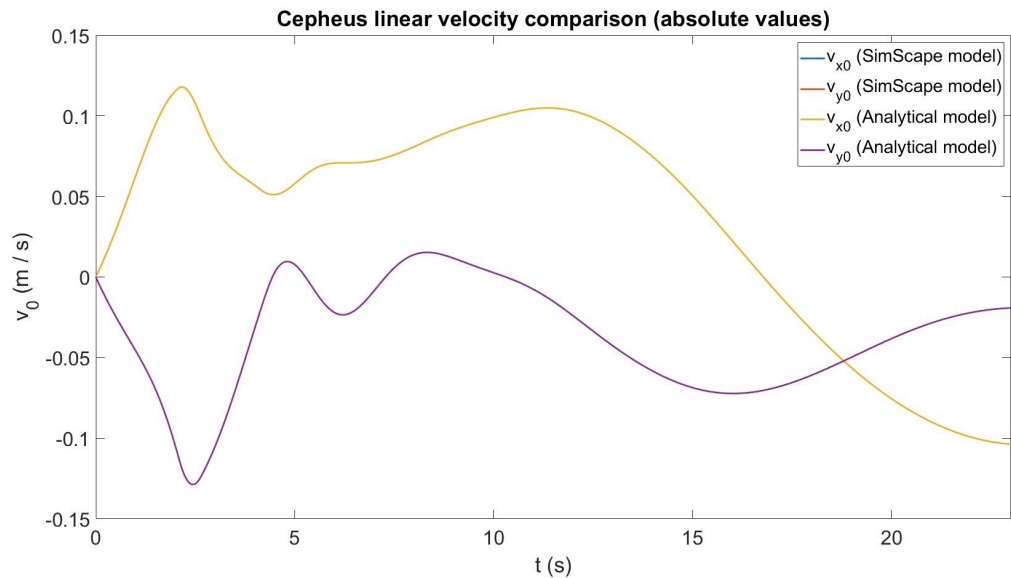
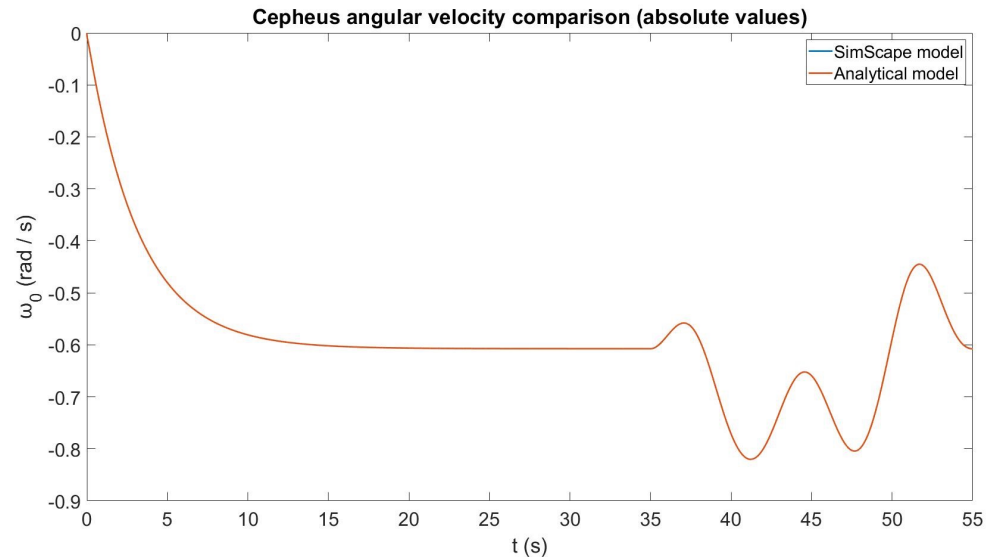
Cepheus



SimScape

# BP1: Experimental Facility & Model (3/4)

- Model response comparisons
  - Analytical vs. Simscape
  - with the **same** excitation
- Responses identical =>  
**analytical Cepheus model verified**



# BP1: Experimental Facility & Model (4/4)

- BP1A **Method** based on System Angular Momentum Conservation

$$Y(\dot{\theta}_1, \dot{\theta}_2, \theta_1, \theta_2, {}^0\omega_{0z}) \mathbf{a} = \mathbf{h}_{cm}$$

- BP1B **Method** based on System Energy Balance

$$Y(\dot{\theta}_1, \dot{\theta}_2, \theta_1, \theta_2, {}^0\omega_{0z}) \mathbf{a} = b$$

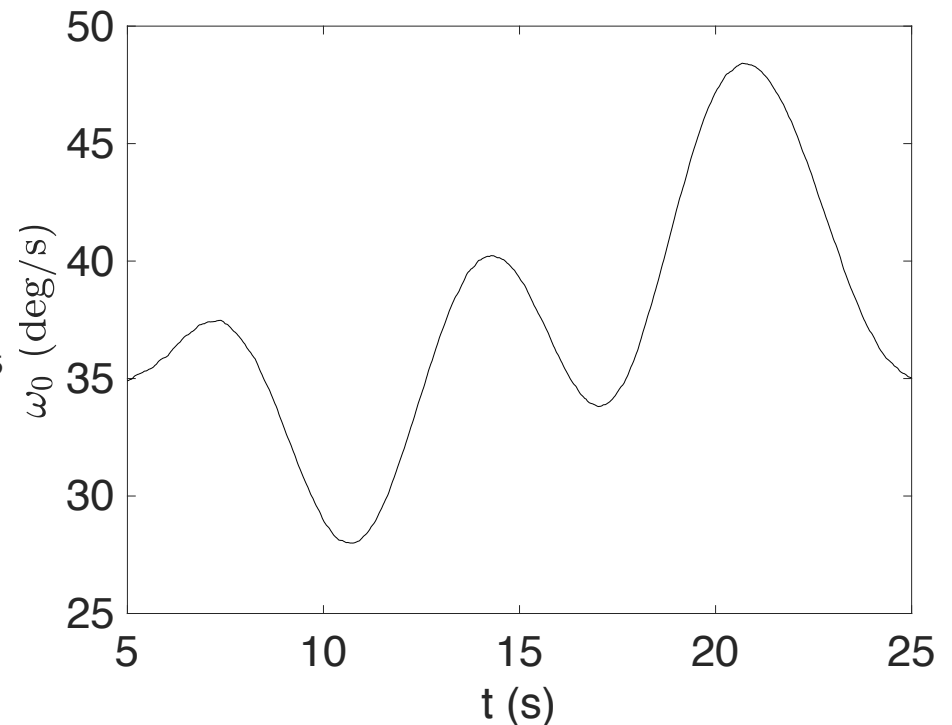
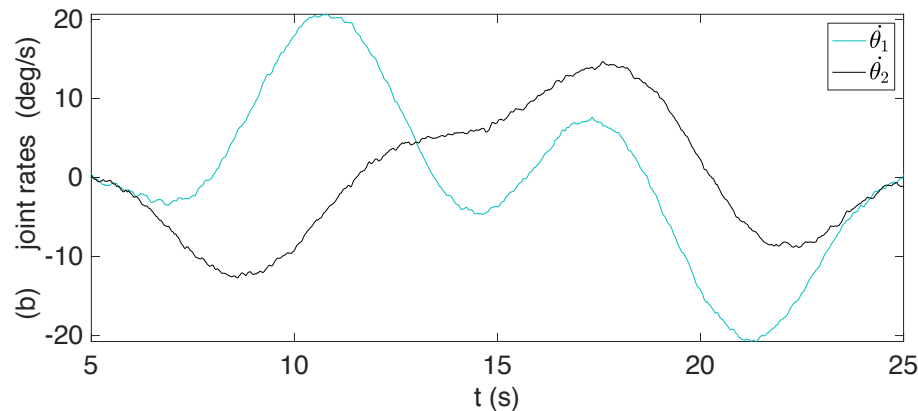
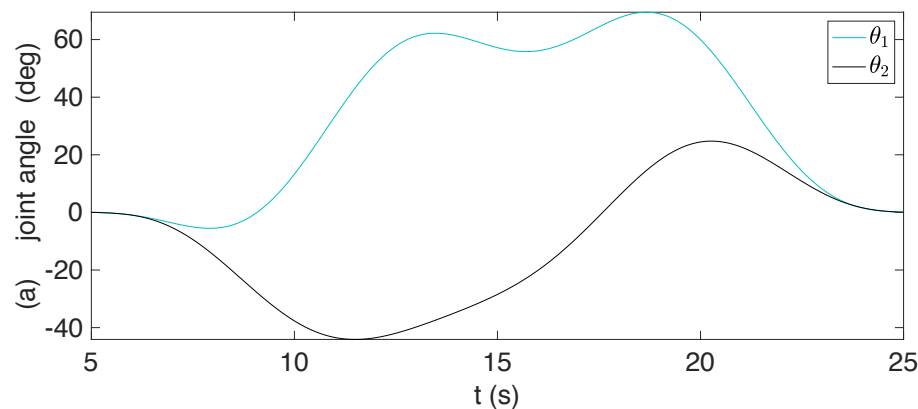
SYSID Measurements Required	Sensor	Unit
S/C angular velocity	IMU	rad/s
S/C linear velocity	Computed	m/s <sup>2</sup>
Manipulator joint angles	Motor encoders	rad
Manipulator joint rates	Computed	rad/s



# BP1A: Excitation & simulated response

□ **RW PI Control** on  $\dot{\theta}_{rw,des} = 150 \text{ rad/s} = 1432.4 \text{ rpm}$

□ **Manipulator PD control** on  $\theta_{i,des}$  -> Fourier series: coefficients obtained by minimizing regressor matrix condition number

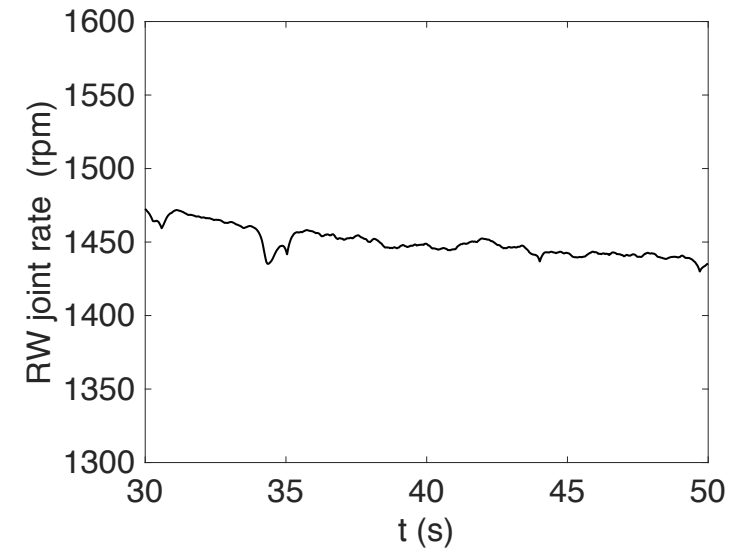
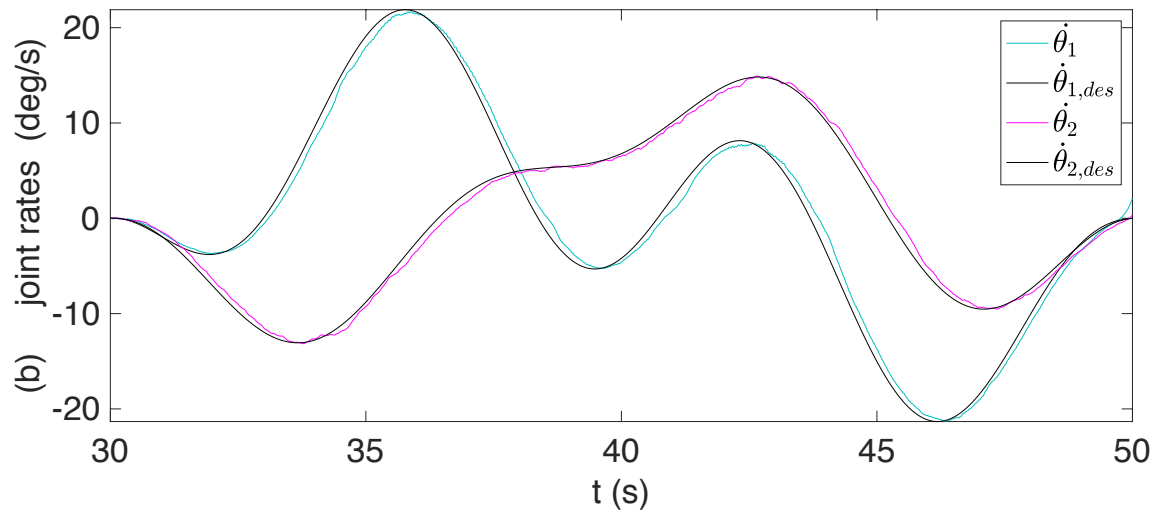
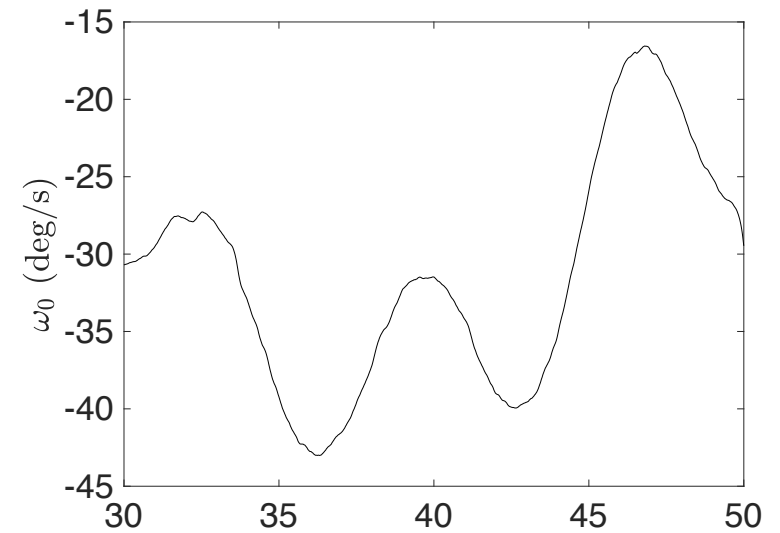
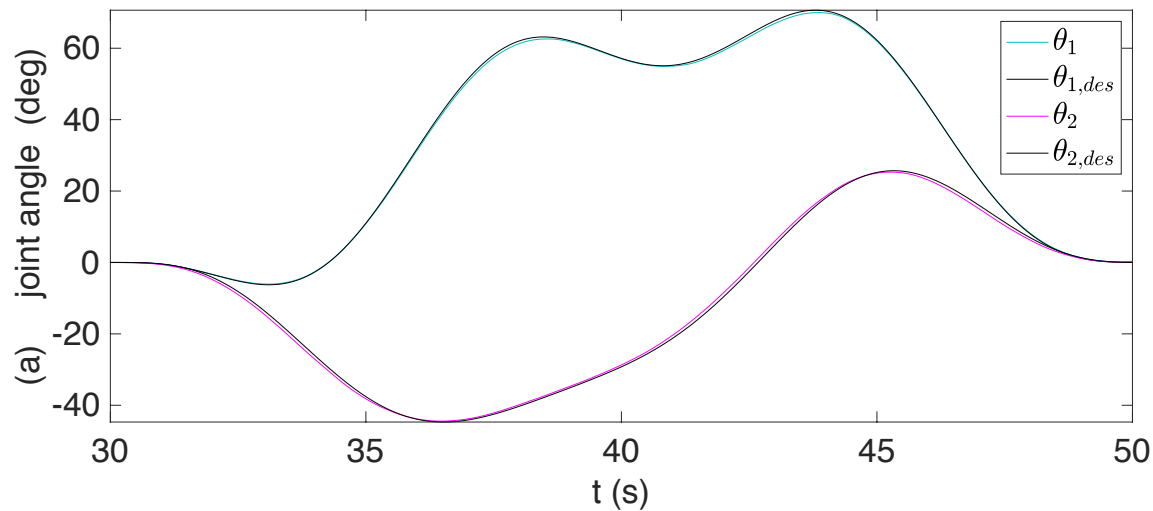


# BP1A: SYSID Results (simulation)

Parametric SYSID by TLS (Algorithm) on Angular Momentum Conservation (Method)

Parameter	True Value	Estimated Value	Relative error (%)
$a_1$	0.041	0.038	<b>5.819</b>
$a_2$	0.014	0.014	2.57
$a_3$	0	-0.0008	-
$a_4$	0	-0.0001	-
$a_5$	0.200	0.202	0.779
$a_6$	0.033	0.033	0.107
$a_7$	0.087	0.089	2.498
$a_8$	0.025	0.024	1.703

# BP1A: Excitation & experimental response



# BP1A: SYSID Results (experiment)

Parameter	Estimated Value
$a_1$	0.030
$a_2$	0.024
$a_3$	-0.032
$a_4$	0.044
$a_5$	0.248
$a_6$	0.015
$a_7$	0.09
$a_8$	0.109

- The “true” system parameters can be obtained by the system detailed CAD drawings
- Discrepancies do exist between the CAD and the real system
- It is more appropriate that the validity of the identified model to be evaluated using the validation strategy described next

# BP1A: Modelling Validation

- Identification Experiment: **Experimental vs. Simulated Setup**

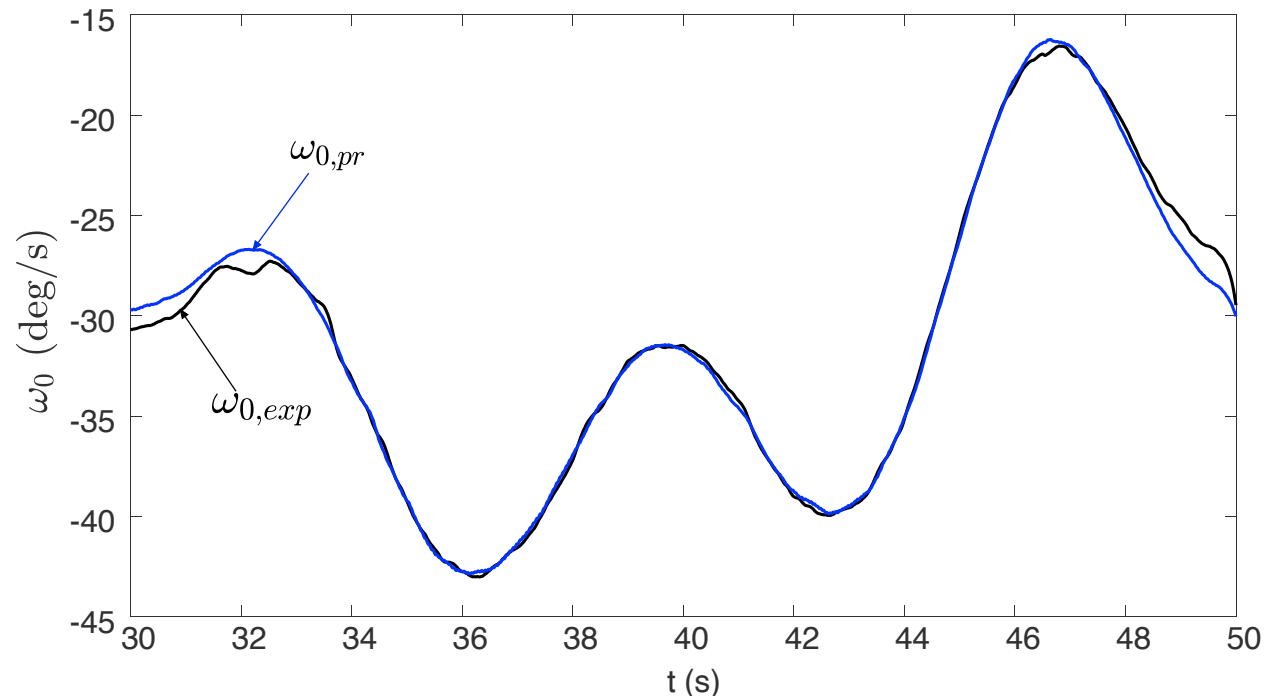
- Same excitation

- Qualitative comparison:  $\omega_{0,exp}$  vs.  $\omega_{0,pr} = D^{-1}(-I_{rw} \dot{\theta}_{rw} - \mathbf{D}_q \dot{\theta})$

- Simulated model is based on identified values

- Very good match**

- The identified parameters can be used to reconstruct the system motion

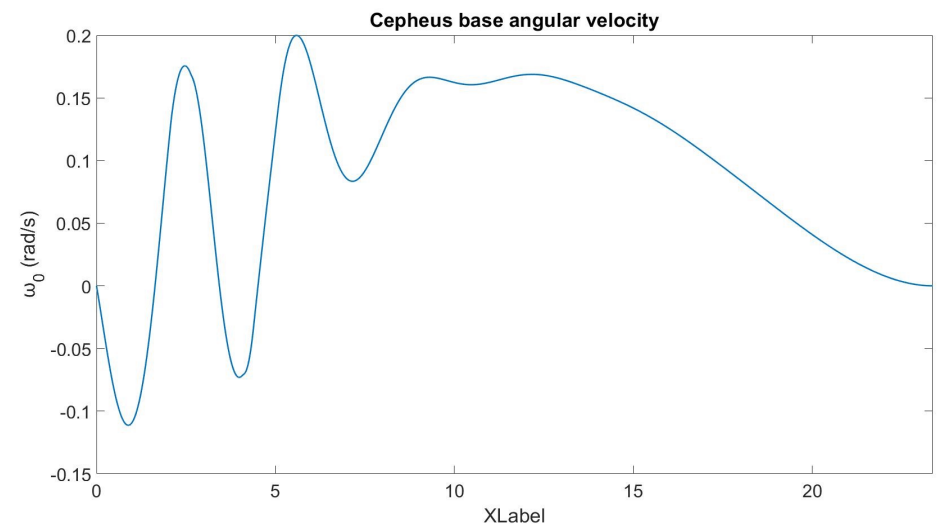
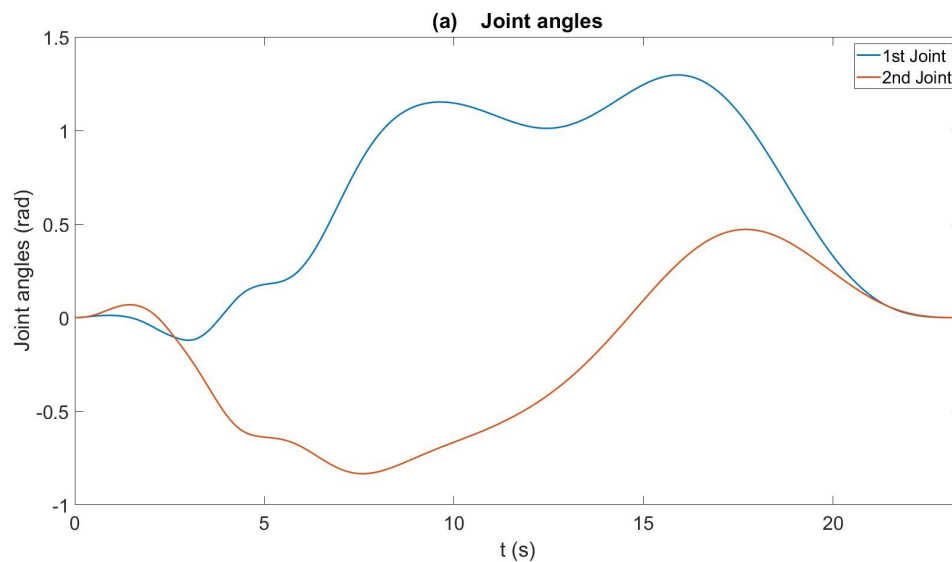


# BP1A: Discussion

- **Simulated data:** Parametric SYSID (Agular Momentum & TLS)
  - Results within (or marginally outside in a single case) the acceptable relative error margin of 5%
  - The execution of the BP1A **simulated experiment** is deemed as **successful**
  
- **Experimental data:** Parametric SYSID (Agular Momentum & TLS)
  - Though some parameter clusters were identified **acceptably**, others were identified with **somewhat large relative errors**
  - However, system **reconstruction** based on the identified parameters with the experimental data, was **successful**
  - **Simulated** identified system response matching the **experimental** system response **very well**

# BP1B: Excitation & simulated response

- Coordinated model-based PD control for Cepheus base position and attitude, and manipulator configuration
  - Cepheus position desired trajectory: **sinusoidal in x-y plane**
  - Cepheus attitude desired trajectory: **5<sup>th</sup> order polynomial**
  - Desired joint-angles trajectory: **Fourier series**



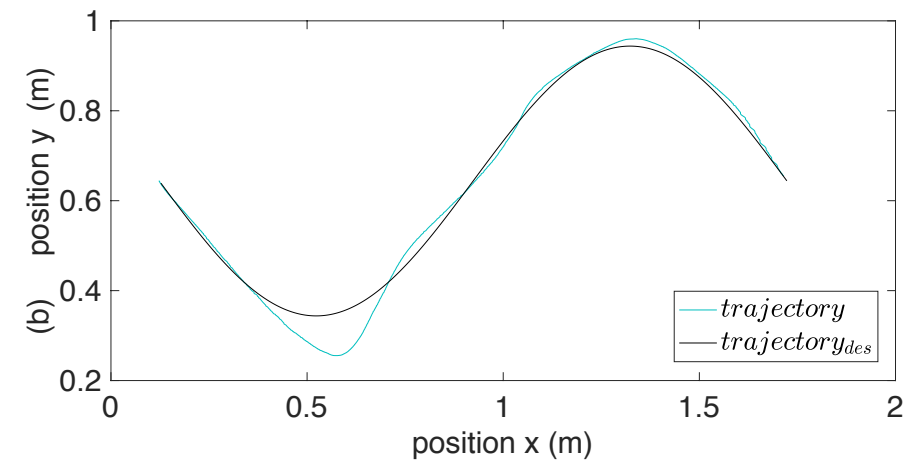
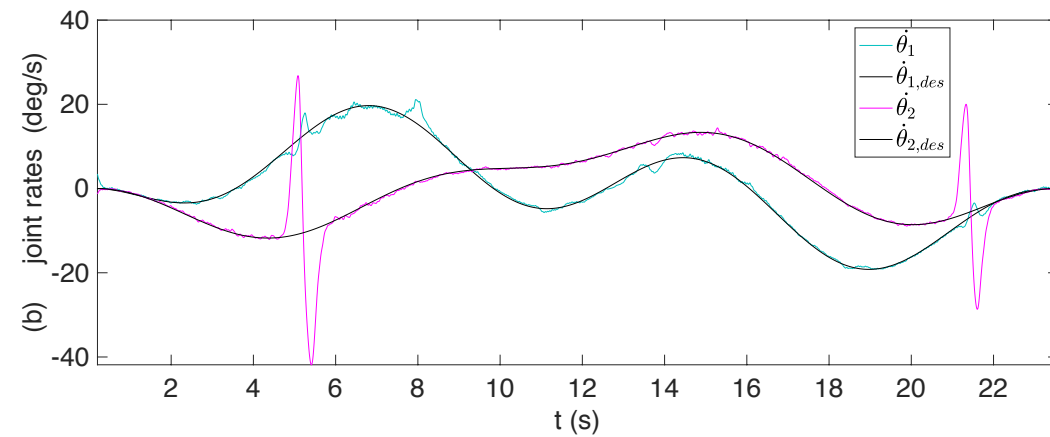
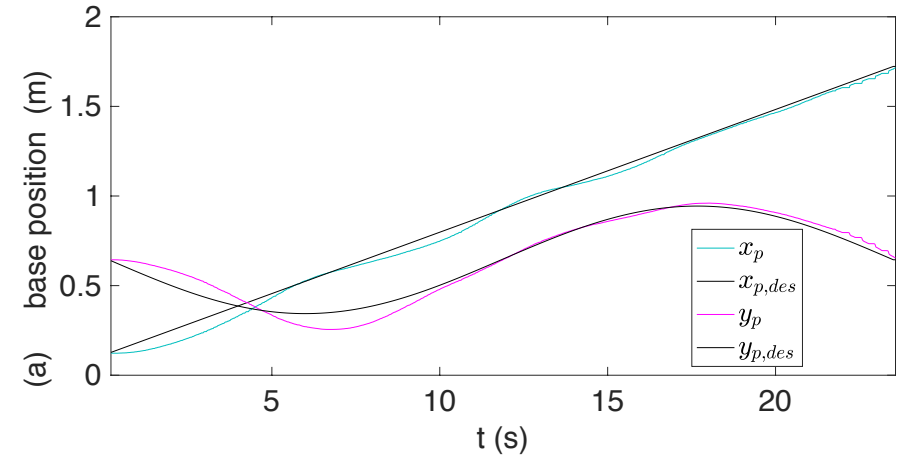
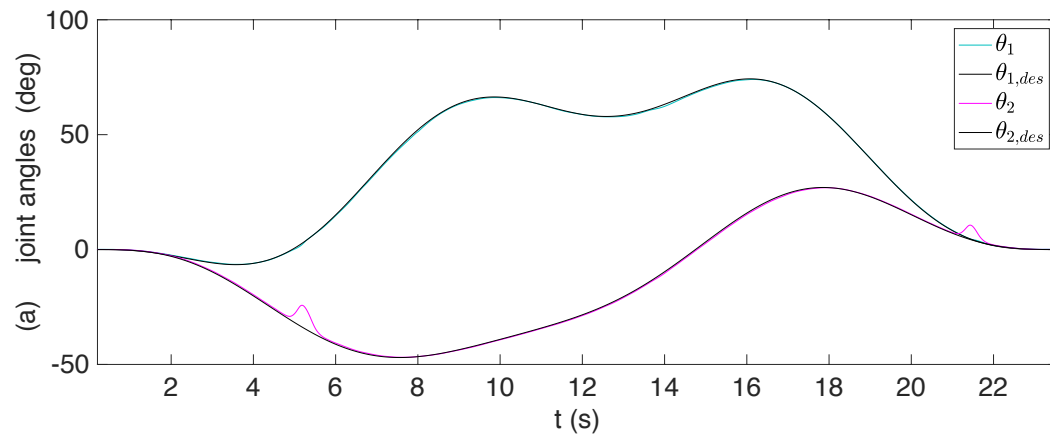
# BP1B: SYSID Results (simulation)

Parametric SYSID by [TLS](#) (Algorithm), [Energy Balance Equation](#) (Method)

Parameter	True Value	Estimated Value	Relative error (%)
$a_1$	13.828	13.983	1.1213
$a_2$	2.1385	2.1734	1.6301
$a_3$	0	-0.074213	-
$a_4$	0.26194	0.25793	1.5325
$a_5$	0.093208	0.076095	<b>18.361</b>
$a_6$	0.90348	0.97262	7.6527
$a_7$	0.034487	0.046775	<b>35.631</b>
$a_8$	0.091739	0.087453	4.6718
$a_9$	0.025426	0.019914	<b>21.678</b>

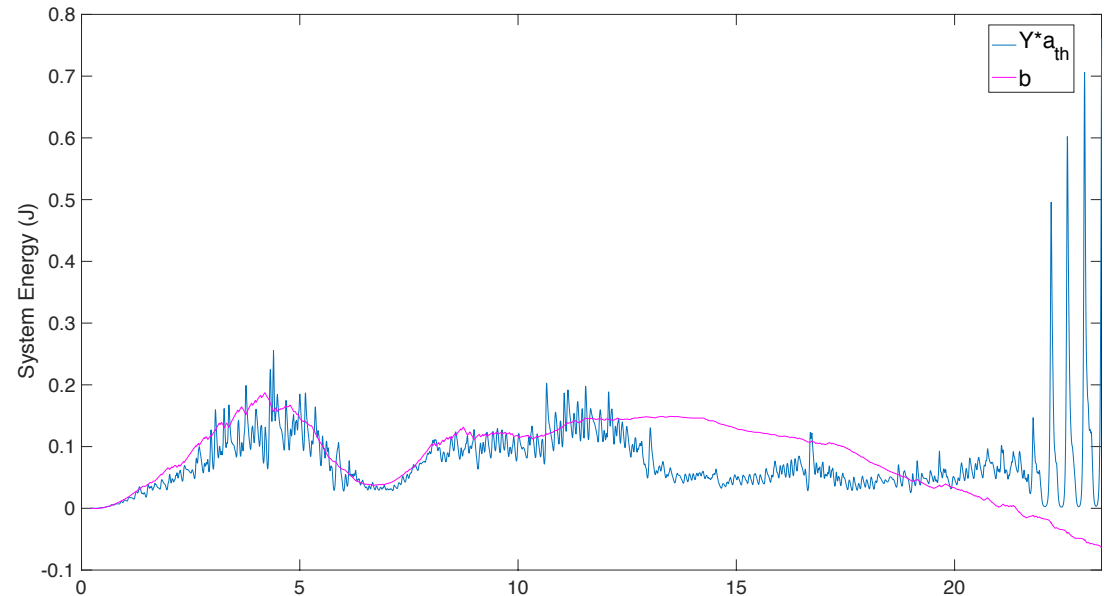


# BP1B: Excitation & experimental response



# BP1B: SYSID Results (experiment)

- The “true” system parameters can be obtained by the system detailed CAD drawings
- Results with data from the first 12s.



Parameter	Value from CAD	TLS Estimated Value Fmax=0.6N	TLS Estimated Value Fmax=0.42N
$a_1$	13.83	23.73	16.90
$a_2$	2.14	4.75	3.39
$a_3$	0.00	-5.95	-4.38
$a_4$	0.26	3.33	2.20
$a_5$	0.09	-1.25	-0.83
$a_6$	0.91	5.74	4.33
$a_7$	0.03	0.36	0.27
$a_8$	0.09	0.37	0.25
$a_9$	0.03	-0.56	-0.39

# BP1B: Modelling Validation

- ❑ Modelling for BP1B validated already in BP1A, except for the thrusters
  - Each thruster-valve pair has been calibrated and tested, using a high-quality ATI force/torque sensor
  - Thruster forces follow the command given
  - In prolonged use and when many of them fire simultaneously, their thrust may be reduced
  
- ❑ Modelling validation for BP1B is complete, except for thruster action consideration

# BP1B: Discussion

- **Simulated data:** Parametric SYSID (Energy Balance & TLS)
  - Most of the results within the acceptable relative error margin of 5%, or close to it (7.6%)
  - Three results with larger relative errors of 18.4%, 21.7% and 35.6%
  - Limitations in excitation and sensors result in marginal SNR
  
- **Experimental data:** Parametric SYSID (Energy Balance & TLS)
  - Most parameter clusters identified with **large relative errors**
  - Low **SNR**, comparison with **CAD “true” values**, and **inaccurate knowledge of the excitation force**, are the main reasons

# BP2: Full-scale Planar System (1/5)

## Model

2D Spacecraft (S/C) with mechanical equivalent model to represent sloshing effect

- **Sloshing Model:** mass-spring-damper to represent sloshing effect
- Sloshing parameters “true” values based on CFD model

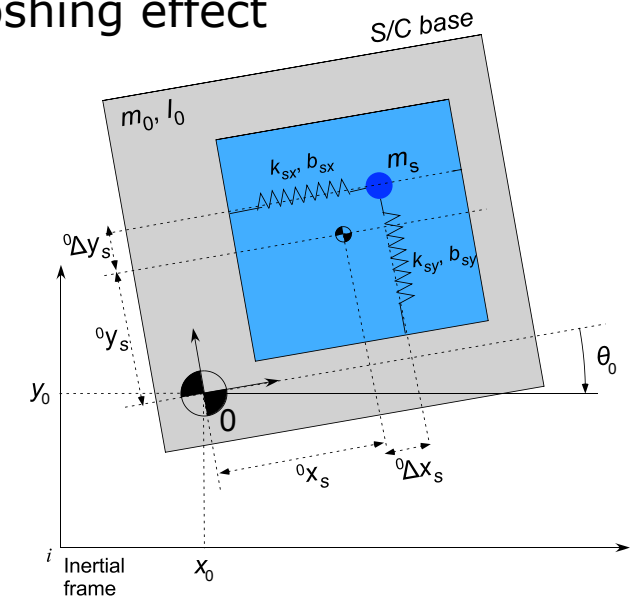
## Assumptions

- S/C inertial parameters assumed known
- S/C states are measurable

## Main challenge

- Sloshing parameters need to be identified in the presence of unmeasured states
- Sloshing states are not measurable

**Additional challenge:** Lack of existing methodologies



# BP2: Full-scale Planar System (2/5)

## Goal

Develop a method that overcomes the challenges and identifies the sloshing parameters

## Contribution

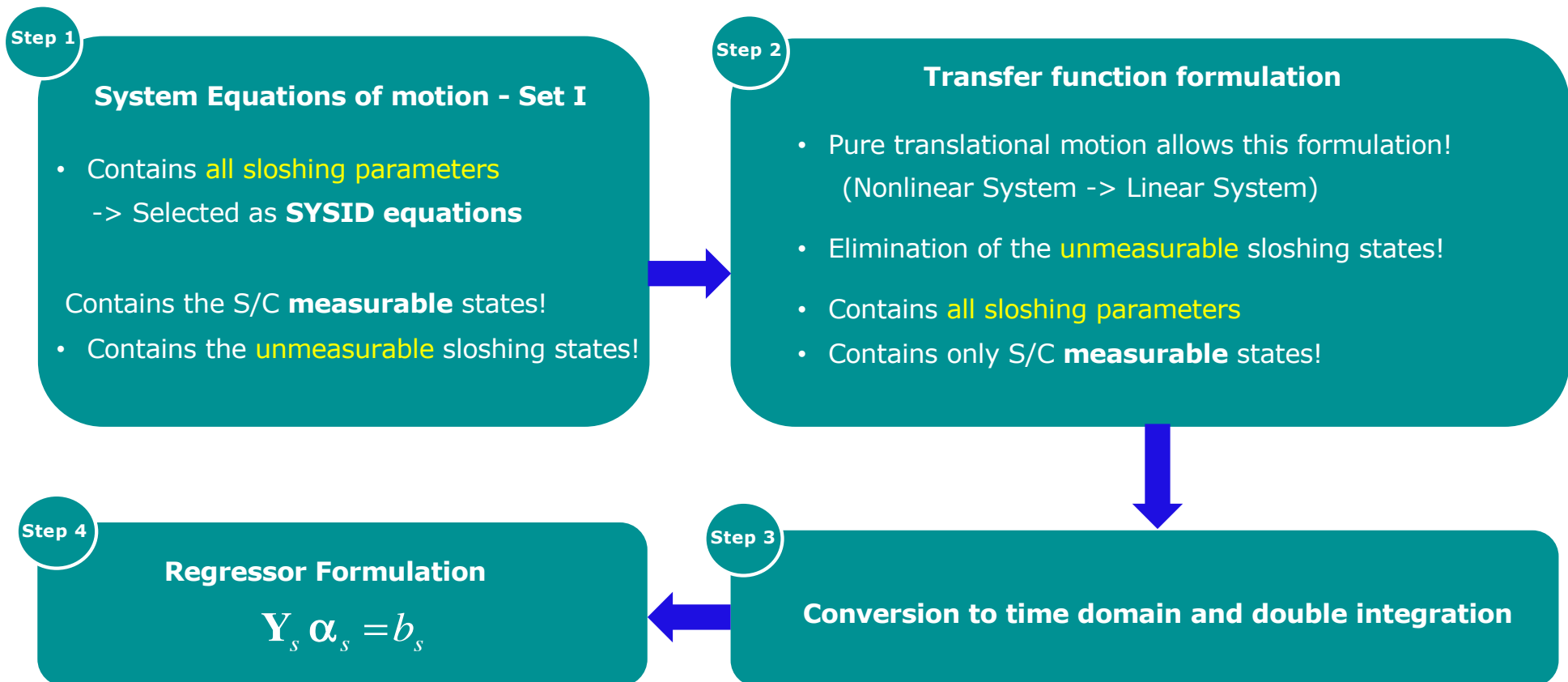
Development of **novel** methods M1, M2, M3 based on **regressor formulation**

## Design of sloshing SYSID Experiment

- Developed methods M1, M2, M3 eliminate the need for **unmeasurable** sloshing states
- In this presentation, focus on **M2**
- Pure translational motion of the system enables the **elimination**

# BP2: Full-scale Planar System (3/5)

## ■ Framework of novel method **M2**



# BP2: Full-scale Planar System (4/5)

## BP2 Methods and Algorithms

- ❑ TLS on regressor formulation-method M1 (M1-TLS)
- ❑ TLS on regressor formulation-method M2 (M2-TLS)
- ❑ TLS on regressor formulation-method M3 (M3-TLS)
- ❑ IV on regressor formulation-method M1 (M1- IV)
- ❑ IV on regressor formulation-method M2 (M2-IV)
- ❑ IV on regressor formulation-method M3 (M3- IV)
- ❑ UKF
- ❑ PEM

## Trade-off Analysis Results

The best algorithm and method combination for BP2 is **M2-TLS**.

- ❑ Max Rel. Error: 3.09%
- ❑ RMS Rel. Error: 2.59%



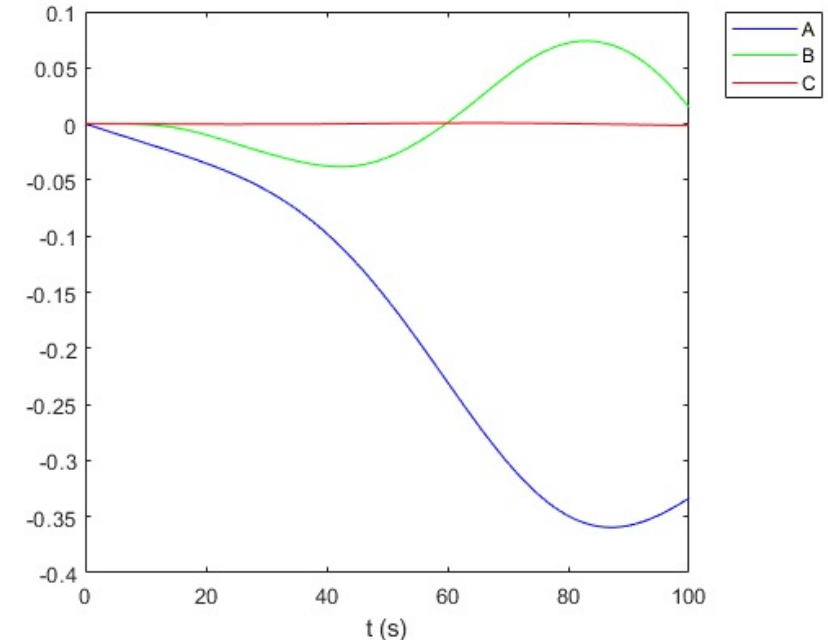
# BP2: Sensitivity Analysis

- If  $e$  is the difference between the response of a system based on the identified parameters and the response of the system with the “true” parameters, then

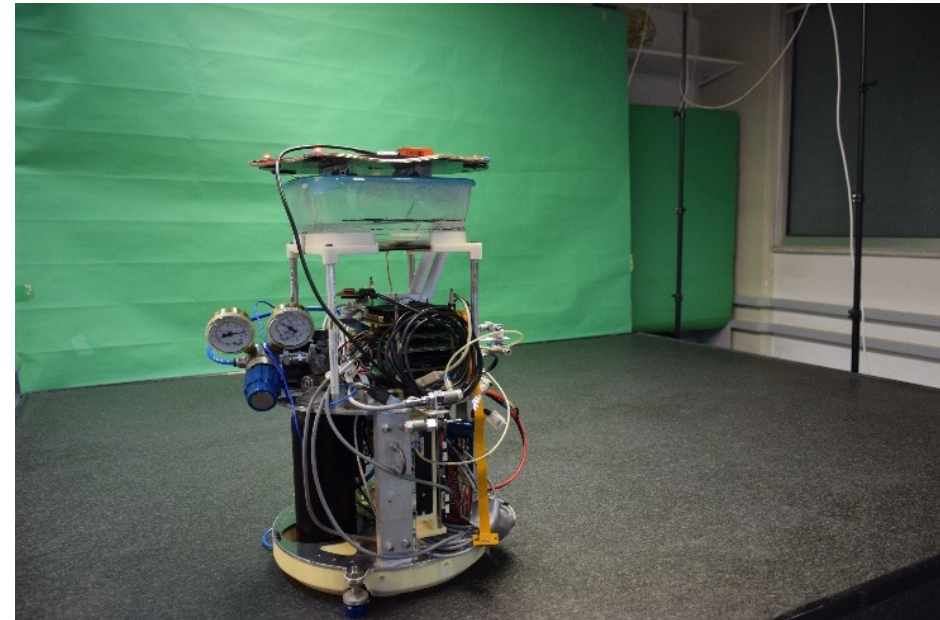
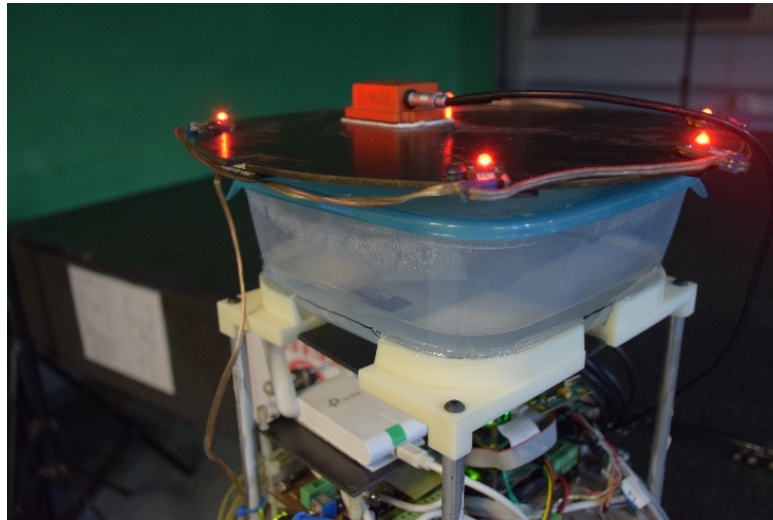
$$\begin{aligned} e &= {}^0x_0(t, m_s, k_{sx}, b_{sx}) - {}^0x_0(t, \bar{m}_s, \bar{k}_{sx}, \bar{b}_{sx}) \\ &= A(t)\varepsilon_m + B(t)\varepsilon_k + C(t)\varepsilon_b \end{aligned}$$

where  $\varepsilon_{m_s}$ ,  $\varepsilon_k$ ,  $\varepsilon_b$  are the relative errors of the identified sloshing parameters  $m_s$ ,  $k_{sx}$ ,  $b_{sx}$  respectively, and  $A(t)$ ,  $B(t)$  and  $C(t)$  are time-dependent coefficients

- Coefficient  $C(t)$ , has **negligible** effect



# BP2: Experimental Facility & Model (1/3)

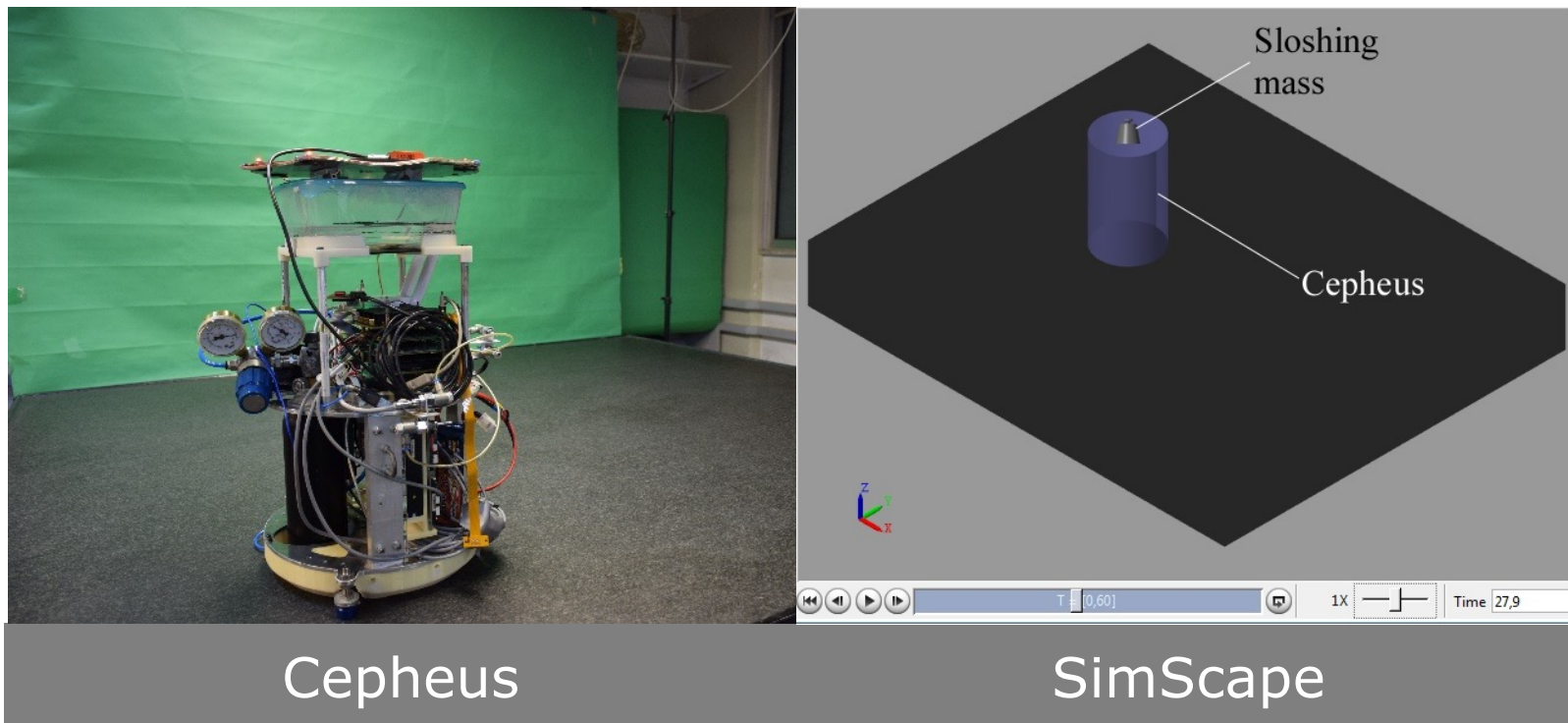


## ❑ No manipulator

Component	Mass	Notes
Robotic System w/o Manipulator	14 kg	N/A
Robotic System w/t Manipulator	15 kg	N/A
Empty plastic Tank	500 g	N/A
"Fuel" (water)	800 g	N/A
CO <sub>2</sub> Tank (empty) CO <sub>2</sub> Tank (full)	800 g 1500 g	Working pressure: 7 bar

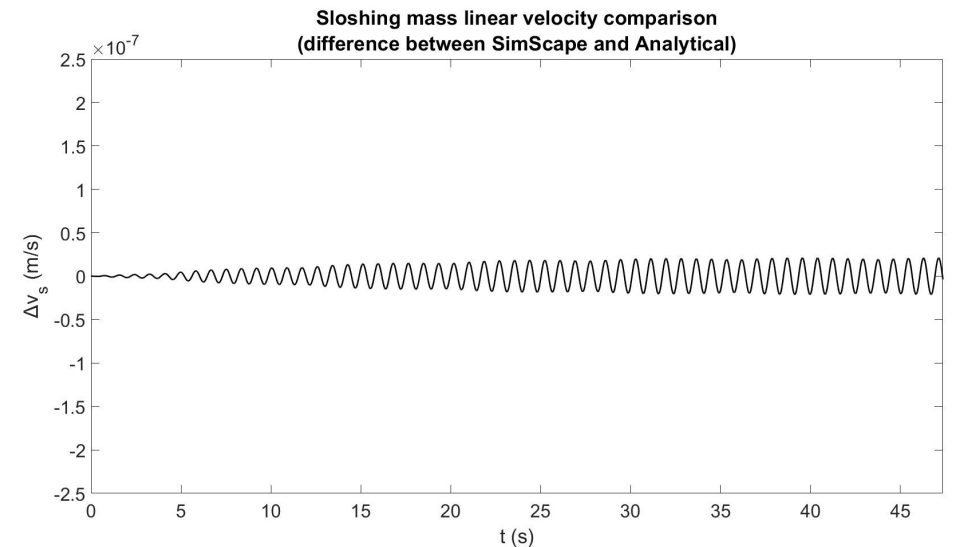
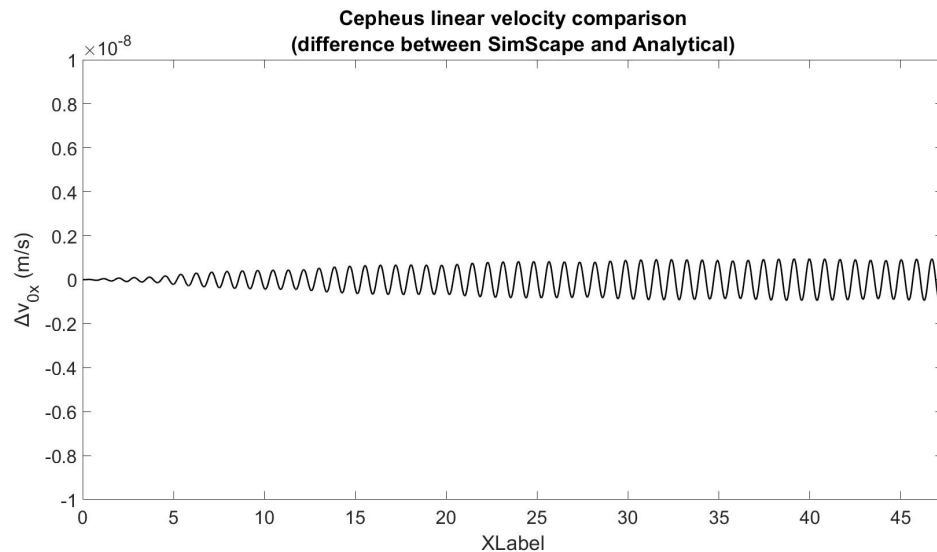
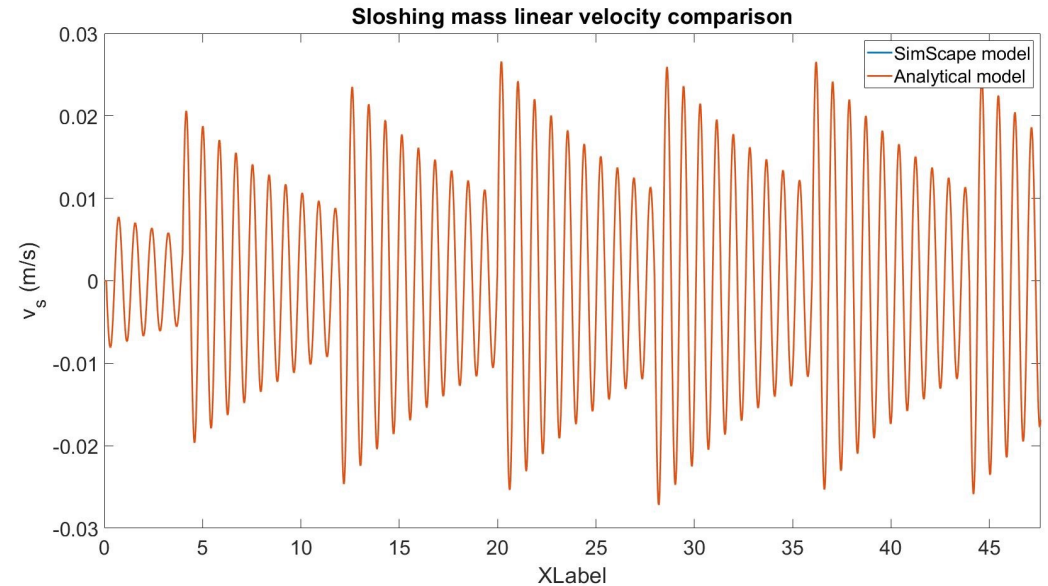
# BP2: Experimental Facility & Model (2/3)

- Inertial parameters, sensors and actuators: those of Cepheus
- Mass-spring-damper parameters in accordance with CFD model

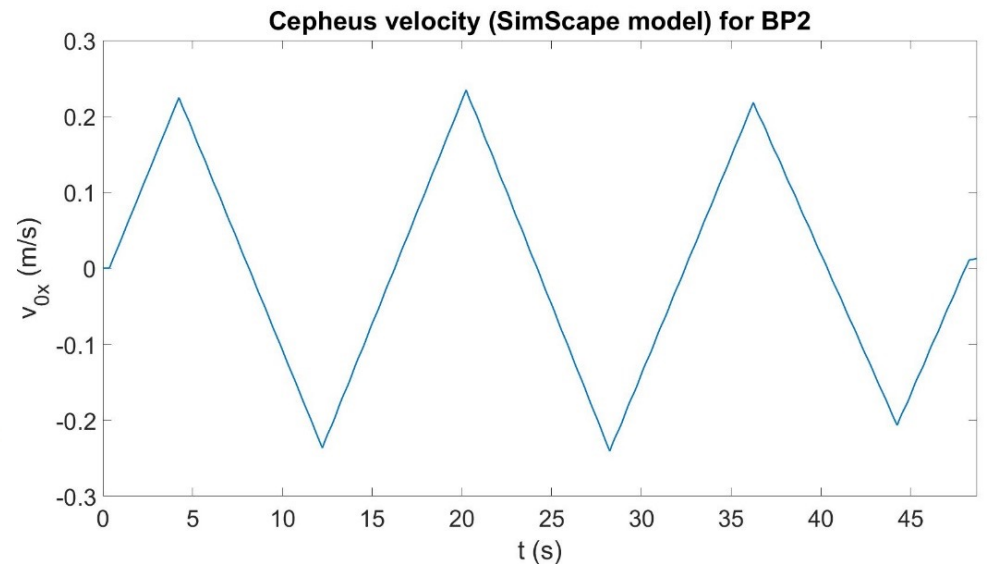
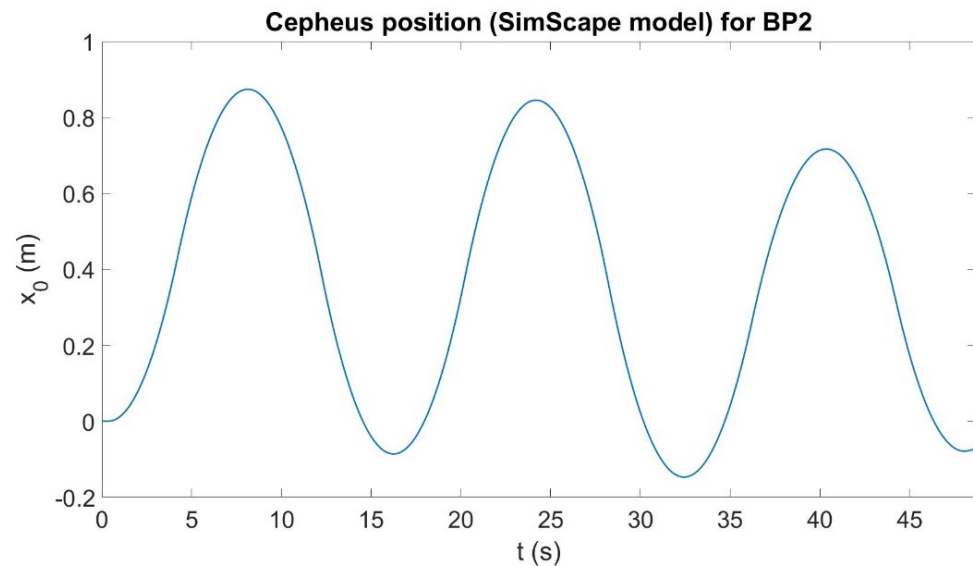
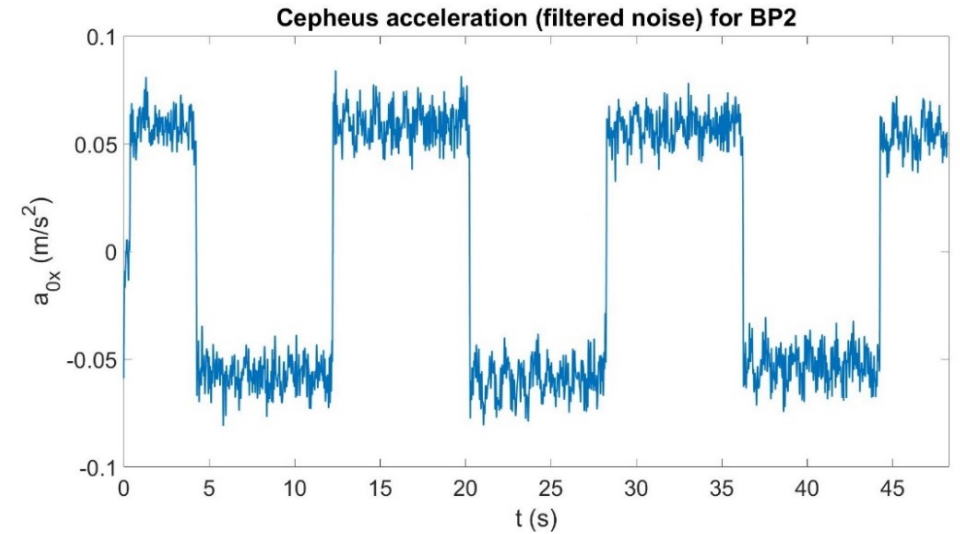
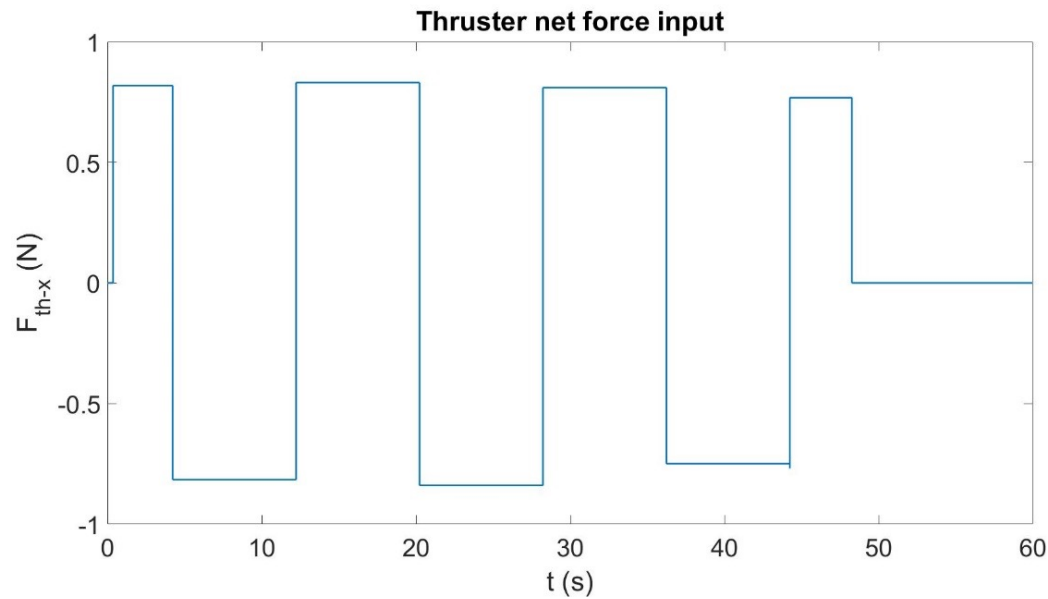


# BP2: Experimental Facility & Model (3/3)

- Compared model response of
  - Analytical vs. Simscape
  - Same excitation
- Responses identical => analytical model **verified**



# BP2: Excitation & simulated response



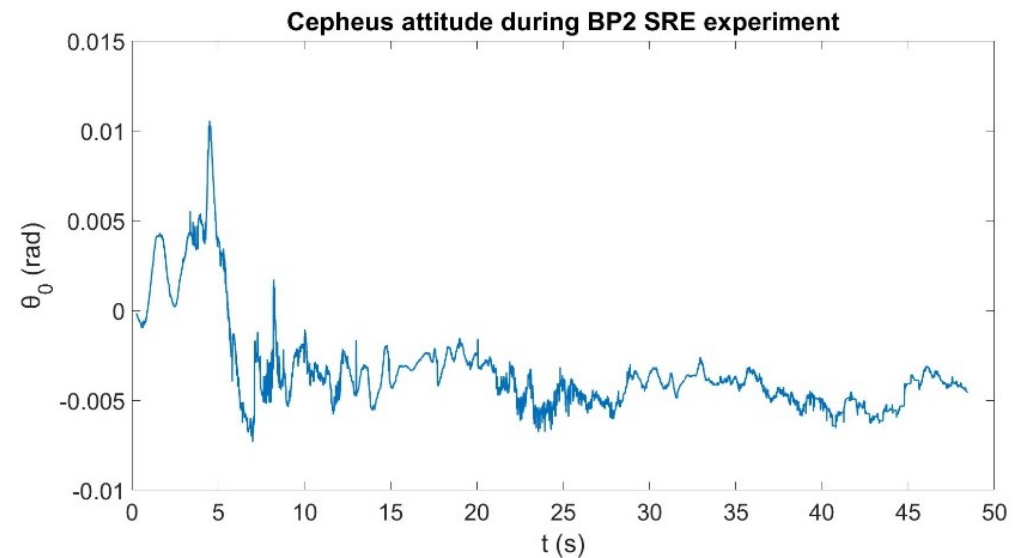
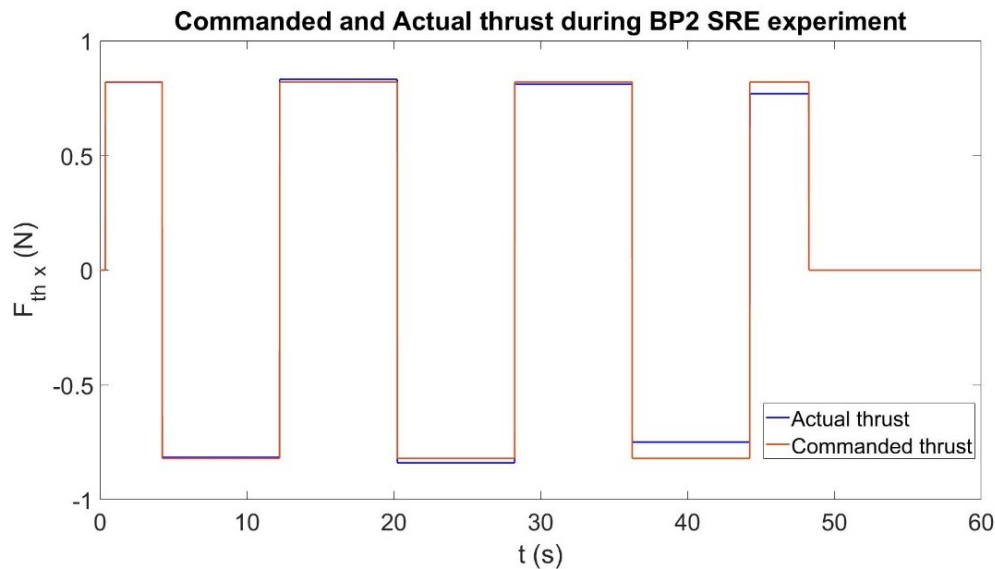
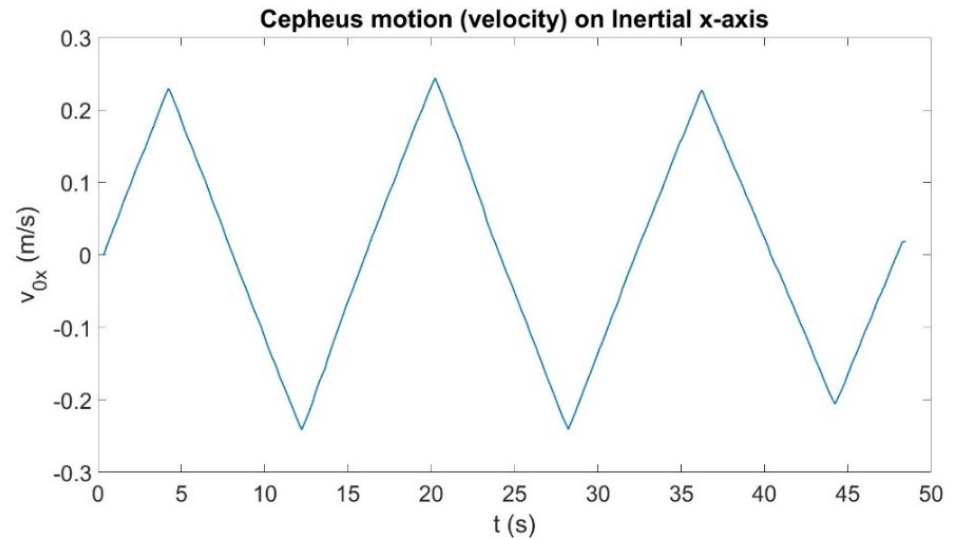
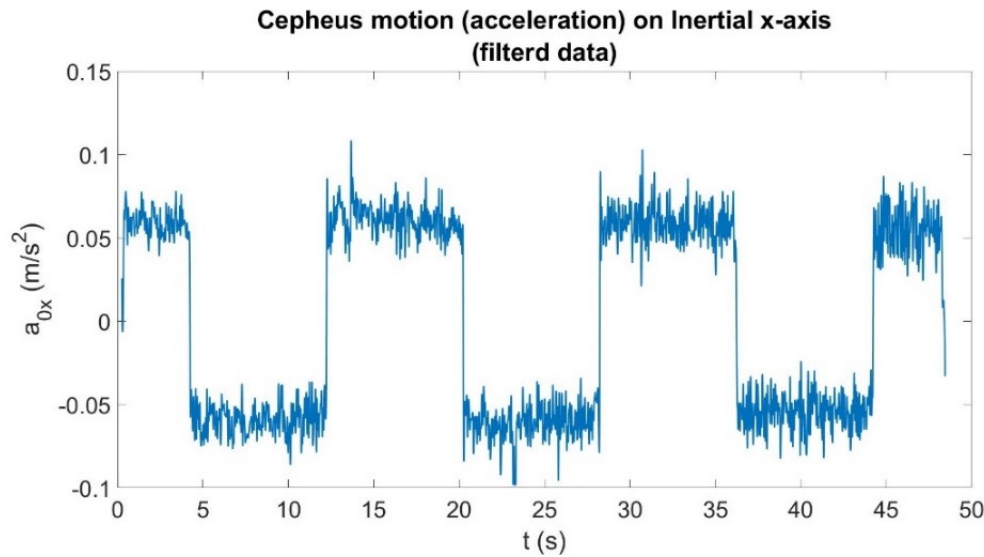
# BP2: SYSID Results (simulation)

Parametric SYSID: TLS (Algorithm), System Transfer Function (Method)

Parameter	True Value	Estimated Value	Relative error (%)
$k_s$ (N/m)	33.2156	13.6968	2.27
$b_s$ (N*s/m)	0.1336	-115.56	-
$m_s$ (kg)	0.650	1.183	<b>8.59</b>



# BP2: Excitation & experimental response



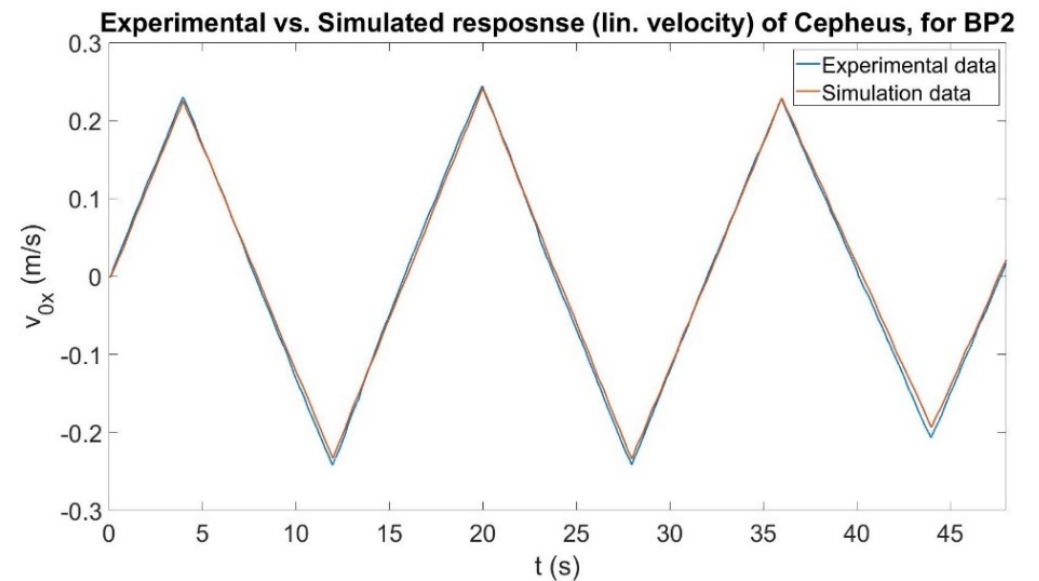
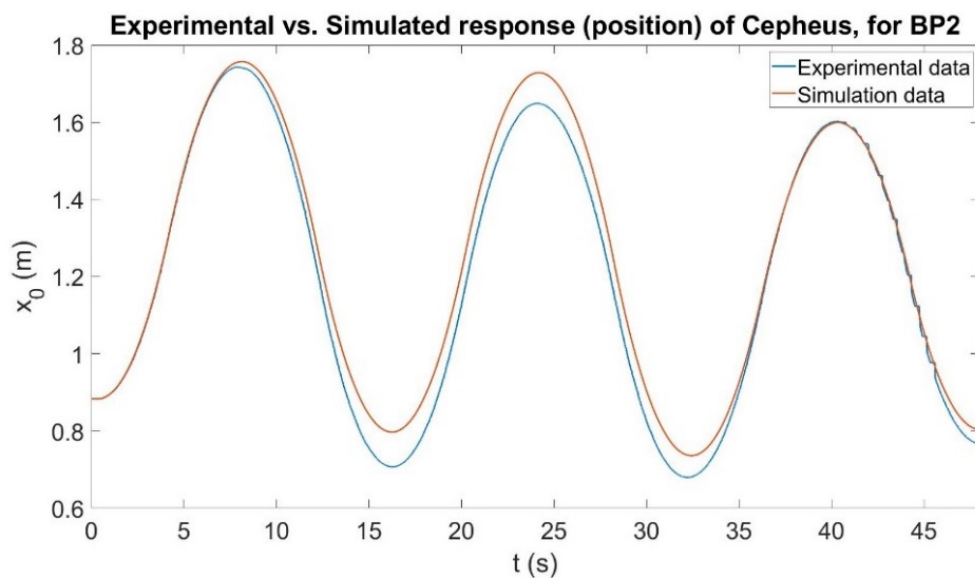
# BP2: SYSID Results (experiment)

Parameter	"True" Value	Estimated Value	Relative error (%)
$m_s$ (kg)	0.650	0.402	<b>20.32</b>
$k_s$ (N/m)	33.2156	13.44	<b>10.32</b>
$b_s$ (N/m/s)	0.1336	-46.17	-



# BP2: Modelling Validation

- Identification Experiment: **Experimental vs. Simulated Setup**
  - **Same** excitation
  - **Qualitative** comparison
- Simulated model based on identified values
- **Very good match**



# BP2: Discussion

## □ Simulated data: Parametric SYSID (TF Method & TLS)

- Damping coefficient not adequately identified (expected), while the other two sloshing model parameters are identified with relative errors **within or close** to the 5% margin
- The execution of the BP2 **simulated experiment** is deemed as **successful**

## □ Experimental data: Parametric SYSID (TF Method & TLS)

- Identified sloshing mass and stiffness of the sloshing model are meaningful but errors outside the 5% limit
- “True” values are obtained by CFD model and fitting on a mass-spring-damper model
- Sloshing mass excitation is close to the acceleration noise levels  
-> difficult to decipher from noise

# BP3: Full-scale Planar System (1/2)

## 2D Model

- ❑ Rotating rigid hub with a flexible appendage mounted on a fixed revolute joint
- ❑ Appendage deflection as a function of the modal shapes

## Modelling Assumptions

- ❑ Hub Model: Rigid body
- ❑ Flexible appendage: Continuous model (Euler-Bernoulli beam)

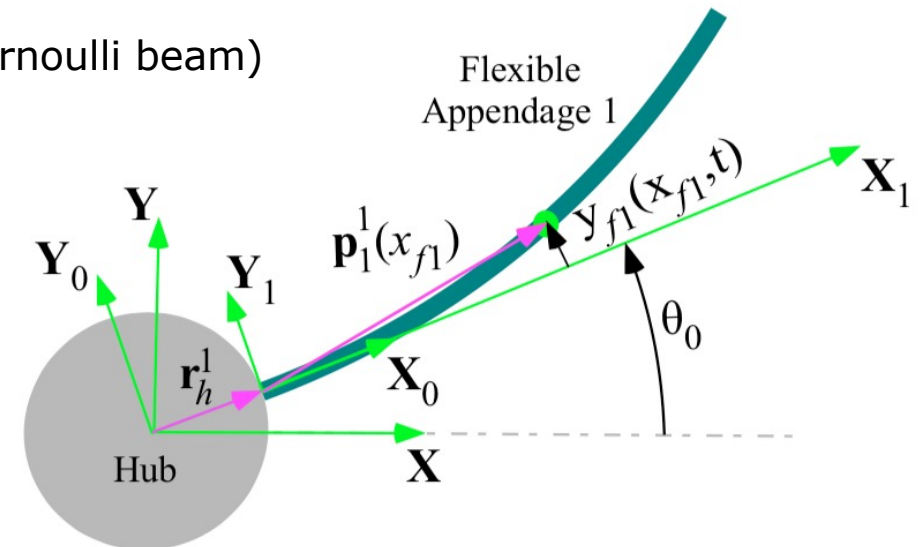
## Goal

Estimation of modal parameters of the appendage

- ❑ Natural frequencies
- ❑ Damping ratios
- ❑ Mode shapes

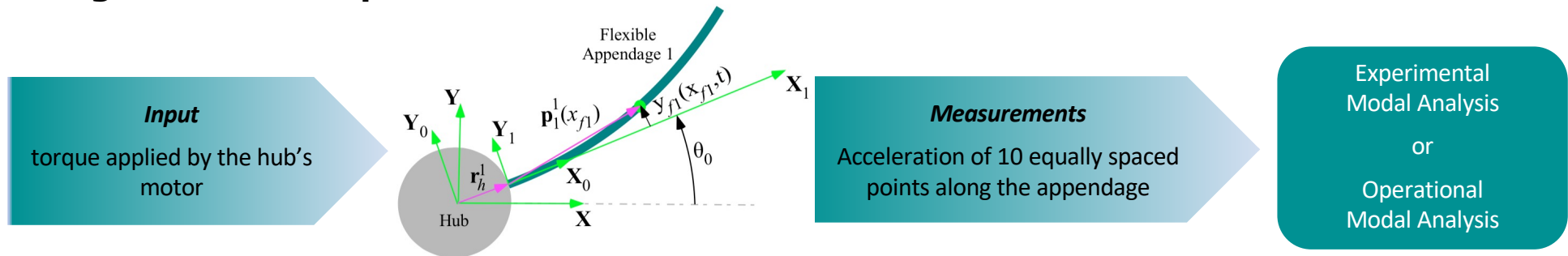
## Cases

- ❑ Experimental Modal Analysis (BP3A): chirp and rectangular signals selected as inputs
- ❑ Operational Modal Analysis (BP3B): specific operational task selected



# BP3: Full-scale Planar System (2/2)

## Design of SYSID Experiment



## Algorithms evaluated

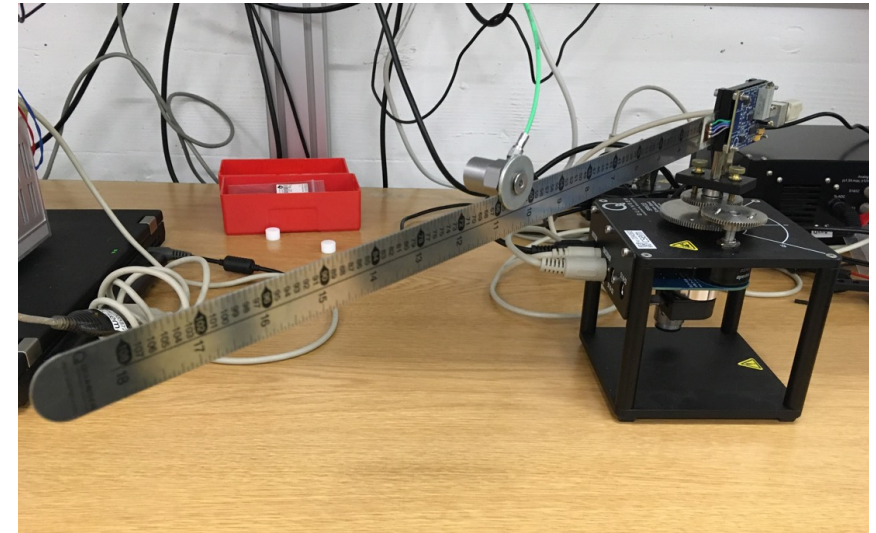
- LSCE
- RFP
- FSDD
- SSI-COV
- SSI-DATA

## Trade-off Analysis Results

The best algorithm for BP3 is **SSI-COV**, for both EMA and OMA cases.

- ❑ Rectangular input signal yields better results than chip signal
- ❑ Relative errors for all modal parameters are quite low
  - Max Rel. Error in Natural Frequencies: 0.02%
  - Max Rel. Error in Damping Ratios: 0.01%
  - MAC Value: 1

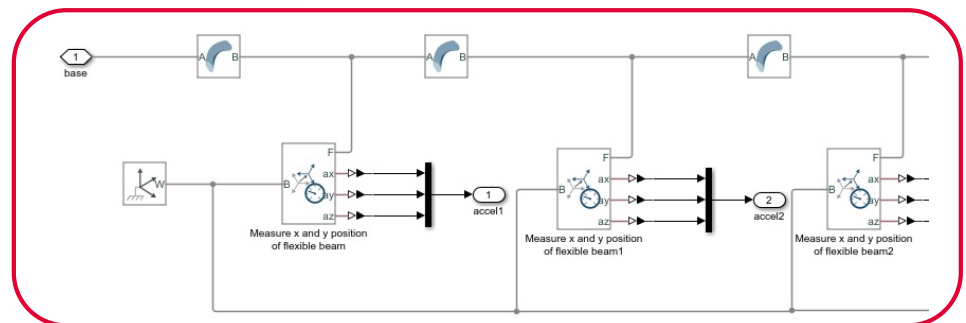
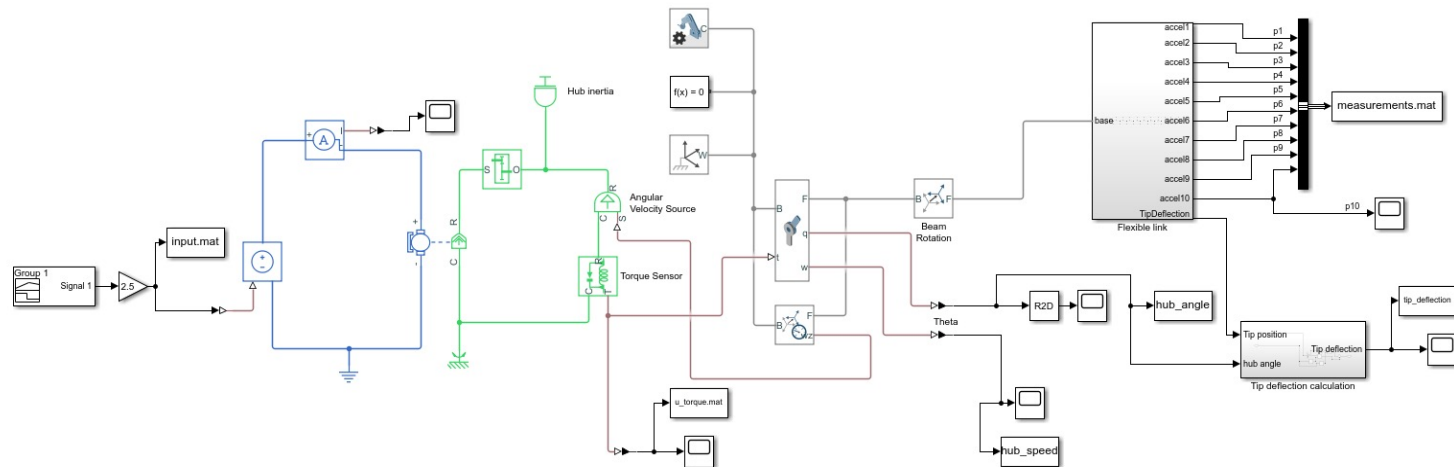
# BP3: Experimental Facility & Model (1/4)



Characteristics	Quanser flexible link	SYSID Measurements Required	Sensor	Unit
Length	40 cm	Hub attitude	Hub motor encoder	rad
Height	2.1 cm			
Thickness	0.09 cm	Linear accel. of points on flexible appendage	Accelerometers	m/s <sup>2</sup>
Flexible link mass	69.7 g			
Young's modulus	193 GPa			
Density (stainless steel)	7850 kg/m <sup>3</sup>			

# BP3: Experimental Facility & Model (2/4)

- SimScape model: succession of 10 flexible beams, with acceleration measurements between them
  - Inertial parameters, sensors, and actuators by [Quanser](#)

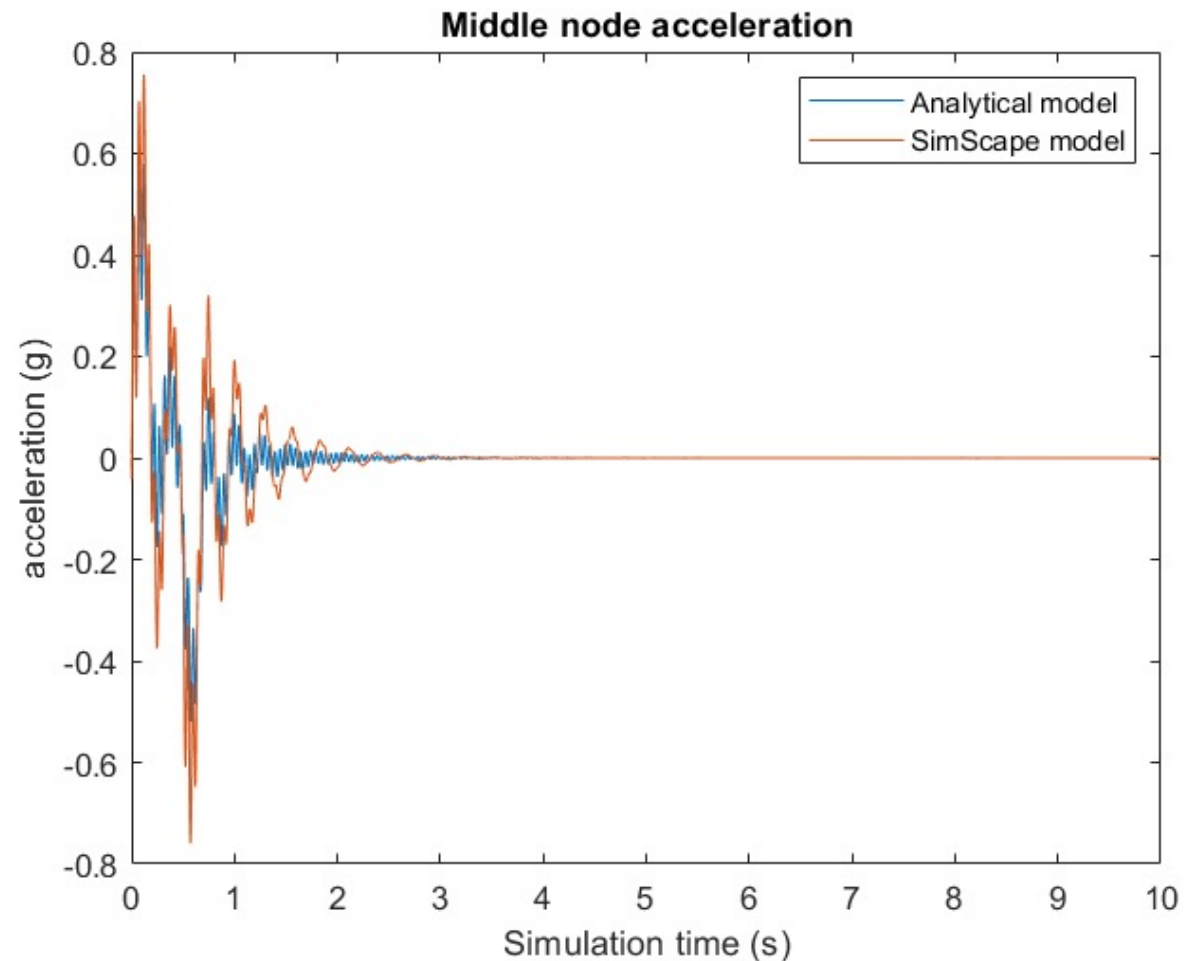


# BP3: Experimental Facility & Model (3/4)

□ Compared model response of

- Analytical vs. Simscape
- **same** excitation

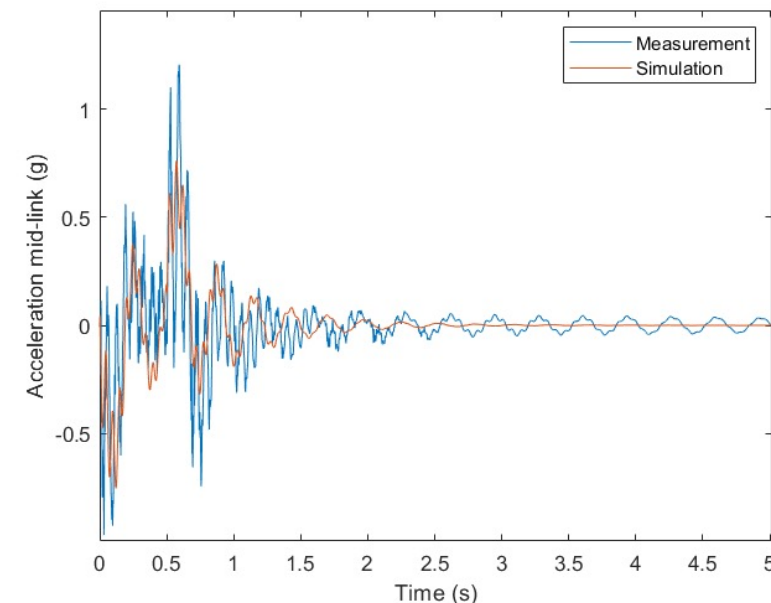
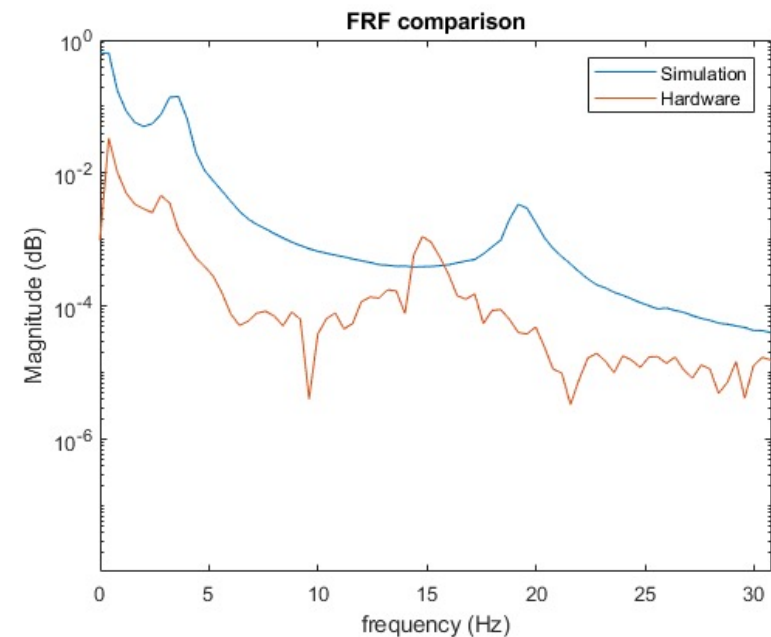
□ Responses very close =>  
analytical model **verified**



# BP3: Experimental Facility & Model (4/4)

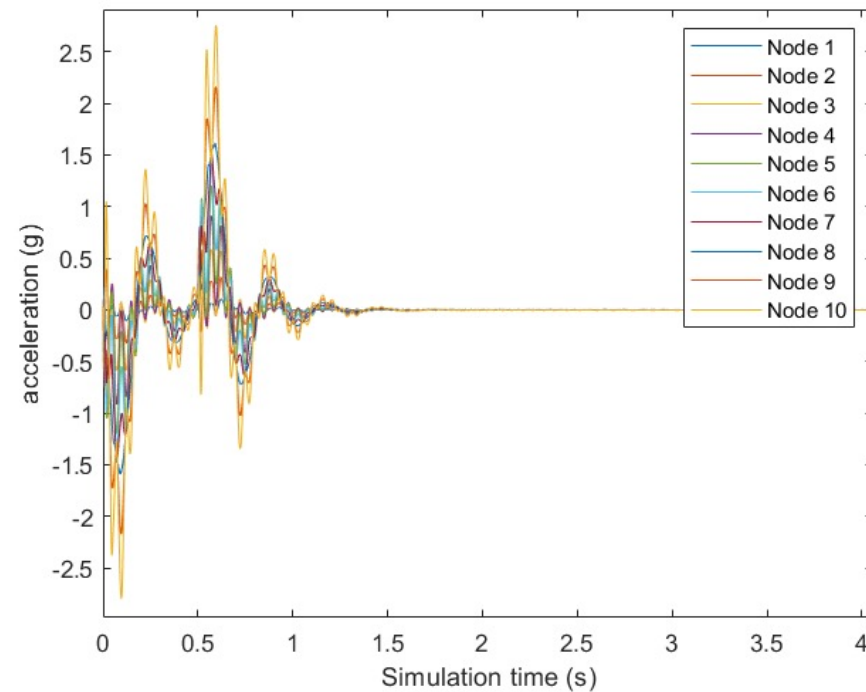
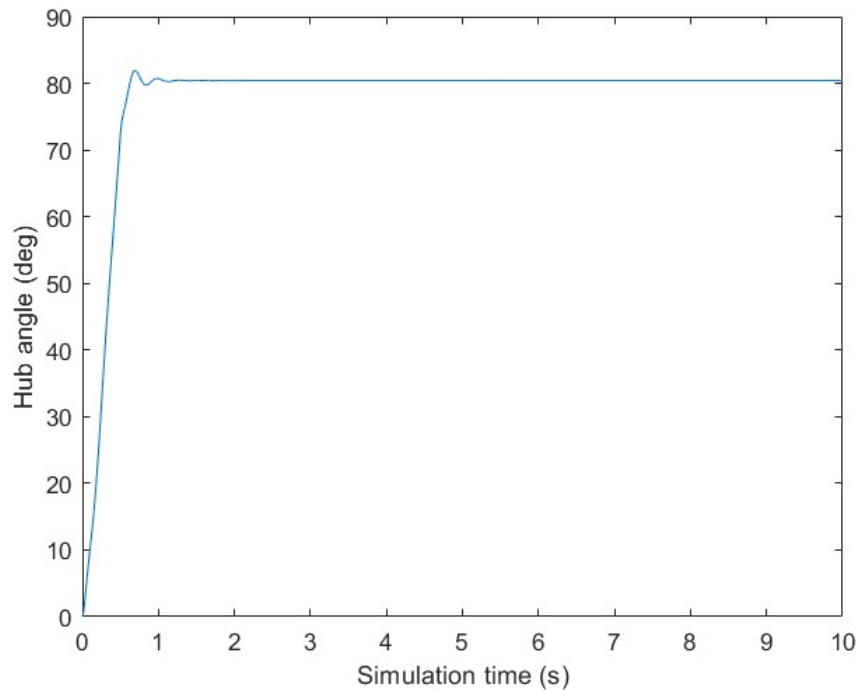
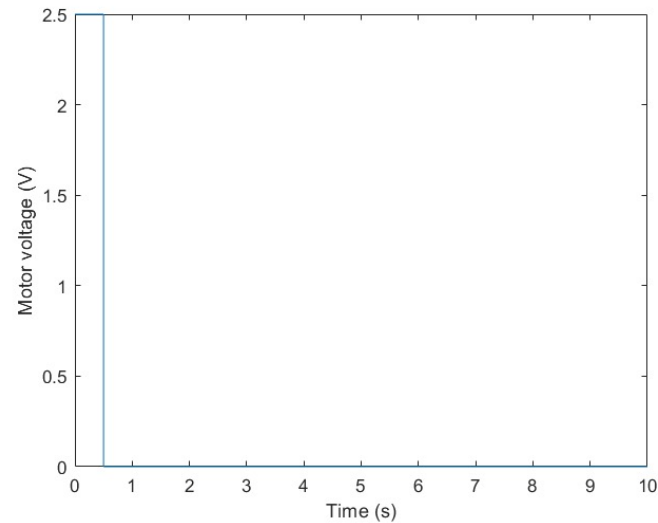
## □ Modelling Validation

- Identification Experiment: Experimental vs. Simulated Setup
  - Same excitation
  - Qualitative comparison
- Simulated model used CAD values
- Modelling validated
- Some discrepancies exist due to:
  - Damping modelling limitations
  - Intrinsic H/W-S/W differences





# BP3A: Excitation & simulated response



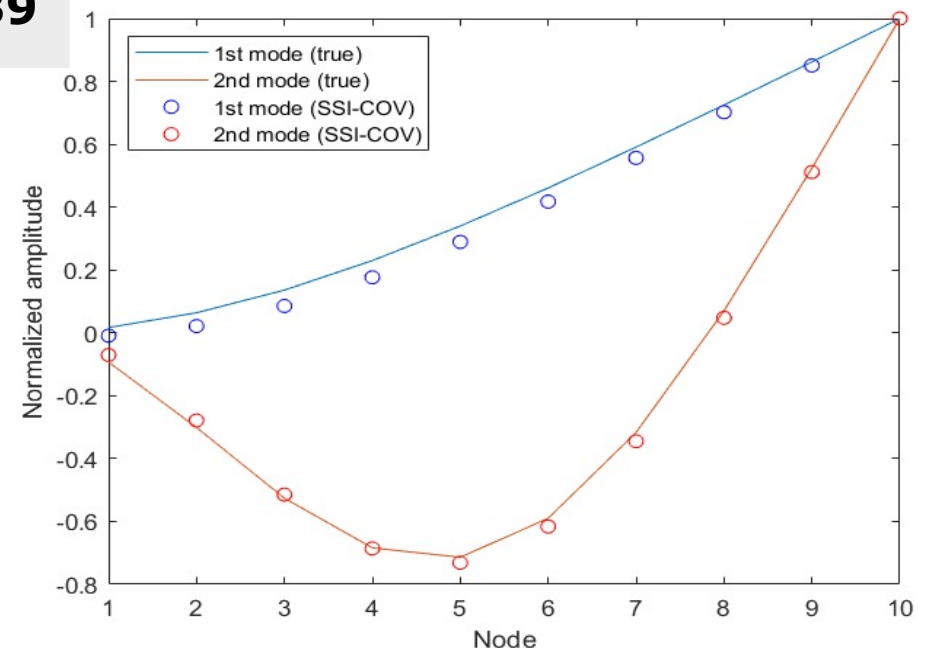
# BP3A: SYSID Results (simulation)

## Modal Analysis by SSI-COV

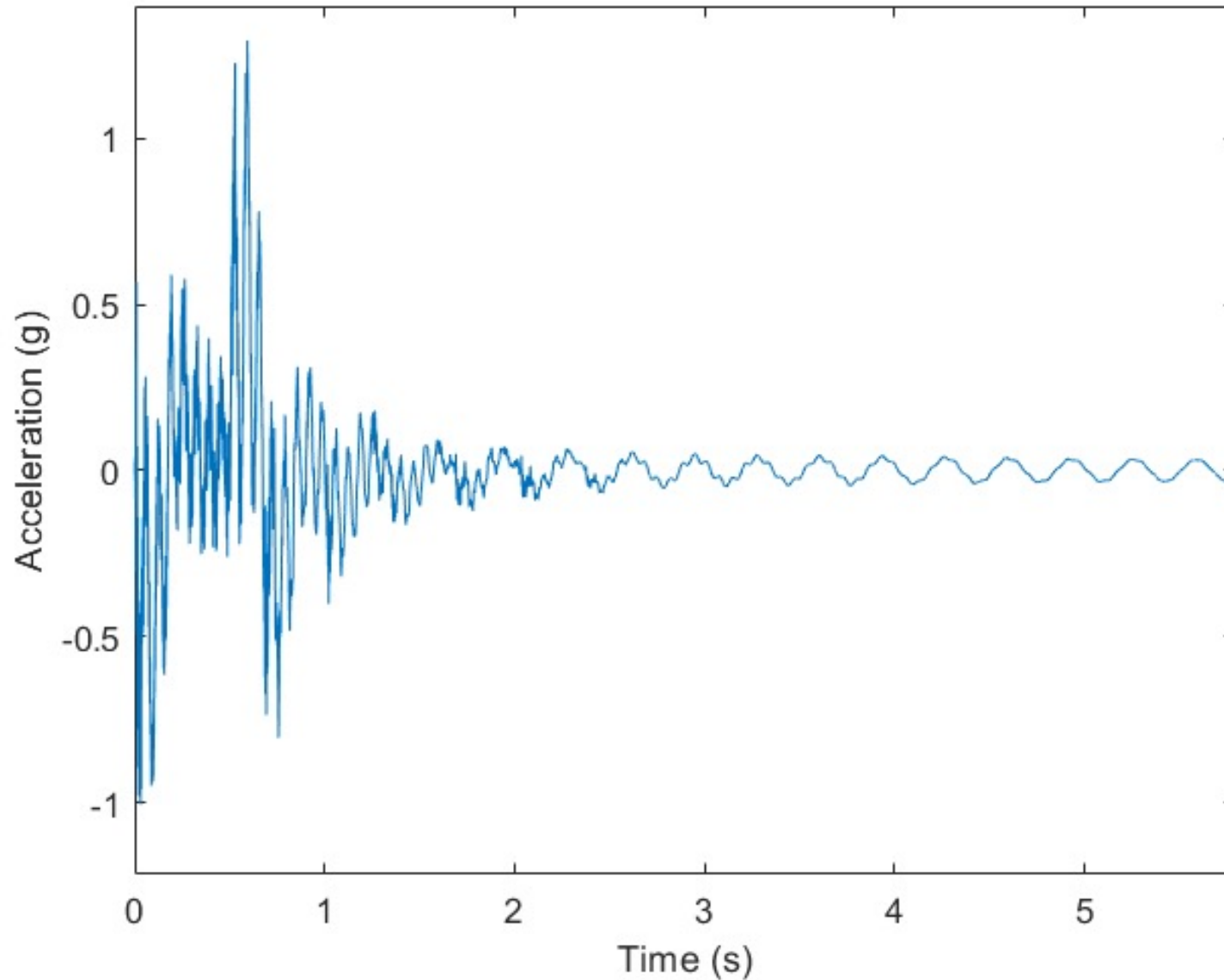
- ❑ Spurious modes linked to the excitation, may be detected
- ❑ Power spectral density function used to determine the correct modes

Parameter	$f_{n1}$ (Hz)	$f_{n2}$ (Hz)	$\zeta_{n1}$ (-)	$\zeta_{n2}$ (-)
True values	33.3	20.68	0.061	0.010
Rel. Error (%)	<b>8.67</b>	-0.23	-11.04	<b>58.39</b>

Mode	MAC value [-]
1 <sup>st</sup>	0.9954
2 <sup>nd</sup>	0.9989



# BP3A: Experimental response



# BP3A: SYSID Results (experimental)

Accelerometer at  $x/L = 0.5$

Parameters	$f_{n1}$ (Hz)	$f_{n2}$ (Hz)	$\zeta_{n1}$ (-)	$\zeta_{n2}$ (-)
Simulated model	3.62	20.63	0.053	0.016
Hardware	2.98	15.21	0.051	0.014
Relative Error (%)	-17.68	<b>-26.72</b>	-3.77	<b>-12.50</b>

# BP3A: Discussion (1/2)

## □ Simulated data: Modal Analysis (SSI-COV)

- The **natural frequencies** considered as **identified correctly** by the SSI-COV algorithm (max relative error a bit outside the acceptable limit of 5% (i.e., 8.67%))
- The first **damping ratio** identified better than the second one (-11.04% vs. 58.39%)
  - 2<sup>nd</sup> damping ratio true value is very small (only 0.010)
- The physical system and its SimScape implementation do not match perfectly
- The execution of the BP3A **simulated experiment** is deemed as **successful** (at least in terms of the natural frequencies)

# BP3A: Discussion (2/2)

- ❑ Experimental data: Modal Analysis (SSI-COV)
- ❑ The accelerometer **directly influences** the flexible link **dynamics**
  - Due to link additional mass, its two natural frequencies shifted lower
- ❑ Accelerometer position affects the results

## Accelerometer at $x/L = 0.75$

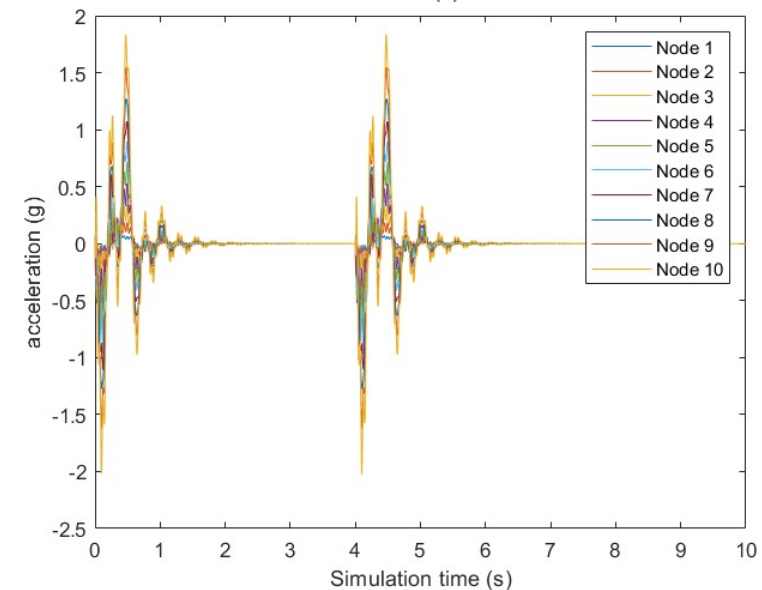
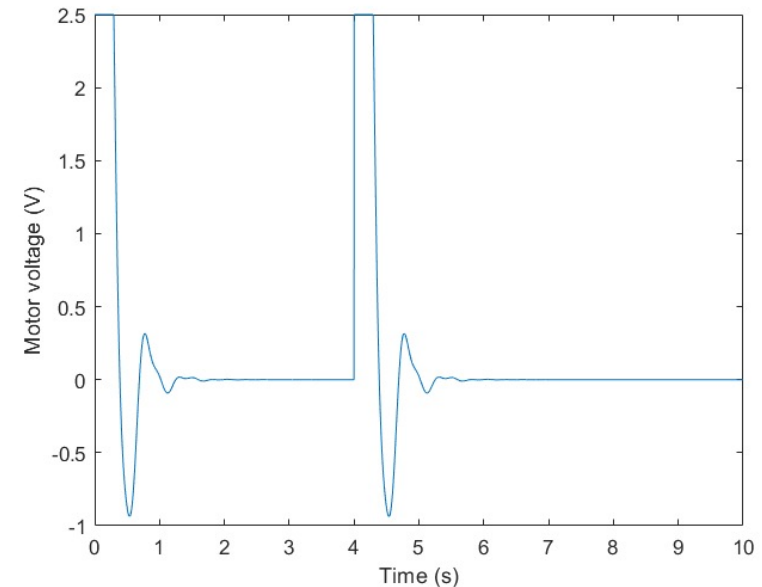
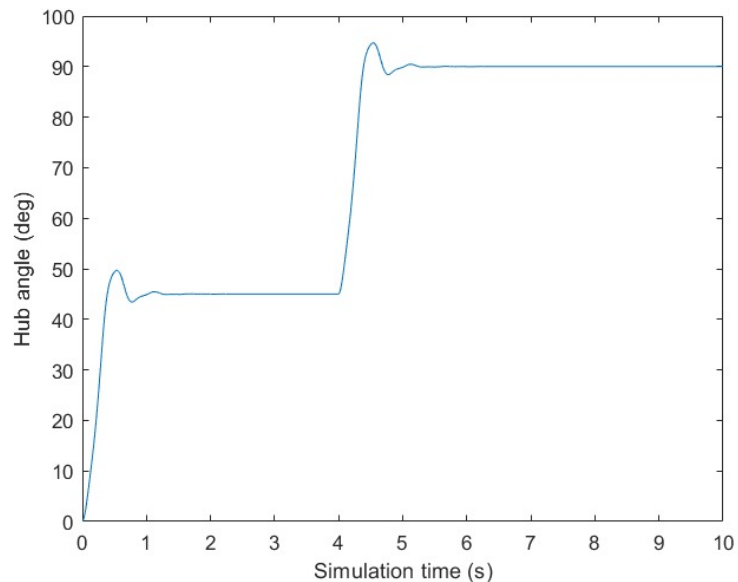
## Accelerometer at $x/L = 0.25$

Parameters	$f_{n1}$ (Hz)	$f_{n2}$ (Hz)	$\zeta_{n1}$ (-)	$\zeta_{n2}$ (-)	Parameters	$f_{n1}$ (Hz)	$f_{n2}$ (Hz)	$\zeta_{n1}$ (-)	$\zeta_{n2}$ (-)
Simulated model	3.62	20.63	0.053	0.016	Simulated model	3.62	20.63	0.053	0.016
Hardware	3.80	20.15	0.071	0.026	Hardware	3.15	17.99	0.059	0.013
Relative Error (%)	4.97	-2.32	33.96	62.50	Relative Error (%)	-12.98	-12.80	11.32	-18.75

# BP3B: Excitation & simulated response

## □ Operational scenario

- The hub **rotates** to reach two angle positions (i.e., 45° and 90°), as fast as possible.
- Quanser system **limitations** observed

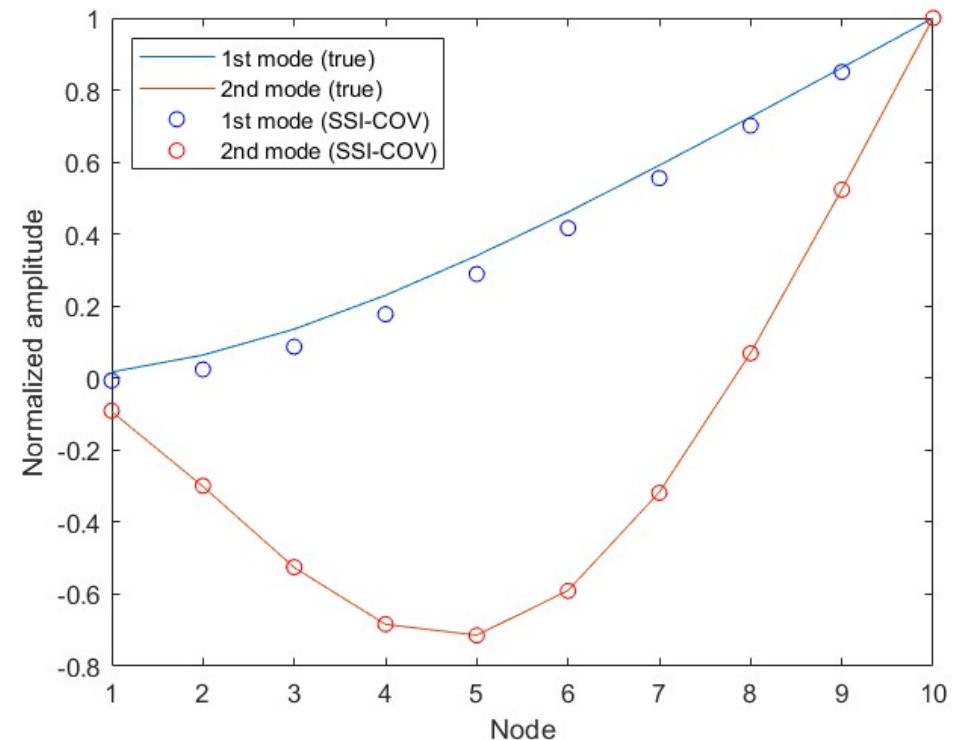


# BP3B: SYSID Results (simulation)

## Modal Analysis by RSSI-COV

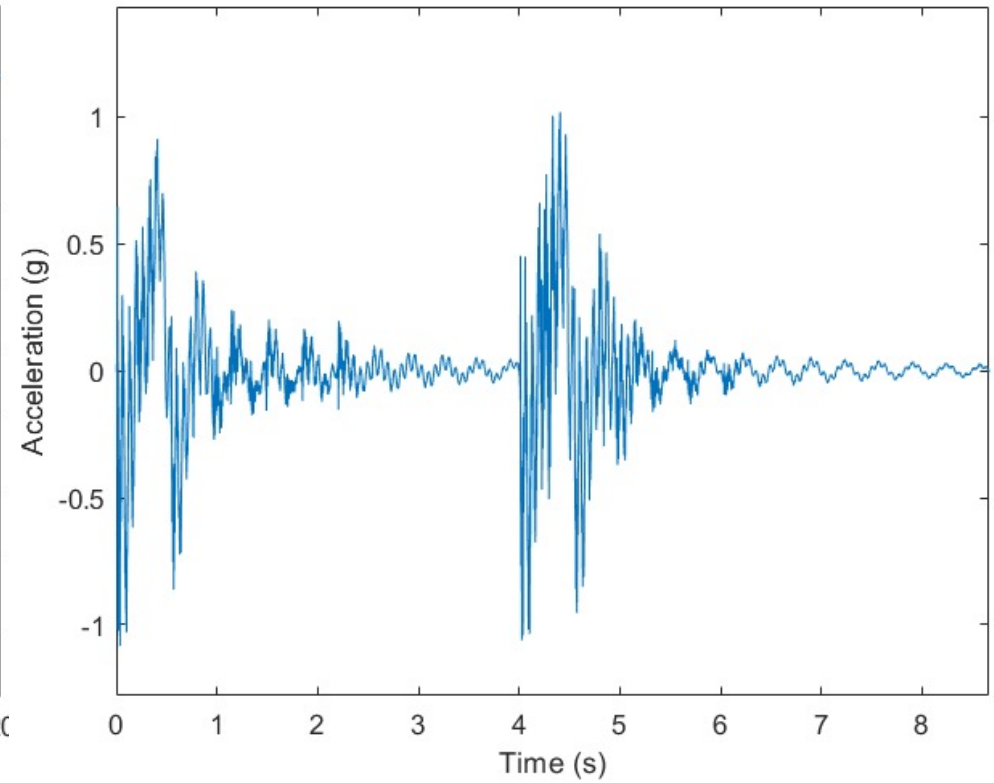
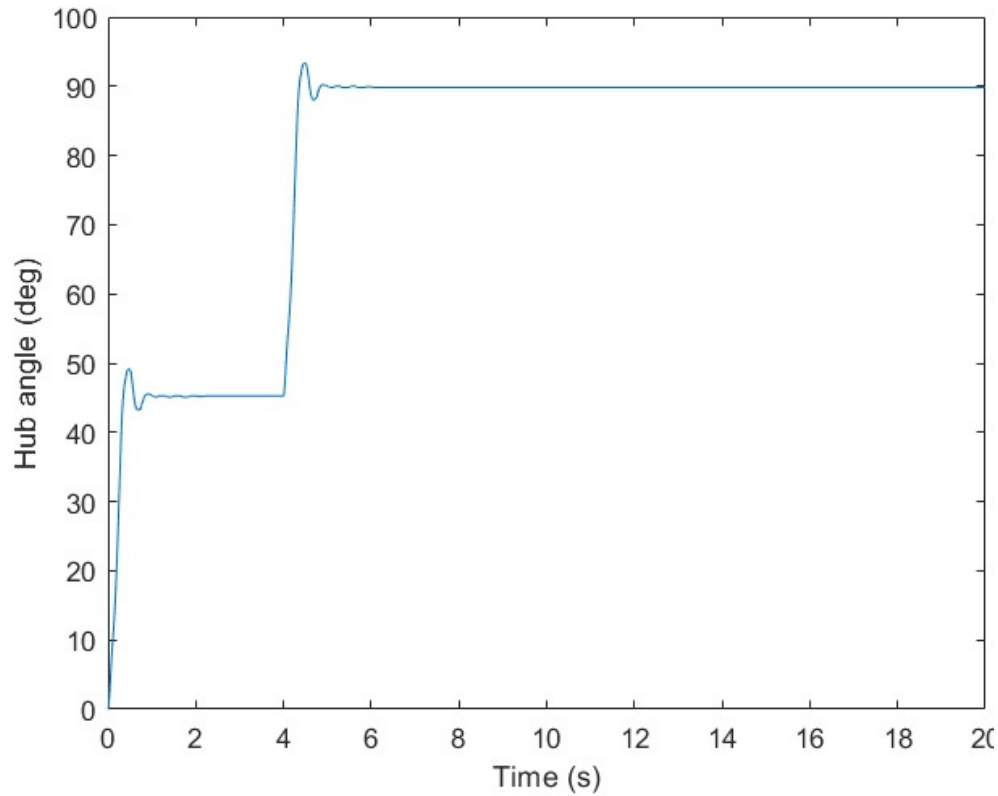
Parameter	$f_{n1}$ (Hz)	$f_{n2}$ (Hz)	$\zeta_{n1}$ (-)	$\zeta_{n2}$ (-)
True values	33.3	20.68	0.061	0.010
Rel. Error (%)	<b>8.35</b>	-3.40	<b>-63.05</b>	59.88

Mode	MAC value [-]
1 <sup>st</sup>	0.9965
2 <sup>nd</sup>	0.9999





# BP3B: Experimental response



# BP3B: SYSID Results (experimental data)

Accelerometer at  $x/L = 0.5$

Parameters	$f_{n1}$ (Hz)	$f_{n2}$ (Hz)	$\zeta_{n1}$ (-)	$\zeta_{n2}$ (-)
Simulated model	3.61	19.98	0.098	0.016
Hardware	3.73	15.09	0.064	0.021
Relative Error (%)	3.32	<b>-24.47</b>	<b>-34.69</b>	31.25

# BP3B: Discussion (1/2)

## □ Simulated data: Modal Analysis (RSSI-COV)

- The **natural frequencies** considered as **identified correctly** by the RSSI-COV algorithm (max relative error a bit outside the acceptable limit of 5% (i.e., 8.35%))
- Both **damping ratios** are identified with relatively high relative errors (63.05% - 58.39%)
  - Both damping ratios true values are quite small (0.06 - 0.01)
- The physical system and its Simscape implementation do not match perfectly
  
- The execution of the BP3B **simulated experiment** is deemed as **successful** (at least in terms of the natural frequencies)

# BP3B: Discussion (2/2)

- Experimental data: Modal Analysis (RSSI-COV)
- The accelerometer directly influences the flexible link dynamics
  - Due to link additional mass, its two natural frequencies shifted lower
- Accelerometer position affects the results

## Accelerometer at $x/L = 0.75$

## Accelerometer at $x/L = 0.25$

Parameters	$f_{n1}$ (Hz)	$f_{n2}$ (Hz)	$\zeta_{n1}$ (-)	$\zeta_{n2}$ (-)	Parameters	$f_{n1}$ (Hz)	$f_{n2}$ (Hz)	$\zeta_{n1}$ (-)	$\zeta_{n2}$ (-)
Simulated model	3.61	19.98	0.098	0.016	Simulated model	3.61	19.98	0.098	0.016
Hardware	3.07	19.85	0.095	0.017	Hardware	3.40	15.72	0.057	0.021
Relative Error(%)	-14.96	-0.65	-3.06	6.25	Relative Error(%)	-5.82	-21.32	-41.84	31.25

# Discussion on BP1 Experiments

- ❑ The SYSID with the BP1A **simulated** data is deemed as **successful**
- ❑ The SYSID with the BP1A **experimental** data is deemed as **partially successful**
  - However, system reconstruction based on identified parameters, was **successful**
- ❑ The SYSID with the BP1B **simulated** data is deemed as **partially successful**
  - Inadequate SNR
- ❑ The SYSID with the BP1B **experimental** data is deemed as **unsuccessful**
  - Main reasons: **Low SNR**, comparison with **CAD “true” values**, and **inaccurate knowledge of the excitation force**

# Discussion on BP2 Experiments

- ❑ The SYSID with the BP2 **simulated** data is deemed as **successful**
- ❑ The SYSID with the BP2 **experimental** data is deemed as **partially successful**
  - Accurate estimation of excitation forces resulted in **meaningful** (if not acceptable) results
  - However,
    - “True” values were obtained by **CFD** model and **fitting** on a mass-spring-damper model
    - Sloshing mass *excitation* is close to the acceleration noise levels -> **difficult to decipher from noise.**

# Discussion on BP3 Experiments

- ❑ The SYSID with the BP3 **simulated** data is deemed as **successful** (at least in terms of the natural frequencies)
  - Model and Simscape implementation do not match perfectly
- ❑ The SYSID with the BP3 **experimental** data is deemed as **partially successful** (depends on accelerometer position)
  - The accelerometer directly influences flexible link dynamics
  - Due to additional mass, natural frequencies shifted lower

# Study Cases



# Basic Considerations (1/2)

## Full-scale Planar System Models (simulations)

- Insight on the SYSID Algorithms requirements
- Develop appropriate **Methods** to apply the **chosen Algorithms**

## Scaled-down Planar Experiments (consortium facilities)

- Significant insight on the SYSID Algorithms and developed Methods requirements, capabilities and limitations

# Basic Considerations (2/2)

## Scaled-down Planar Experiments (simulations)

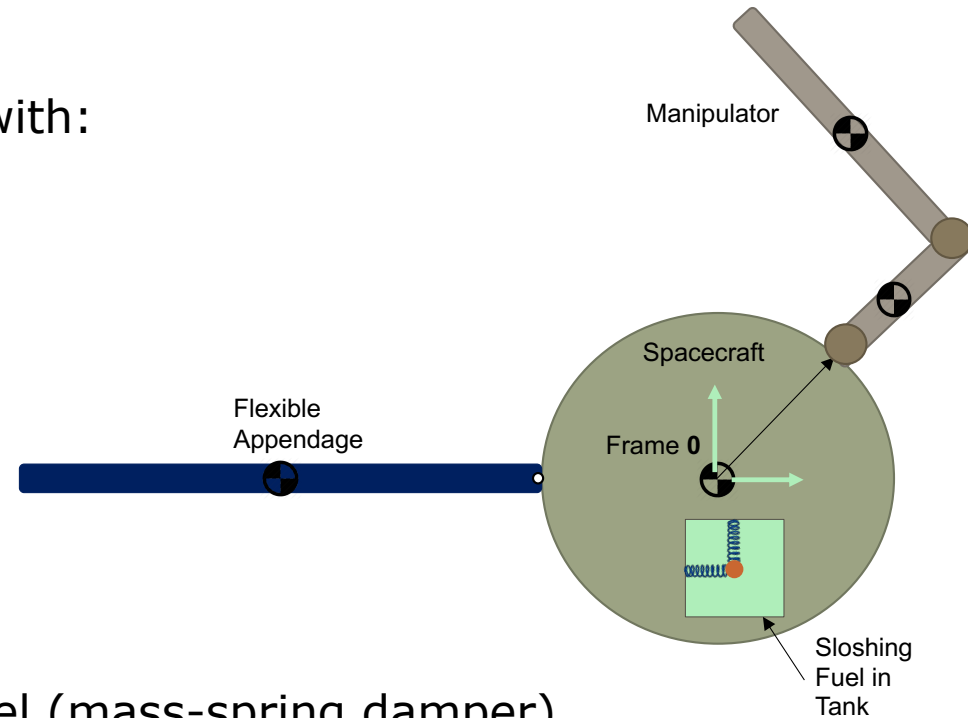
- **Validate** the developed Analytical Models
- **Design of excitation** signal to be used for the h/w experiment
- **Gain knowledge** on the behaviour of the experimental set-up (limitations, sources of error, etc.) and on the SYSID algorithm
- **Validate** the experimentally Identified Models, using Analytical and/ or SimScape models

## Full-scale Spatial (3D) System Models (simulations)

# SC1: Full-scale Planar System (1/7)

## 2D System

- Manipulator equipped chaser S/C with:
  - a fuel tank
  - a flexible appendage



## Modelling Assumptions

- S/C Model: Rigid body
- Fuel Sloshing Model: Lumped model (mass-spring damper)
- Flexible appendage: Continuous model (Euler-Bernoulli beam)

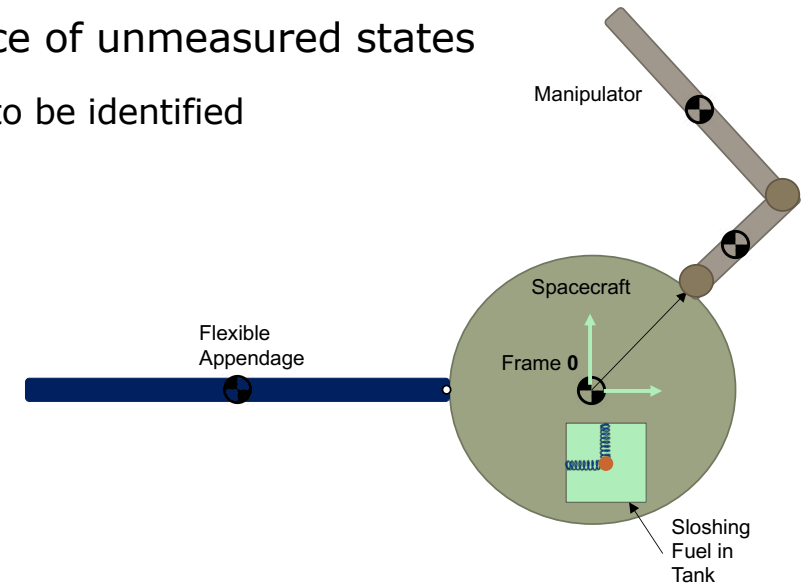
# SC1: Full-scale Planar System (2/7)

## Main challenge

- All system parameters to be identified in the presence of unmeasured states
  - Inertial, sloshing, modal parameters of chaser system to be identified
  - Sloshing states are not measurable
  - Modal states are not measurable

## Additional challenge

Lack of existing methodologies



## Goal

Develop a method that overcomes the challenges and identify all the Chaser's parameters

## Contribution

Development of a method based on two subsequent experiments (stages)

# SC1: Full-scale Planar System (3/7)

## Design of SC1 SYSID

### Experiments:

- Experiment 1
- Experiment 2

#### SYSID Experiment 1

- The S/C orientation is kept constant
- Inputs: Only net forces act on the S/C

##### Modal Analysis for Flexible Appendage

Modal parameters of the flexible appendage can be identified

##### Parametric SYSID 1 for Sloshing

The sloshing parameters can be identified

#### SYSID Experiment 2

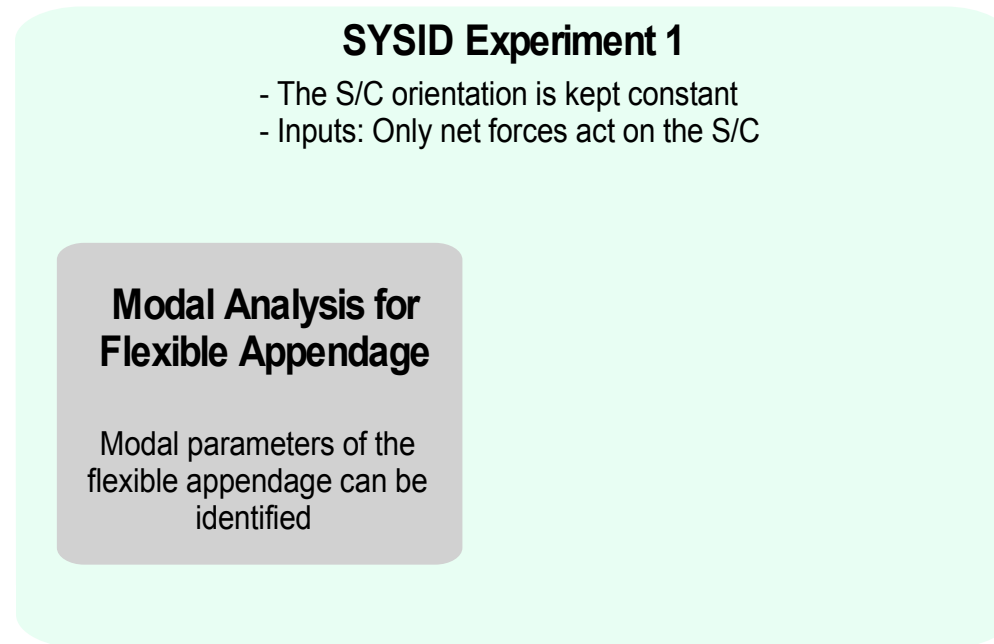
- The S/C orientation is **not** kept constant; it is free to change
- Inputs: Net forces/moment act on the S/C, torques act on arm joints

##### Parametric SYSID 2 for Space Robot

The space robot's inertial parameters can be identified

# SC1: Full-scale Planar System (4/7)

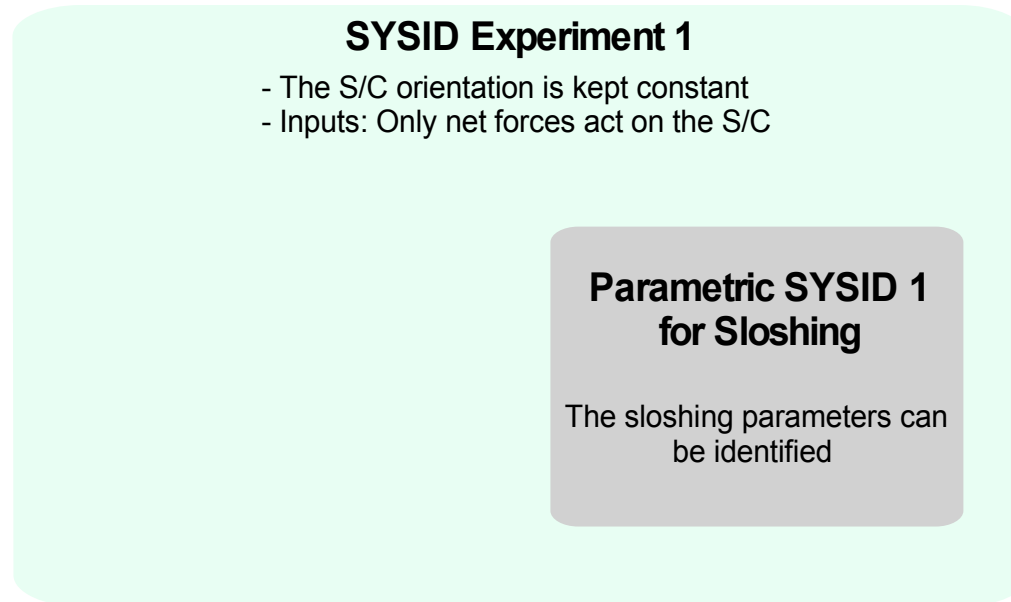
**Design of SYSID Experiment 1:** Pure translation by applying net forces only



- **Modal parameters identified:** natural frequencies, damping ratios, mode shapes
- Measurements of flexible appendage tracked points accelerations
- **SSI-COV** algorithm used based on the BP3 Trade-off Analysis

# SC1: Full-scale Planar System (5/7)

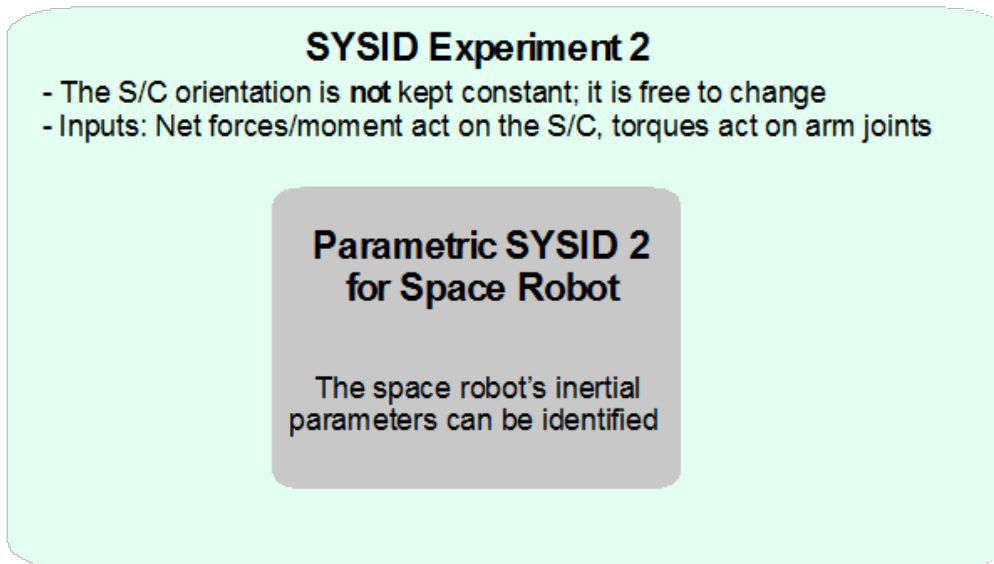
## Design of SYSID Experiment 1: Pure translation of S/C, arm locked



- Novel Method developed based on [transfer function formulation](#) (same framework as BP2-M2)
  - [Eliminates unmeasurable](#) sloshing and modal [states](#) from SYSID equations
  - [Decouples](#) sloshing [identification](#) from modal parameters identification
  - Allows for sloshing parameters identification to [run in parallel](#) with modal analysis
- TLS algorithm used based on the BP2 Trade-off Analysis.

# SC1: Full-scale Planar System (6/7)

## Design of SYSID Experiment 2: S/C translation & rotation, arm performs trajectories



- *Excitation similar to BP1B*
- All *Fourier series coefficients* obtained by **minimizing** regressor matrix **condition number**

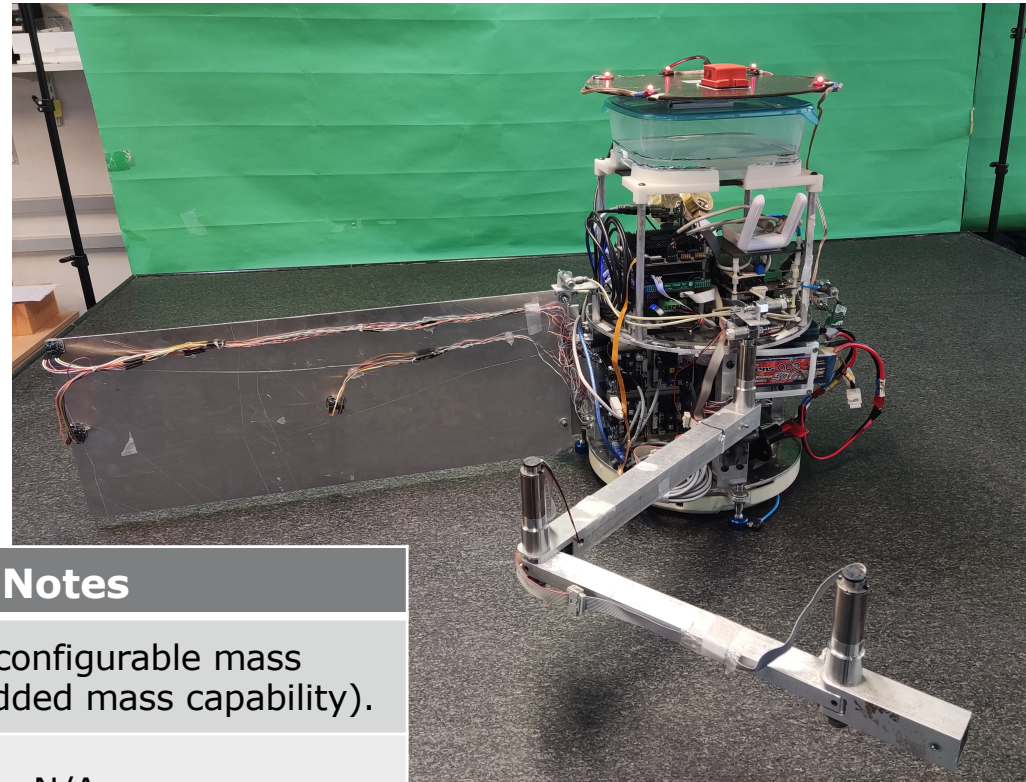
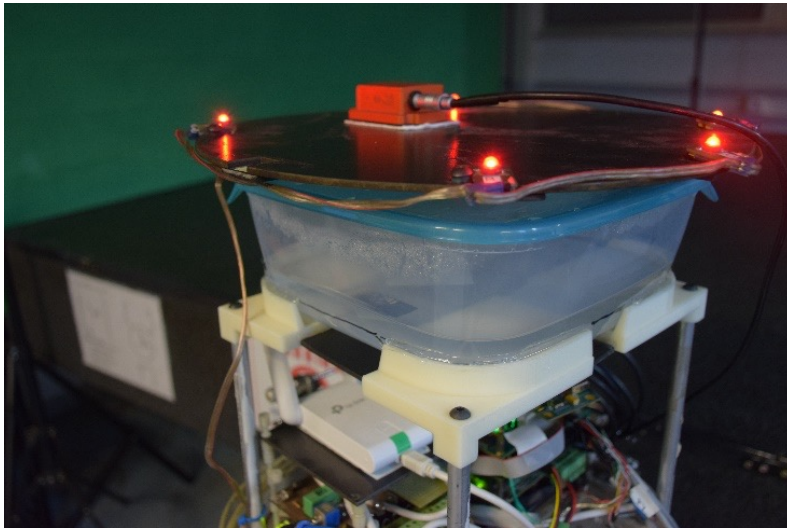
- Method developed, consisting of:
  - A **SYSID equation** based on *energy balance* (same framework as BP1-M2)
  - An **estimator** for the unmeasurable *sloshing* states based on *equations of motion*
  - An **estimator** for the unmeasurable *modal* states based on *assumed modes method*
- TLS algorithm used based on the BP1 Trade-off Analysis.



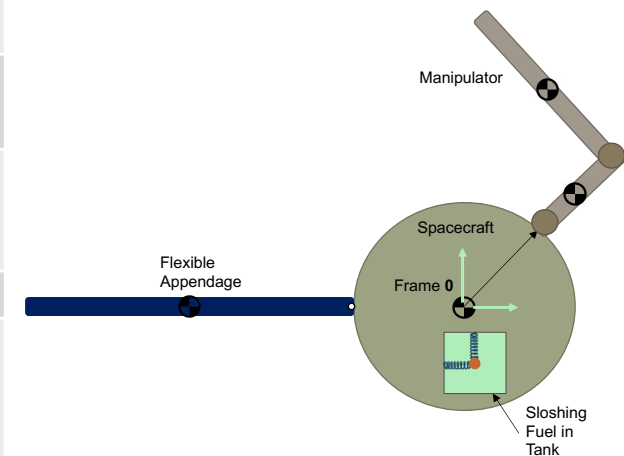
# SC1: Full-scale Planar **SYSID Results (7/7)**

- SYSID in [Experiment 1](#), yields [good results](#) in general
  - Relative errors for most modal and parametric SYSID, are low
    - Max Rel. Error in Natural Frequencies (*SSI-COV*): 3.14%
    - Max Rel. Error in Sloshing Estimation (*TLS*): 3.63% (damping excluded)
  - [RTLS](#) was tried also, with Max. Rel. Error in Sloshing Estimation: 2.40%
  - Relative errors of estimated sloshing damping coefficients are large; negligible effect on the S/C response prediction (see sensitivity analysis earlier in this presentation)
- SYSID in [Experiment 2](#) yields [acceptable](#) identification
  - Max Relative Error in Inertial Estimation: 4.62%
- Thus, SC1 SYSID for both Experiment 1/2, is deemed as [successful](#)

# SC1: Experimental Facility & Model



Component	Mass	Notes
Robotic System w/o Manipulator	13 kg	Cepheus has reconfigurable mass (provision for added mass capability).
Robotic System w/t Manipulator	14 kg	N/A
Empty Plastic Tank	500 g	N/A
Water Emulating Sloshing Fuel	800 g	Based on CFD model, only about 650g of the 800 g are contributing to the sloshing phenomenon.
Solar Panel	440 g	N/A
CO <sub>2</sub> Tank (empty)	900 g	Working pressure: 7 bar
CO <sub>2</sub> Tank (full)	1650 g	



# SC1 EXP1: SYSID Results (simulation)

## □ Experiment 1

### ■ Modal Analysis

Parameters	SSI-COV	RSSI-COV	SSI-COV	RSSI-COV
Type	Bending	bending	bending	bending
True values (Hz)	1.947		12.200	
Est. value (Hz)	1.946	1.942	12.275	12.254
Rel. Error (%)	<b>0.049</b>	<b>0.222</b>	<b>0.614</b>	<b>0.447</b>

### ■ Parametric (sloshing) SYSID (realistic noise models)

Param	True Value	Est. Value TLS	Relative error (%)	Est. Value RTLS	Relative error (%)
M	15.117	15.178	<b>0.4011</b>	15.2072	<b>0.5966</b>
$m_s$	0.625	4.0178	<b>542.84</b>	4.0204	<b>543.27</b>
$k_s$	33.2156	717.3224	--	715.9319	--
$b_s$	0.1336	3.0551	--	2.3180	--
$\rho$	0.675	-0.2563	<b>137.96</b>	-0.1739	<b>125.76</b>

### ■ Parametric (sloshing) SYSID (increased SNR)

Relative Error for Parameter	Relative Error (%) from Simulation		
	Lower noise, 3 acc/meters	Lower noise, 7 acc/meters	Noiseless, 3 acc/meters
M	<b>0.014662</b>	<b>0.0095055</b>	<b>6.5045e-10</b>
$m_s$	<b>15.026</b>	<b>0.52262</b>	<b>0.028216</b>
$k_s$	<b>15.294</b>	<b>0.73895</b>	<b>0.028216</b>
$b_s$	<b>24.451</b>	<b>8.6107</b>	<b>0.028216</b>
$\rho$	<b>29.036</b>	<b>4.5398</b>	<b>0.061576</b>

# SC1 EXP2: SYSID Results (simulation)

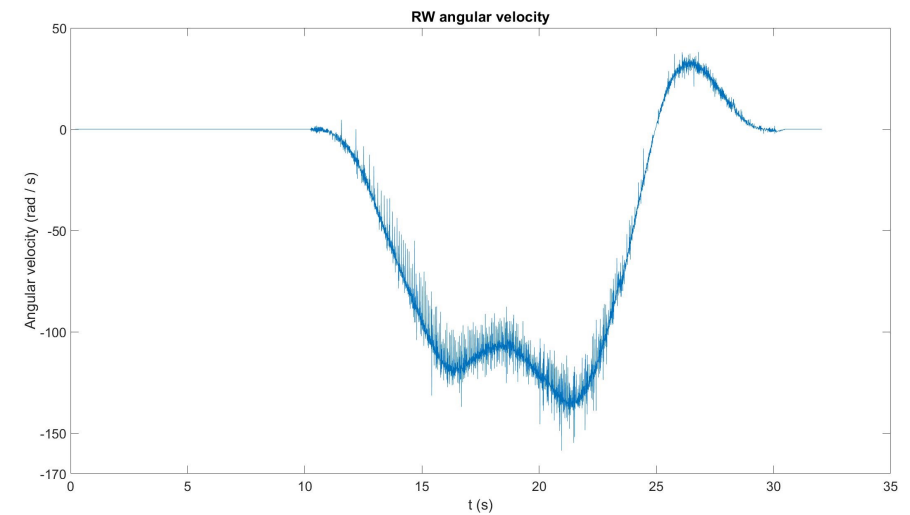
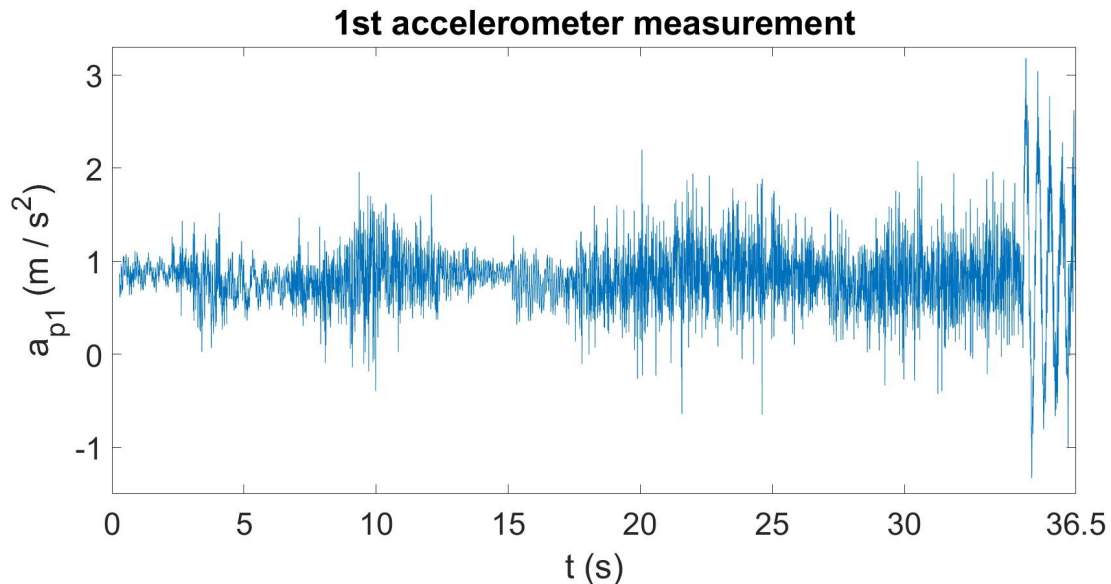
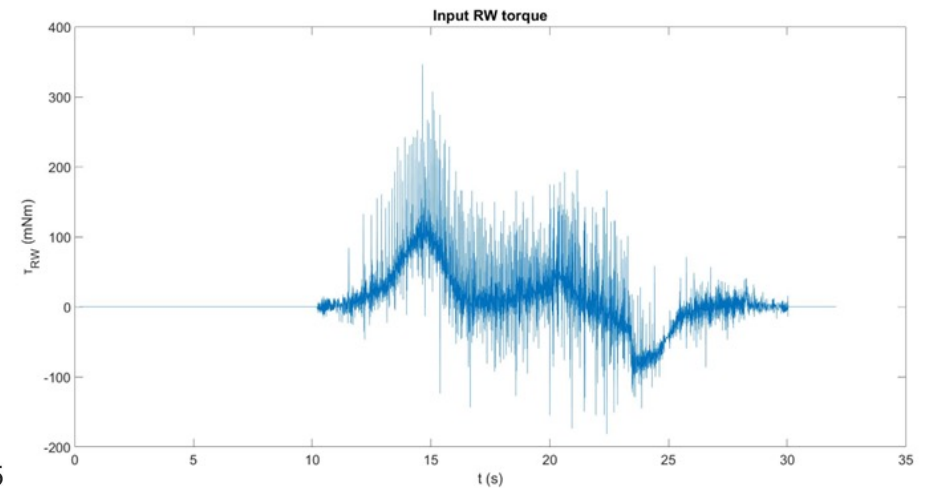
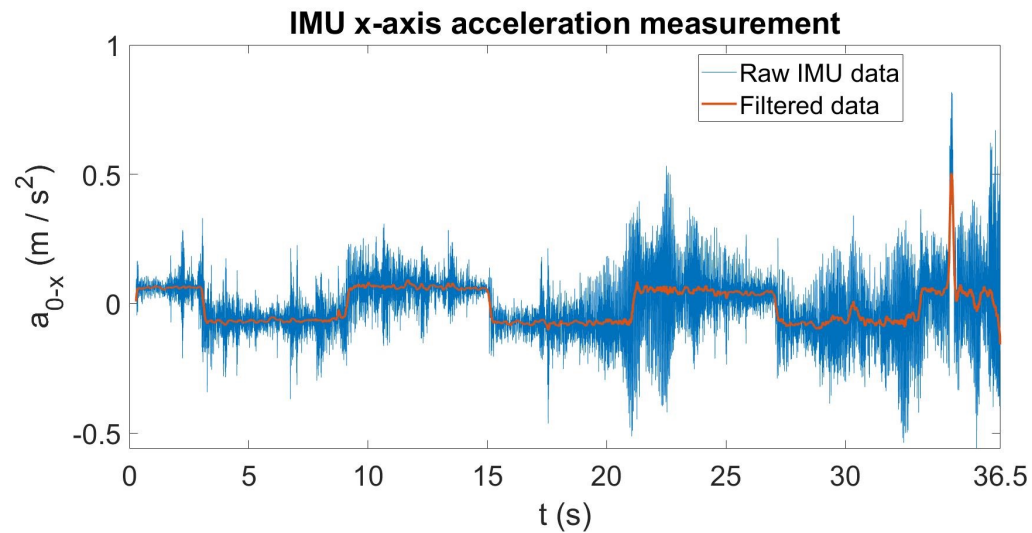
## □ Experiment 2

### ■ Parametric SYSID (inertial)

Param	True Val.	Est. Value TLS	Rel. error (%)	Est. Value RTLS	Rel. error (%)	Rel error (%) (lower noise) TLS
$a_1$	0.424	0.4068	<b>4.06</b>	0.4051	<b>4.45</b>	<b>0.97</b>
$a_2$	0.13626	0.1366	<b>0.29</b>	0.1195	<b>12.30</b>	<b>5.69</b>
$a_3$	0.21477	0.2333	<b>8.65</b>	0.2496	<b>16.20</b>	<b>0.40</b>
$a_4$	0.20152	0.1192	<b>40.82</b>	0.0959	<b>52.41</b>	<b>8.30</b>
$a_5$	0.26194	0.2360	<b>9.89</b>	0.2305	<b>11.99</b>	<b>6.13</b>
$a_6$	0.03933	0.0841	<b>113.7</b>	0.0807	<b>105.1</b>	<b>2.96</b>
$a_7$	0.09321	0.1502	<b>61.11</b>	0.1531	<b>64.30</b>	<b>3.59</b>
$a_8$	0.03569	0.0653	<b>83.04</b>	0.0660	<b>84.97</b>	<b>4.84</b>
$a_9$	0.05626	0.0645	<b>14.73</b>	0.0715	<b>27.07</b>	<b>4.55</b>
$a_{10}$	0.0127	0.0017	<b>86.40</b>	-0.0002	<b>101.5</b>	<b>8.08</b>
$a_{10}$	0.02002	0.0386	<b>92.70</b>	0.0407	<b>103.1</b>	<b>7.94</b>
$a_{12}$	0.02442	0.0262	<b>7.30</b>	0.0308	<b>26.35</b>	<b>4.00</b>

### ■ Estimators used for unmeasurable quantities

# SC1: Experimental response



# SC1 EXP1&2: SYSID Results (experimental)

## Experiment 1

### Modal Analysis

Parameters	SSI-COV	RSSI-COV	SSI-COV	RSSI-COV
Type	bending	bending	bending	bending
True values	1.947 (Hz)		12.200 (Hz)	
Estimated value	2.271 (Hz)	2.265 (Hz)	11.62 (Hz)	11.566 (Hz)
Rel. Error (%)	<b>-16.85</b>	<b>-16.33</b>	<b>4.73</b>	<b>5.19</b>

### Parametric (sloshing) SYSID

Parameter	True Value	Estimated Value TLS	Relative error (%)	Estimated Value RTLS	Relative error (%)
M	15.117	11.7012	<b>22.596</b>	12.09	<b>20.027</b>
$m_s$	0.625	-8.1245	--	-10.655	--
$k_s$	33.2156	0.3339	<b>98.977</b>	1.5275	<b>95.401</b>
$b_s$	0.1336	-7.3121	--	-15.879	--
$\rho$	0.675	0.7711	<b>14.232</b>	0.7856	<b>16.391</b>

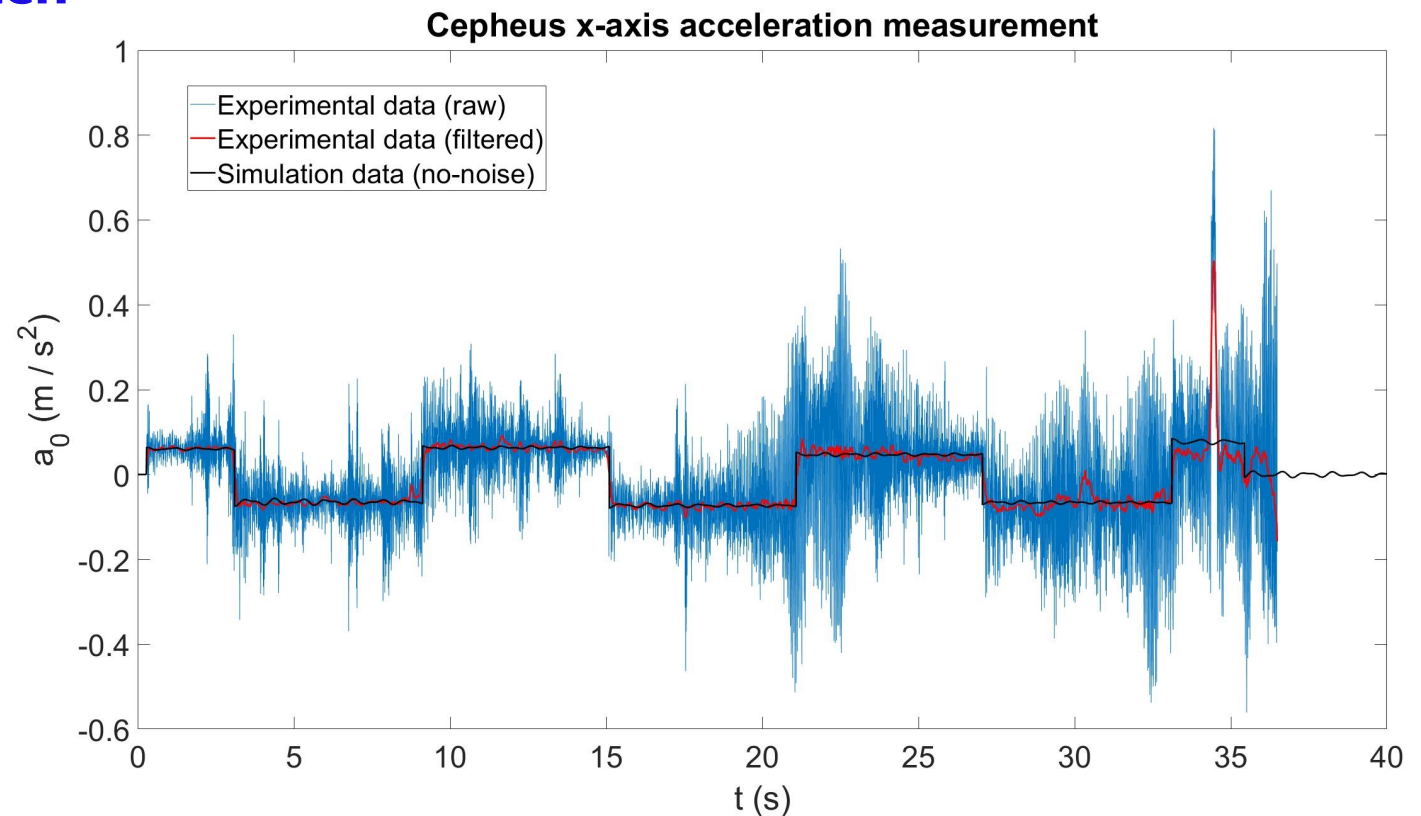
## Experiment 2

- Estimators used for unmeasurable quantities
- SYSID results not meaningful**



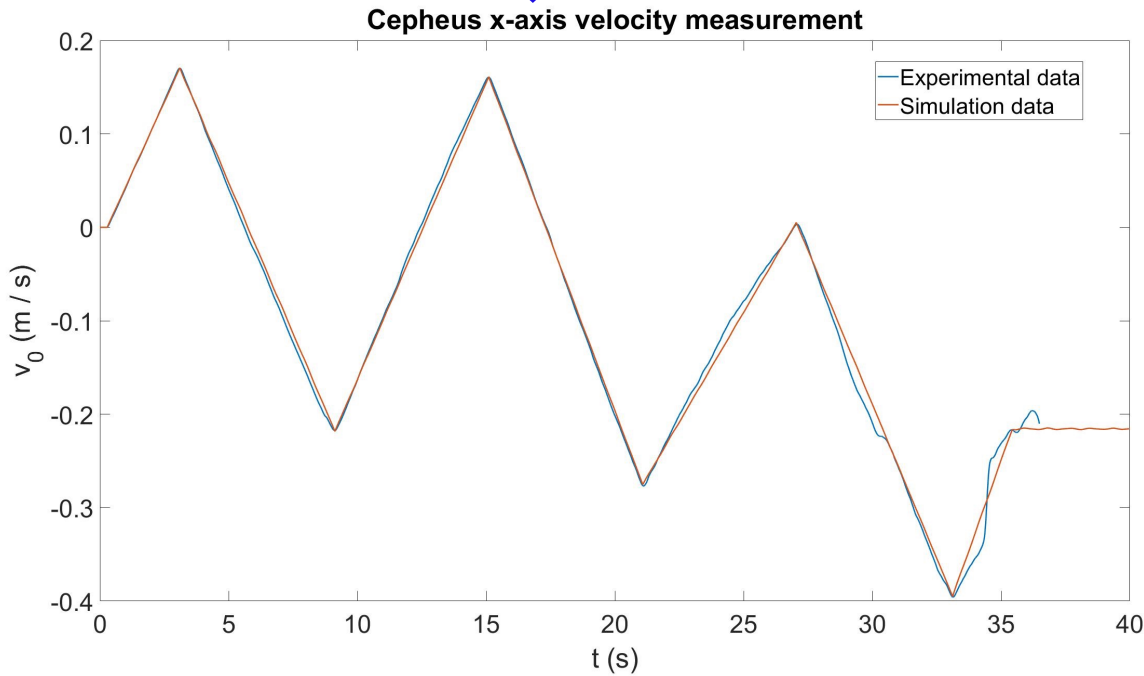
# SC1: Modelling Validation (1/2)

- Identification Experiment: **Experimental vs. Simulated Setup**
  - Same excitation
  - **Qualitative** comparison
- **Very good match**

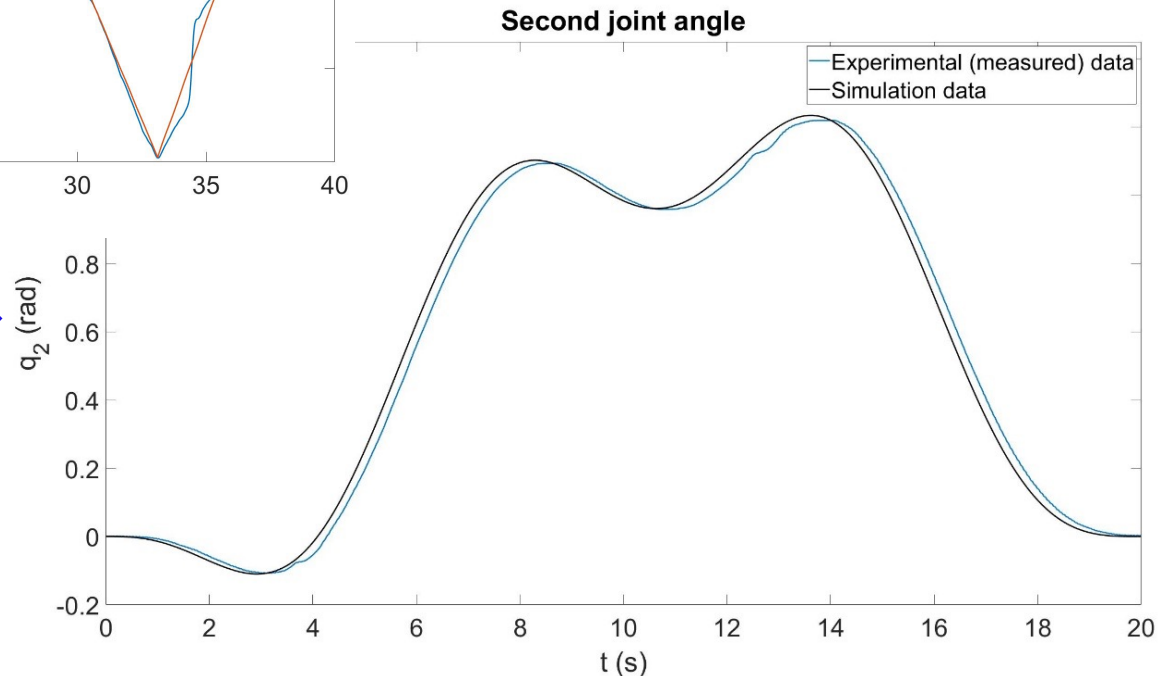


# SC1: Modelling Validation (2/2)

- Experiment 1



- Experiment 2



- Very good match**



# SC1: Discussion: Simulated Data

- ❑ **Parametric SYSID** with both **TLS** and **RTLS** for **SC1** (both Experiment 1 and 2), does **not yield meaningful results** for several parameters
  - Inadequate SNR is observed
  - *Increasing SNR* (e.g., by lower noise or more accelerometers) leads to **significant improvement** and **good** results
- ❑ **Modal Analysis** with both **SSI-COV** and **RSSI-COV** for **SC1** (Experiment 1), is deemed as **successful** in identifying the first two natural frequencies
- ❑ **Recursive** implementations of the Algorithms
  - yield **slightly worse** results to the non-recursive ones
  - but converge at about **halfway** through the simulation

# SC1: Discussion: Experimental Data (1/2)

❑ **Parametric SYSID** with both **TLS** and **RTLS** for **SC1** (both Experiment 1 and 2), does **not yield meaningful results** for *most parameters*

➤ Experiment 1 is close to BP2, which yielded good results. But “close” is not “the same”:

➤ Added mass  lower max accel.  lower excitation  lower SNR

➤ Added oscillations from flexible panel, make the excitation force reconstruction more difficult  again, lower SNR

❑ **Recursive** implementations (same as in simulation)

- Yield **slightly worse** results to the non-recursive ones
- Converge at about **halfway** through the simulation

# SC1: Discussion: Experimental Data (2/2)

- ❑ **Modal Analysis** with both **SSI-COV** and **RSSI-COV** for **SC1** (Experiment 1), is deemed as **successful** in identifying the first two *natural frequencies*
  - ID of 2<sup>nd</sup> bending frequency is good, but ID of 1<sup>st</sup> one has 16% relative error.
  - However, all Modal Analysis (with data from >10 experiments) yielded a 1<sup>st</sup> bending frequency of 2 to 2.3 Hz.
  - CAD-FEM models 1<sup>st</sup> bending frequency of 1.95Hz, used as “true”
  - Possibly the **actual** 1<sup>st</sup> bending frequency is 2 - 2.3 Hz, yielding significantly lower error
- ❑ Results **consistent** with the simulated experiment results

BPs					SCs	
1A	1B	2	3A	3B	1	2

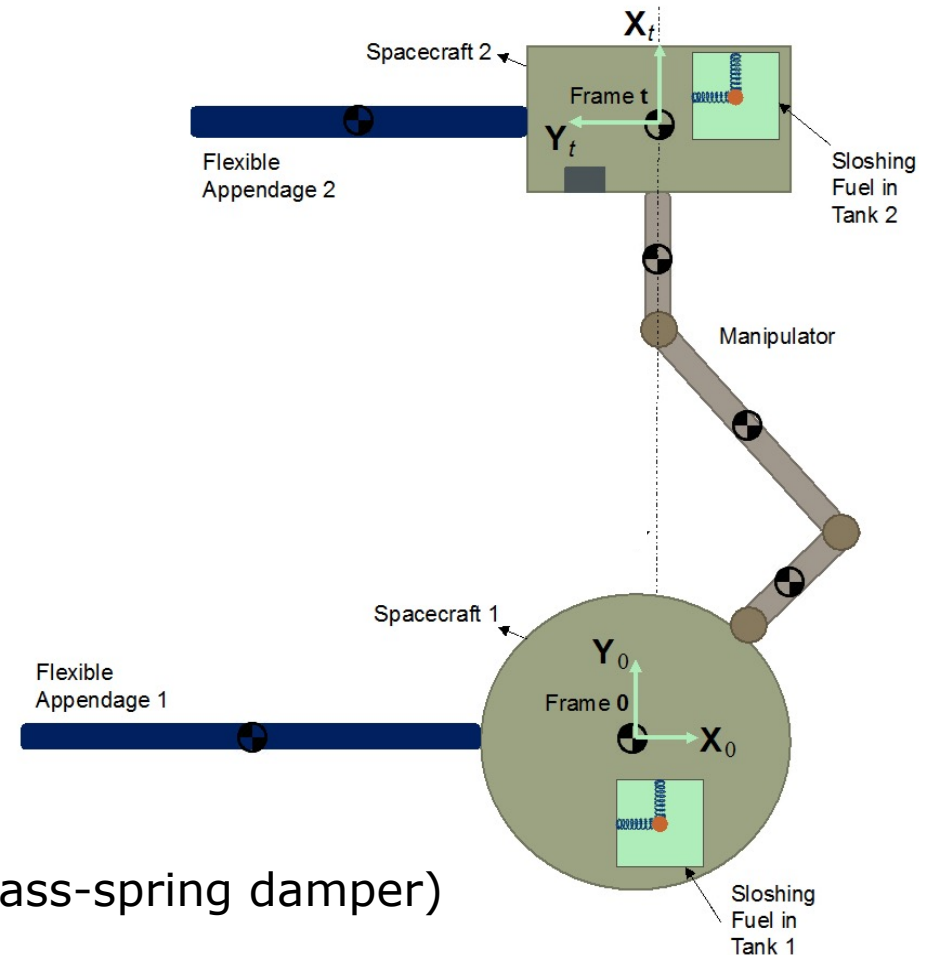
# SC2: Full-scale Planar System (1/6)

## 2D System

- Manipulator equipped chaser S/C with:
  - a fuel tank
  - a flexible appendage
- Grasped target S/C with:
  - a fuel tank
  - a flexible appendage

## Modelling Assumptions

- S/C Model: Rigid body
- Fuel Sloshing Model: Lumped model (mass-spring damper)
- Flexible appendage: Continuous model (Euler-Bernoulli beam)
- Rigidly grasped Target S/C



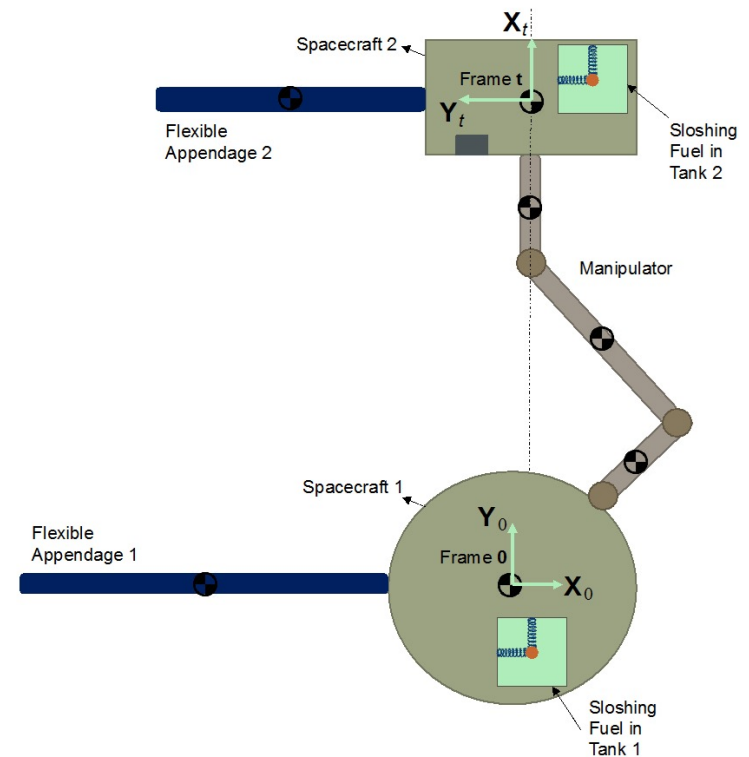
# SC2: Full-scale Planar System (2/6)

## Main challenge

- All system parameters to be identified in the presence of **unmeasurable** states
  - Inertial, sloshing, modal parameters of Target system to be identified
  - **Sloshing states** are not measurable
  - **Modal states** are not measurable

## Additional challenge

**Lack** of existing methodologies



# SC2: Full-scale Planar System (3/6)

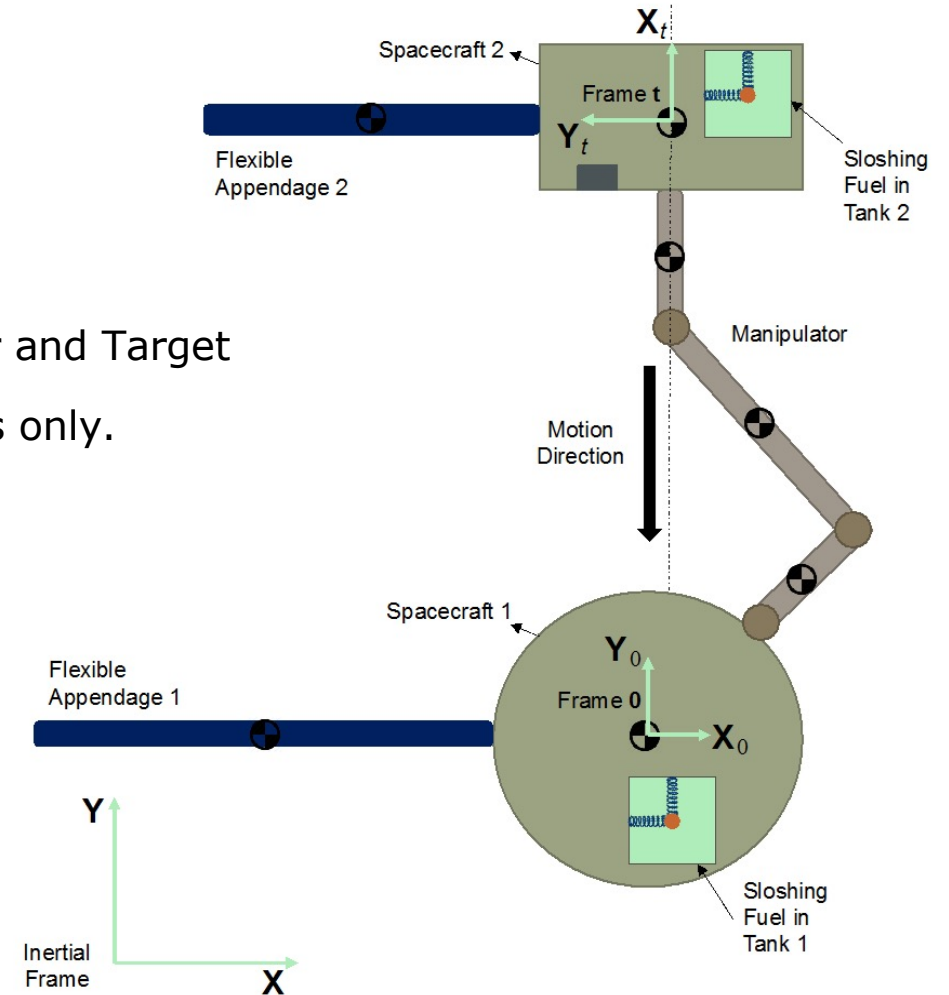
## SC2 Task: Berthing

### ■ Requirements

- Fixed Chaser attitude
- Constant relative attitude between Chaser and Target
- Target translation along the inertial **Y**-axis only.

### ■ Control

- Coordinated control
- Control in Cartesian space
- Model-based PD control law



# SC2: Full-scale Planar System (4/6)

## SYSID during Berthing

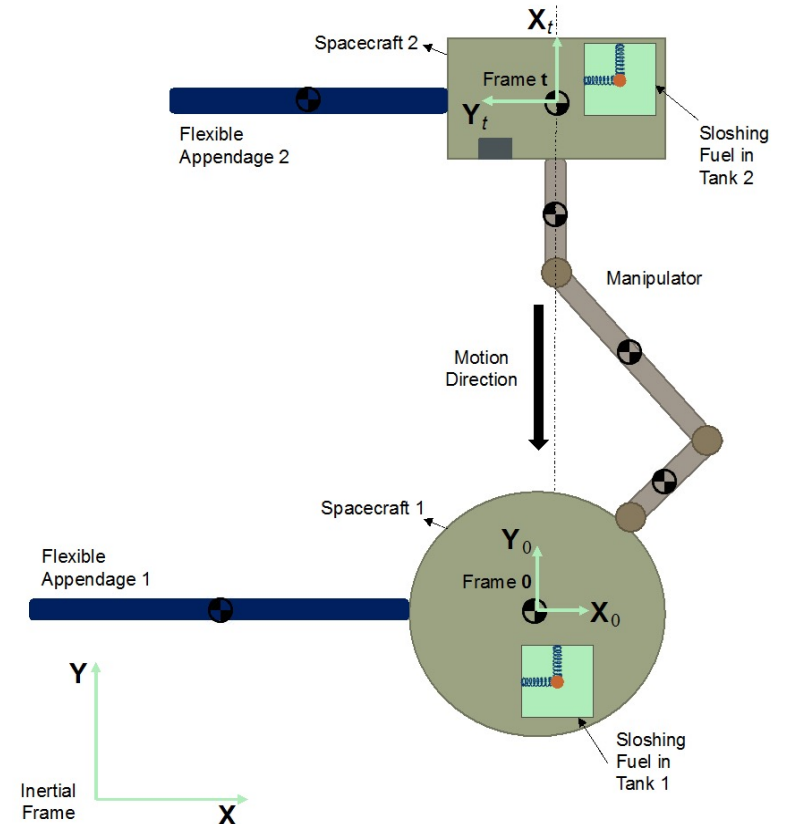
- The Target's S/C orientation is kept constant
- The Target's S/C translates along inertial  $Y$  axis

### Modal Analysis for Flexible Appendage

Modal parameters of the Target's flexible appendage can be identified

### Parametric SYSID for Sloshing and Mass

The Target's sloshing parameters and S/C mass can be identified



- Due to the chosen motion, **impossible** to identify
  - the target S/C's polar moment of inertia
  - the sloshing model parameters on the  $Y_t$ -axis
- In the absence of rotation, the Target CoM position is not be identified

# SC2: Full-scale Planar System (5/6)

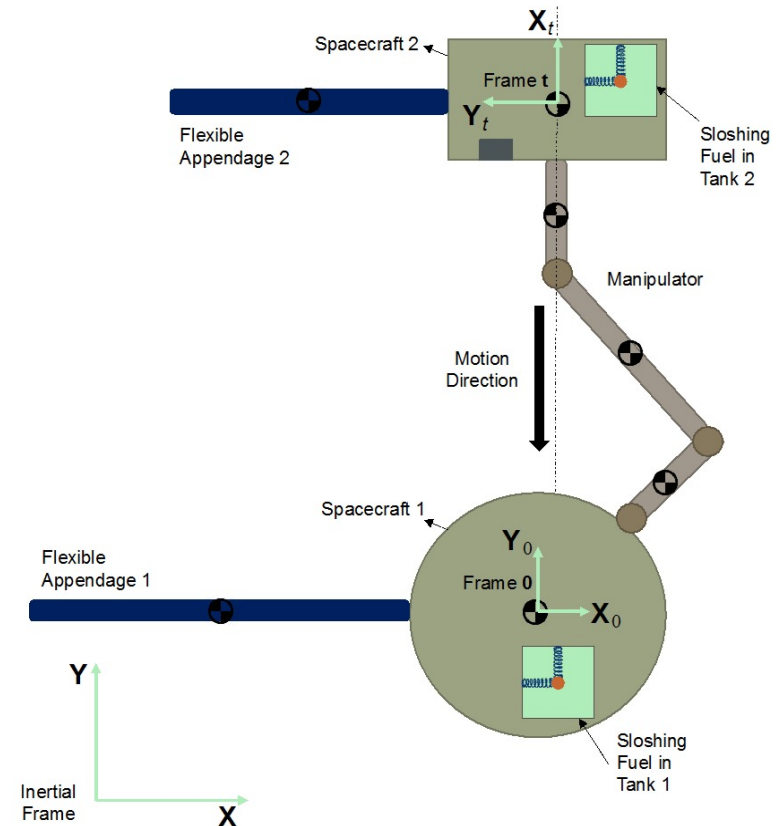
## Modal Analysis for Flexible Appendage

### SYSID during Berthing

- The Target's S/C orientation is kept constant
- The Target's S/C translates along inertial **Y** axis

### Modal Analysis for Flexible Appendage

Modal parameters of the Target's flexible appendage can be identified

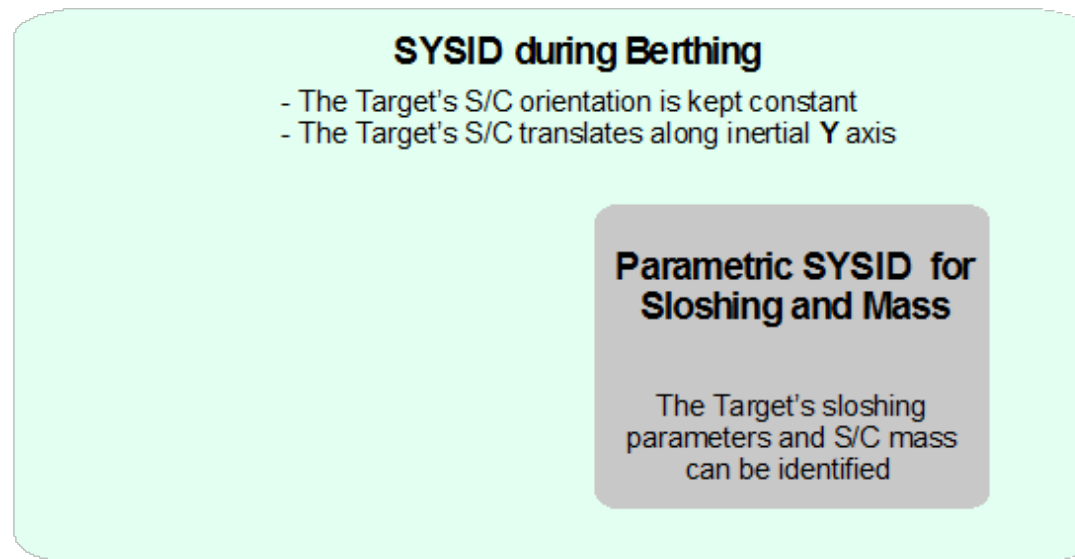


- Pure **translation** only in inertial **Y**-axis, by applying **net forces** only
- Measurements of flexible appendage tracked points **accelerations**
- **Recursive SSI-COV** algorithm used based on the BP3 Trade-off Analysis



# SC2: Full-scale Planar System (6/6)

## Parametric SYSID for sloshing and inertial parameters



- Novel method developed based on transfer function formulation (as in BP2-M2)
  - Eliminates unmeasurable sloshing and modal states from SYSID equations
  - Decouples sloshing identification from modal parameters identification
  - Allows for sloshing and S/C mass identification to run in parallel with modal analysis
- Recursive-TLS (RTLS) algorithm used based on the BP1 Trade-off Analysis

# SC2: Discussion on Simulated Data (1/3)

- ❑ Modal SYSID yields **very good results**, within acceptable limits
  - Requires enough measurements, leading to a **long** operation
  - Manipulator workspace limits result to **very slow operation**
    - **Benefits** Modal Analysis
    - But results in **very low SNR**
- ❑ Parametric SYSID yields **poor results**, due to the **low SNR**
  - Enhanced trajectory

# SC2: Discussion on Simulated Data (2/3)

- ❑ **Enhanced trajectory** case: a two-part trajectory considered
  - **Part 1**: General motion of Target, aligning the S/C berthing fixtures
  - **Part 2**: Pure translation of Target (as the original SC2 motion)
- ❑ Even then, **SNR** is still **not adequate**
- ❑ However, note that **lower noise levels** result in adequate SNR and **very good Parametric SYSID** results

# SC2: Discussion on Simulated Data (3/3)

- For SYSID, two fundamental requirements must be satisfied:
  - Behaviours due to parameters must be **excited**
  - Measured quantities of **appropriate SNR** must be available
- **When** these **requirements** are **satisfied** (e.g., noiseless measurements or exciting enough motion as in SC1), the **evaluated/developed methods** and algorithms **perform successfully**
- Else, SYSID results may not be useful

# **SYSID Detailed Design**

## **3D Study Case 1**

### **(simulations)**

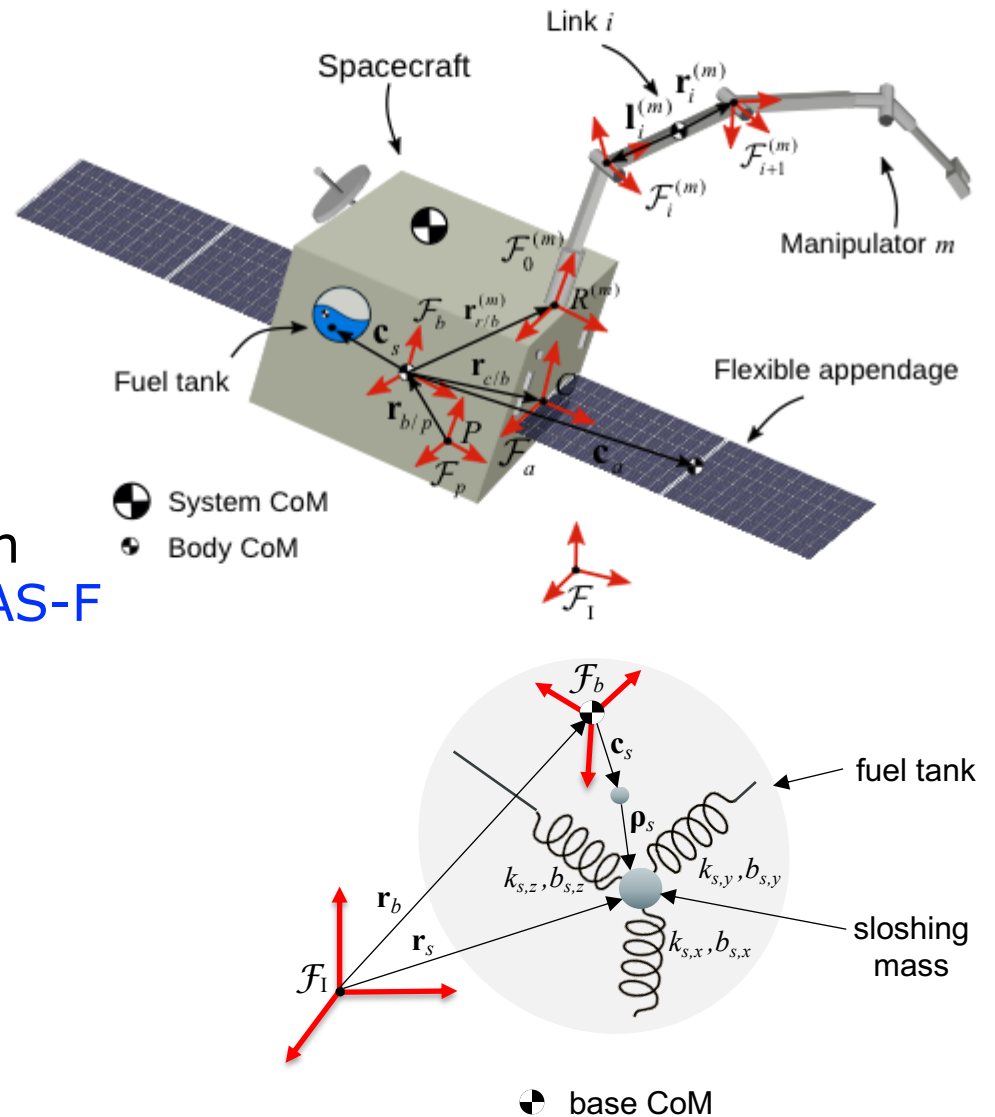
# Analytical Full-scale 3D SC1 Model

## □ SC1 model

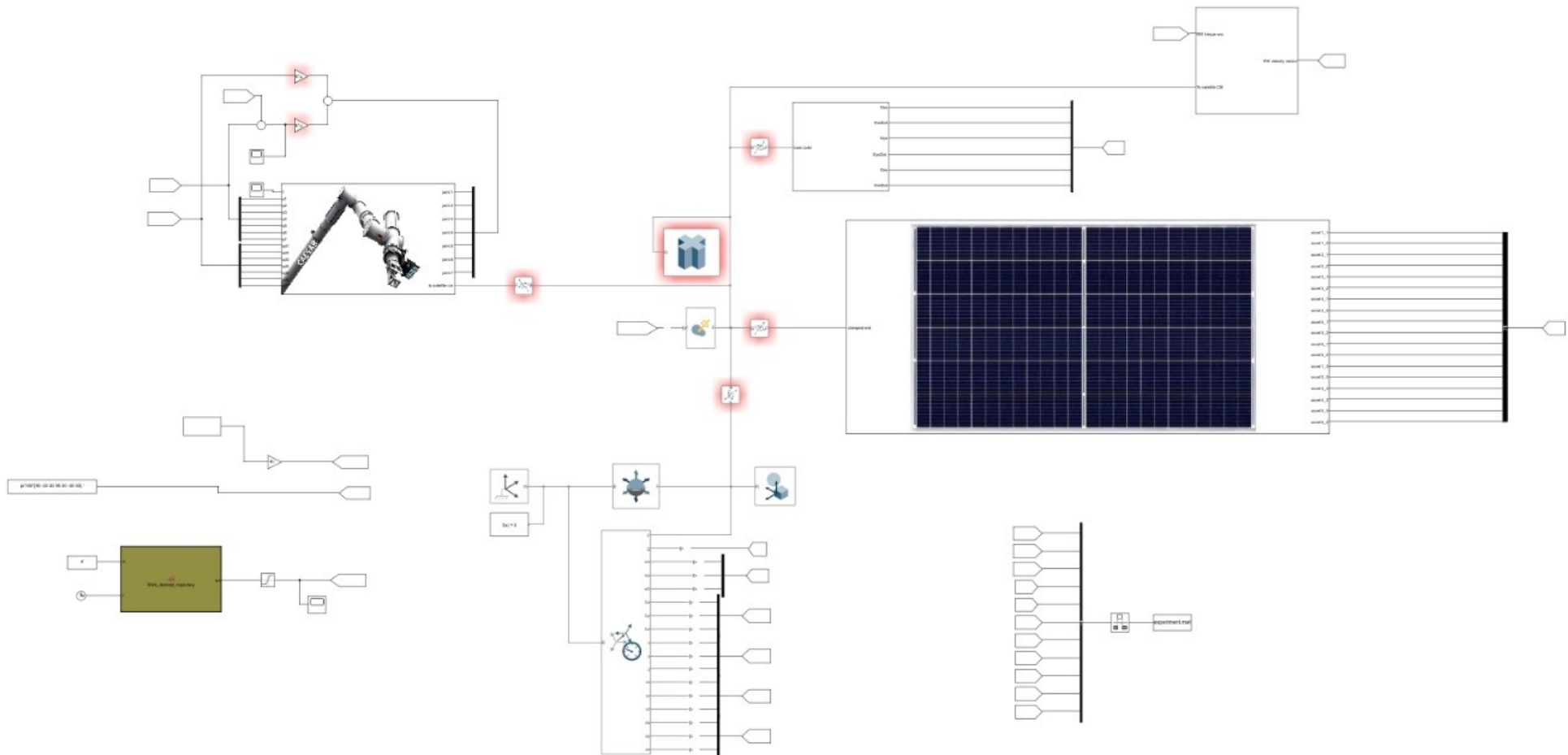
- Quasi-Lagrangian approach
- System equations of motion

## □ Structure & Parameters

- Parameters in accordance with realistic values provided by TAS-F
- Manipulator based on DLR's CAESAR
- Sensors and actuators in accordance with actual ones



# Simscape Full-scale 3D Model



# Sensors and Actuators

## □ Sensors

- IMU
- Sun-tracker/ Star-tracker
- Motor-encoders
- Flexible appendage accelerometers
  - Realistic noise models

## □ Actuators

- Joint motors
- Reaction wheels
- Thrusters

## □ First order low-pass Infinite Impulse Response (IIR)



# Method and Algorithm

□ 2-stage motion (Experiment 1 & 2)

## □ Experiment 1

- Modal Analysis with [SSI-COV](#)
- Parametric SYSID (sloshing model parameters) with [TLS](#) on a Method based on the [System Transfer Function](#)
  - Method [decouples](#) Parametric SYSID from Modal Analysis

## □ Experiment 2

- Parametric SYSID (inertial parameters) with [TLS](#) on a Method based on the [System Energy Balance](#)

□ [Novel estimators](#) for the unmeasurable quantities

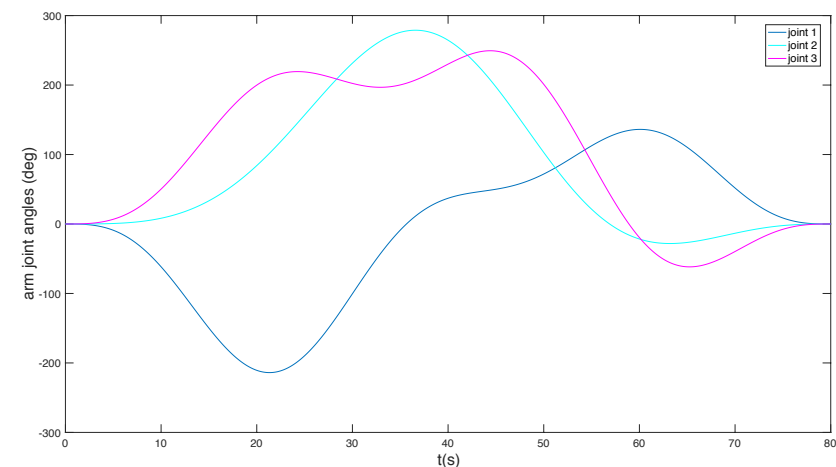
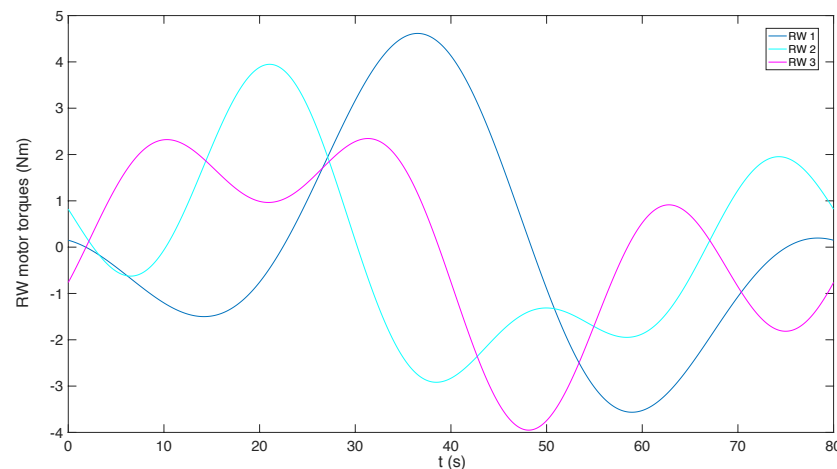
# Excitation & simulated response

## ❑ Experiment 1

- Thruster forces: consecutive pulses

## ❑ Experiment 2

- RW torque input: Truncated Fourier series
- Manipulator torque inputs: PD controller on desired joint trajectories (truncated Fourier series)
- All Fourier series coefficients obtained by **minimizing** regressor matrix **condition number**



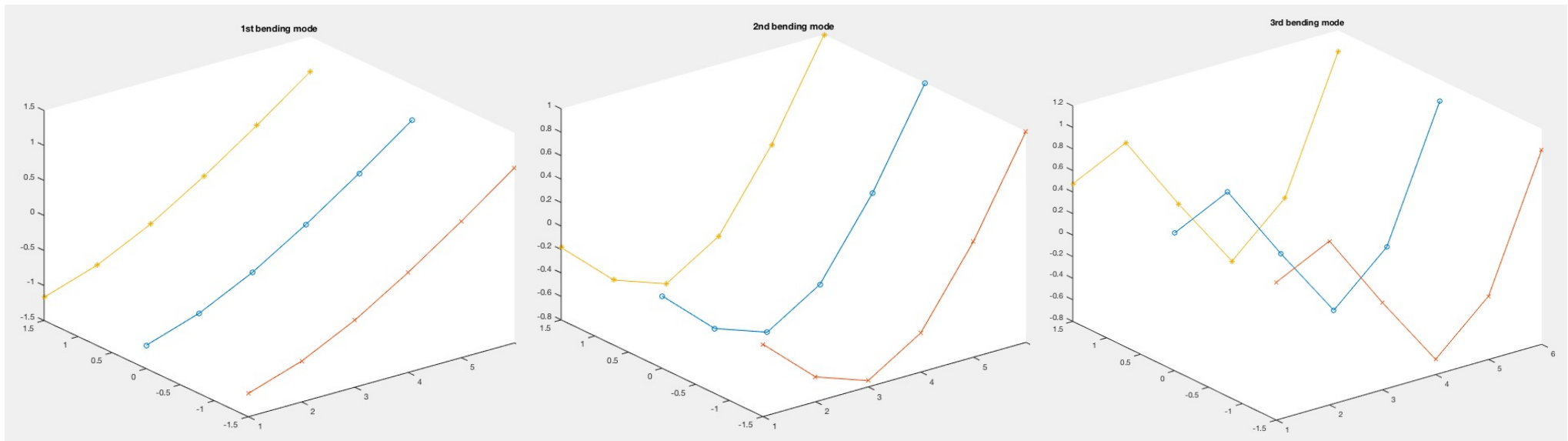
# Experiment 1 SYSID Results

## Modal Analysis

Parameters	(Hz)	(Hz)	(Hz)
Type	bending	bending	bending
True values	0.046	0.286	0.801
Estimated value	0.046	0.287	0.800
Rel. Error (%)	<b>0.114</b>	<b>0.354</b>	<b>0.245</b>

## Parametric (sloshing) SYSID with TLS

Parameter	True Value	Estimated Value	Relative error (%)
<b>M</b>	1023.55	1022.22	<b>0.129</b>
<b>m<sub>s</sub></b>	49.6	49.90	<b>3.41</b>
<b>k<sub>s,x,y,z</sub></b>	0.41	0.41	<b>0.788</b>
<b>b<sub>s,i</sub></b>	0.02	-	-
<b>ρ</b>	2700	2761.17	<b>2.266</b>



# Experiment 2 SYSID Results

## Parametric (inertial) SYSID

Parameter	True Value	Estimated Value	Relative error (%)
$\pi'_m(1)$	235904.27	232816.76	1.31
$\pi'_m(2)$	42646.93	42500.42	0.34
$\pi'_m(3)$	216860.44	215087.54	0.82
$\pi'_m(4)$	-43783.03	-44874.32	-2.49
$\pi'_m(5)$	-78364.67	-76945.42	-1.81
$\pi'_m(6)$	-16799.40	-17113.4	-1.87
$\pi'_m(7)$	-674.38	-695.10	-3.07
$\pi'_m(8)$	-3145.80	-3127.54	-0.58
$\pi'_m(9)$	-1205.82	-1190.96	-1.23
$\pi'_m(10)$	-0.50	-0.53	<b>-5.83</b>
$\pi'_m(11)$	-1.50	-1.44	-3.85
$\pi'_m(12)$	-0.60	-0.62	-4.14
$\pi'_m(13)$	837.41	835.22	0.26
$\pi'_m(14)$	837.42	837.65	0.03
$\pi'_m(15)$	-720.27	-715.63	-0.64
$\pi'_m(16)$	720.32	716.36	0.55
$\pi'_m(17)$	150.00	149.28	0.48
$\pi'_m(18)$	-117.04	-121.40	-3.72
$\pi'_m(19)$	117.09	122.08	4.26
$\pi'_m(20)$	50.00	51.67	3.34
$\pi'_m(21)$	-101157.00	-103746.97	-2.56
$\pi'_m(22)$	-471870.00	-466707.79	-1.09
$\pi'_m(23)$	-180873.00	-177657.18	-1.78
$\pi'_m(24)$	-33719.00	-35920.32	<b>-6.53</b>
$\pi'_m(25)$	-157290.00	-161684.34	-2.79
$\pi'_m(26)$	-60291.00	-61632.43	-2.22
$\pi'_m(27)$	7500.00	7586.22	1.15

# Discussion on SC1 Full-scale 3D Simulation (1/2)

- ❑ **Modal Analysis** with **SSI-COV** and **Parametric SYSID** with **TLS** for SC1 (**Experiment 1**), are deemed as **successful** in identifying the first three **natural frequencies** and the **sloshing model parameters**, respectively.
  - Identified parameters within the 5% relative error margin
  
- ❑ **Parametric SYSID** with **TLS** for SC1 (**Experiment 2**), is also deemed as **successful** in identifying the **inertial parameters**.
  - Two parameter clusters marginally outside the 5% error margin
  
- ❑ For computational reasons, the first three flexible panel bending modes and the first three manipulator DoFs only were used

# Discussion on SC1 Full-scale 3D Simulation(2/2)

- ❑ Simulations of a full-scale 3D system yield very good results
  
- ❑ Most of the scaled-down SC1 actual and simulated experiments did not!
  - Sensor resolution is not scaled down according to length scale
  - Space-ready sensors (modelled for the full-scale system) are far superior to the available sensors at the SRE
  - Small disturbances existing in the experimental facility do not exist in space
  - Those small disturbances affect the scaled-down systems more significantly

# **Sensitivity, Robustness, & Sampling Considerations**

# **1. Sensitivity Analysis (preliminary)**

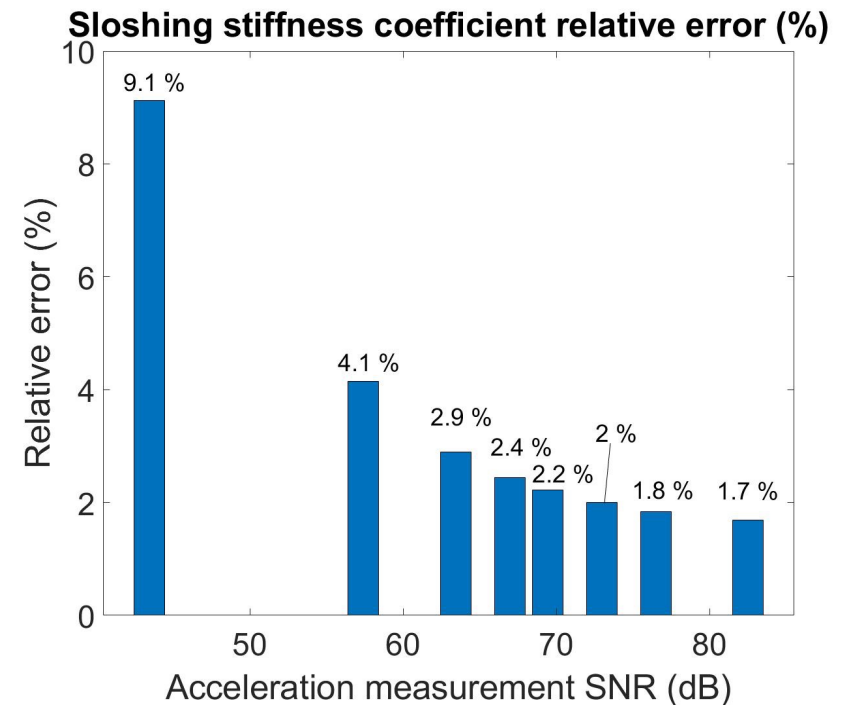
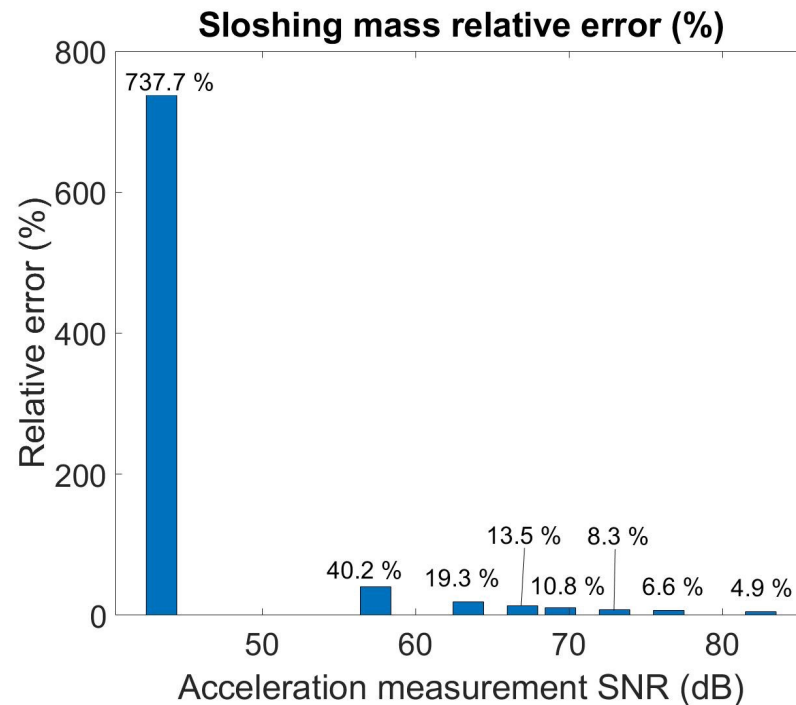


# Sensitivity Analysis Examples

- Identify **factors** whose variation **affects** the **SYSID** process
  - What is the various factors **impact on** the identification **results**?
  - Which **estimated variables** are **impacted most**?
  - To **what extent** can a factor be varied before crossing a pre-defined threshold on an estimated variable?
  
- **Parametric** SYSID Sensitivity Analysis **Illustrative Examples**
  - SC2-Exp2: **SNR**
  - BP1A: **Mass ratio of manipulator – S/C**
  
- **Modal** SYSID Sensitivity Analysis **Illustrative Examples**
  - BP3: **SNR**
  - BP3: **Hub inertia**

# Parametric SYSID Sensitivity Analysis (1/2)

## □ SNR for SC2-Exp2





# Parametric SYSID Sensitivity Analysis (2/2)

□ Manipulator – S/C mass ratio for BP1A

Mass ratio	$a_1$ error (%)	$a_2$ error (%)	$a_3$ error (%)	$a_4$ error (%)	$a_5$ error (%)	$a_6$ error (%)	$a_7$ error (%)	$a_8$ error (%)
60	-1.204	-4.458	7.497	12.222	0.073	1.845	1.031	4.509
40	-1.199	-4.443	7.475	12.206	0.072	1.839	1.031	4.481
25.92 (nominal)	-1.192	-4.421	7.457	12.181	0.069	1.830	1.033	4.437
20	-1.187	-4.404	7.443	12.162	0.068	1.823	1.034	4.401
10	-1.165	-4.346	7.401	12.092	0.061	1.795	1.039	4.254
5	-1.133	-4.291	7.380	12.015	0.051	1.752	1.041	4.009

- Nonnegligible but small effect
- Almost all relative errors decrease as the manipulator-to-S/C mass ratio increases

# Modal SYSID Sensitivity Analysis

- ❑ SNR for BP3  very small increase of errors with SNR variation, after a quite low dB threshold
- ❑ Hub inertia for BP3  very small effect

## Discussion

- SNR increase leads to a dramatic improvement of SYSID results
- Subsystems mass ratio variations have limited effect
- Future work suggestions
  - Sensitivity Analysis to be run for all BPs and SCs, for those and other Factors
  - Sensitivity Analysis for simultaneous variation of Factors. Monte-Carlo Analysis

## 2. Robustness Considerations

# Robust On-line Capabilities (1/2)

- ❑ Robust control of a **fundamentally nonlinear system** (e.g., space manipulator), is an **open research issue**
  - Nonlinear robust controllers such as SMC, have known issues (e.g., actuator chattering)
  - NMPC not always convex and computationally expensive
  - Use of LPV, though very good for linearizable systems, is still an open research issue for complex, highly nonlinear systems

# Robust On-line Capabilities (2/2)

## □ Lines of attack

- **Feedback linearization** (model-based control), assisted by a **linear robust controller** (e.g.,  $H^\infty$ )
- **Partial linearization** due to uncertainty results in “disturbance” term with known bounds, related to the uncertainty statistics
- In operational scenarios and as data are collected during task execution, the uncertainty statistics can be obtained on-line
- Online adaptation of controller parameters

# SYSID results statistics

- 100 simulations of BP1A are run with different noise profiles
  - Different seed number on the random number generator

Inertial Parameters Cluster	Mean value	Mean value 95% confidence interval	$\sigma$	$\sigma$ 95% confidence interval
$a_1$	-26.917	[-26.927, -26.907]	0.0496	[0.0436, 0.0577]
$a_2$	-9.224	[-9.242, -9.207]	0.0893	[0.0784, 0.1038]
$a_3$	10.582	[10.553, 10.611]	0.1445	[0.1269, 0.1679]
$a_4$	3.077	[3.067, 3.087]	0.0504	[0.0443, 0.0586]
$a_5$	964.646	[964.51, 964.782]	0.6851	[0.6015, 0.7959]
$a_6$	16.743	[16.731, 16.755]	0.0612	[0.0537, 0.0711]
$a_7$	44.44	[44.428, 44.452]	0.0597	[0.0524, 0.0694]
$a_8$	10.933	[10.916, 10.950]	0.0852	[0.0748, 0.0989]

- Statistics for relative errors (%) are also obtained



# Computational Impact Preliminary Analysis

- ❑ On-line robust controller adaptation requirements using uncertainty statistics derived from a repetitive SYSID process are discussed:
  - in terms of time requirements for the statistics derivation
  - in terms of buffer size
  
- ❑ Additional factors identified
  - CPU available time for the additional computations
  - Additional energy consumed for such computations
  - Closed-loop system stability during robust controller parameter adaptation

# 3. Sampling Rate Considerations

# Parametric SYSID Sampling Rate Considerations

## □ Non-recursive implementation

- 2.5 Hz to 66 Hz
- High sampling rate is **not** a requirement for SYSID
  - **Lower** sampling rate **improves** regressor condition number
  - However, enough data with low sampling rate, leads to prolonged experiments (see 3D SC1)

## □ Recursive implementation

- Several measurements at 50Hz per step, but only a few steps to converge
- **Important future work**: Trade-off between measurements requirement per step vs. steps required for convergence, considering sampling rate and computational realistic constraints

# Modal Analysis Sampling Rate Considerations

- ❑ For both SSI-COV and RSSI-COV
  - To be able to:
    - Identify the largest natural frequency considered having significant effect on system motion
    - Distinguish it from identified spurious modes
  - Then, sampling rate must be at least 2 to 3.5 times the natural frequency

# Project Output Exploitation

# In-Flight Experiments (1/2)

- ❑ Identification of inertial parameters using Parametric SYSID with SPHERES-like
  - With varying inertial parameters
  
- ❑ Identification of modal parameters using Modal SYSID with SPHERES-like
  - Simple panels attached in various positions of chassis
  
- ❑ Identification of inertial parameters of a manipulator using Parametric SYSID with a SPHERES-like or Astrobe-like system
  - Use of manipulator with custom made links (variable inertial parameters)
  - Experiments with emphasis in uncertain grasping and manipulation

# In-Flight Experiments (2/2)

## ❑ Full Mated Experiments

- Orbital Express Mission or EROSS-like experiments
- Satellites for these experiments do not need to be of medium/large scale  
→ exploit the Newspace trend of small satellites

## ❑ Components

- 7dof manipulator-equipped Chaser satellite
- Active Target satellite, with varying inertial properties (e.g., by use of simple mechanisms).
- Control Room can activate/deactivate subsystems, to allow for different SYSID scenarios

## ❑ Indicative experiments

- Experiments like SC1 and SC2 (both with Experimental and Operational excitation) can be considered.

# ECSS Requirements Guidelines

- Accuracy of the Model Parameters
- Measurement Noise & SNR Improvement
- Experimentation



# Conclusions

# Conclusions (1/4)

- ❑ Linearization of a fundamentally nonlinear system, such as a space manipulator, around an equilibrium point, would result in derived system dynamics valid only close to that point.
- ❑ Study of the full nonlinear system was opted
- ❑ Analytical models were verified by comparison to Simscape models responses and (when applicable) by comparison to the experimental facilities system responses

# Conclusions (2/4)

- ❑ Modal analysis is found to be quite successful with SSI-COV and RSSI-COV (except for the damping ratios identification)
- ❑ Parametric SYSID with TLS and RTLS is also found to be quite successful (except for the sloshing damping coefficients identification), provided adequate measurements SNR exists
- ❑ **Recursive** implementations of the Algorithms provided similar results than the **non-recursive** ones (somewhat higher relative errors), but required about **half the time** to yield these results

# Conclusions (3/4)

- It was observed that the SYSID results were **affected by four main factors**:
  - Accuracy of the model parameters knowledge  
When comparing SYSID results with inaccurate estimations of the actual system parameters, then even perfect SYSID may seem erroneous
  - Signal to Noise Ratio (SNR)  
**Solutions: higher excitation** (if possible), **better sensors, filtering** (be careful of the time-shift when online)
  - Sampling Rate
  - Experimental facilities disturbances

# Conclusions (4/4)

- ❑ Even for a **highly-nonlinear, complex system** such as a full-scale spatial Space Manipulator System, the **SYSID results** are quite promising
- ❑ For **easily linearizable systems** (e.g., satellite operating around certain attitude “equilibrium-points”), the **results** are expected to be at least equally good
- ❑ **Standardized** off-line and especially **on-line SYSID** can be very **useful in enhancing robust control performance in space**
- ❑ We are **not “there” yet**, but these initial results are definitely promising, and **the goal looks both “doable” and “worth doing”!**

# Managerial

# Status

- The project has been completed
- Significant delays due to:
  - Covid-19 lockdowns (force majeure)
  - Technical complexity
  - Certain steps where needed that SoW did not include (CCN has been issued for this reason)
- Deliverables completed







**Thank you**