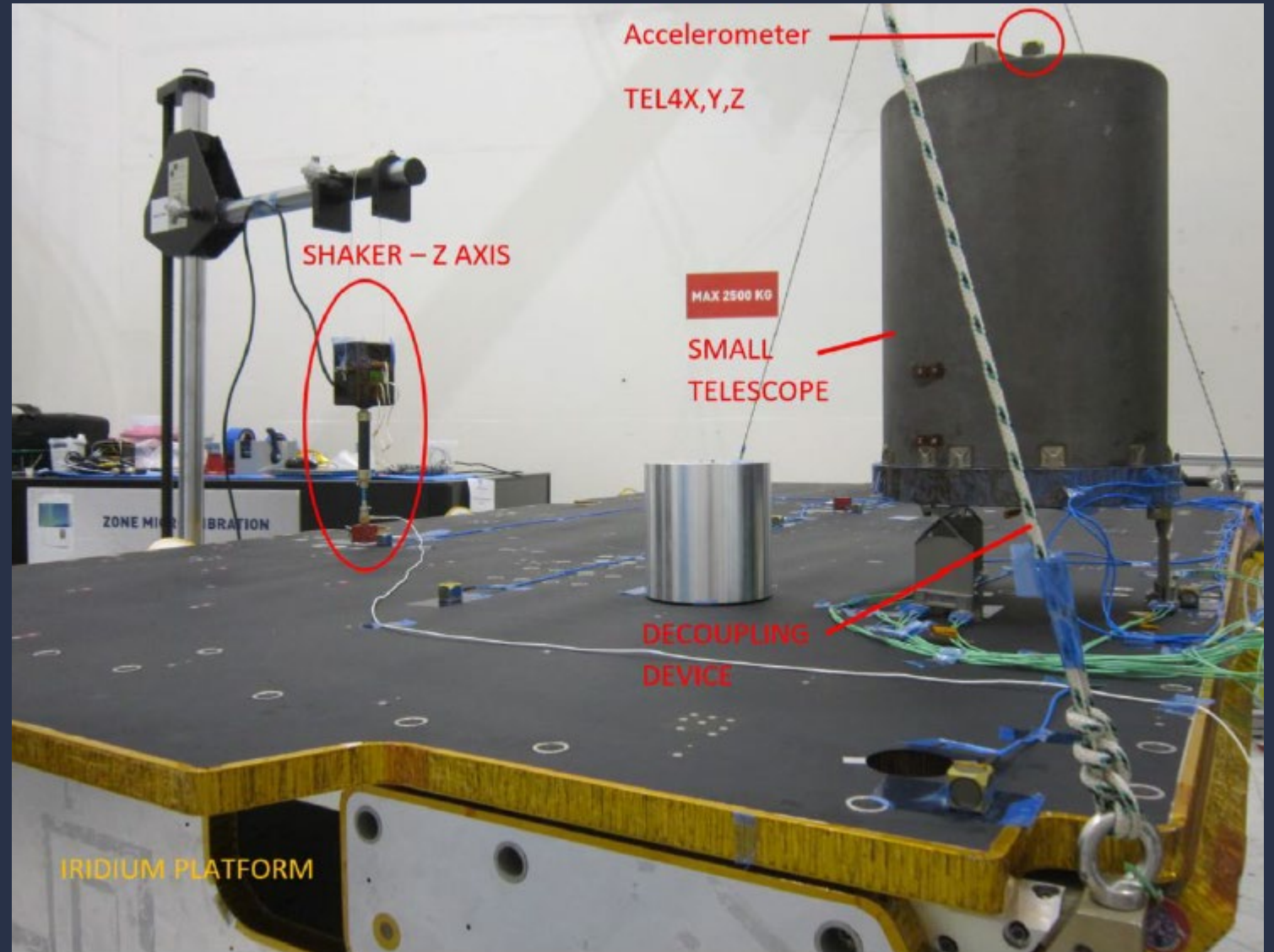


# IMPROVE Improvement of Microvibration Prediction and Verification Methods

Emmanuel ONILLON (CSEM)  
Gilles Carte (TAS)



# Agenda

Project introduction, structure and organization – CSEM

Stepper motor modelling and correlation – CSEM

Cryo cooler motor modelling and correlation – TAS

Time domain summation methodology – CSEM

Frequency domain summation methodology– TAS

Test results - CSEM / TAS

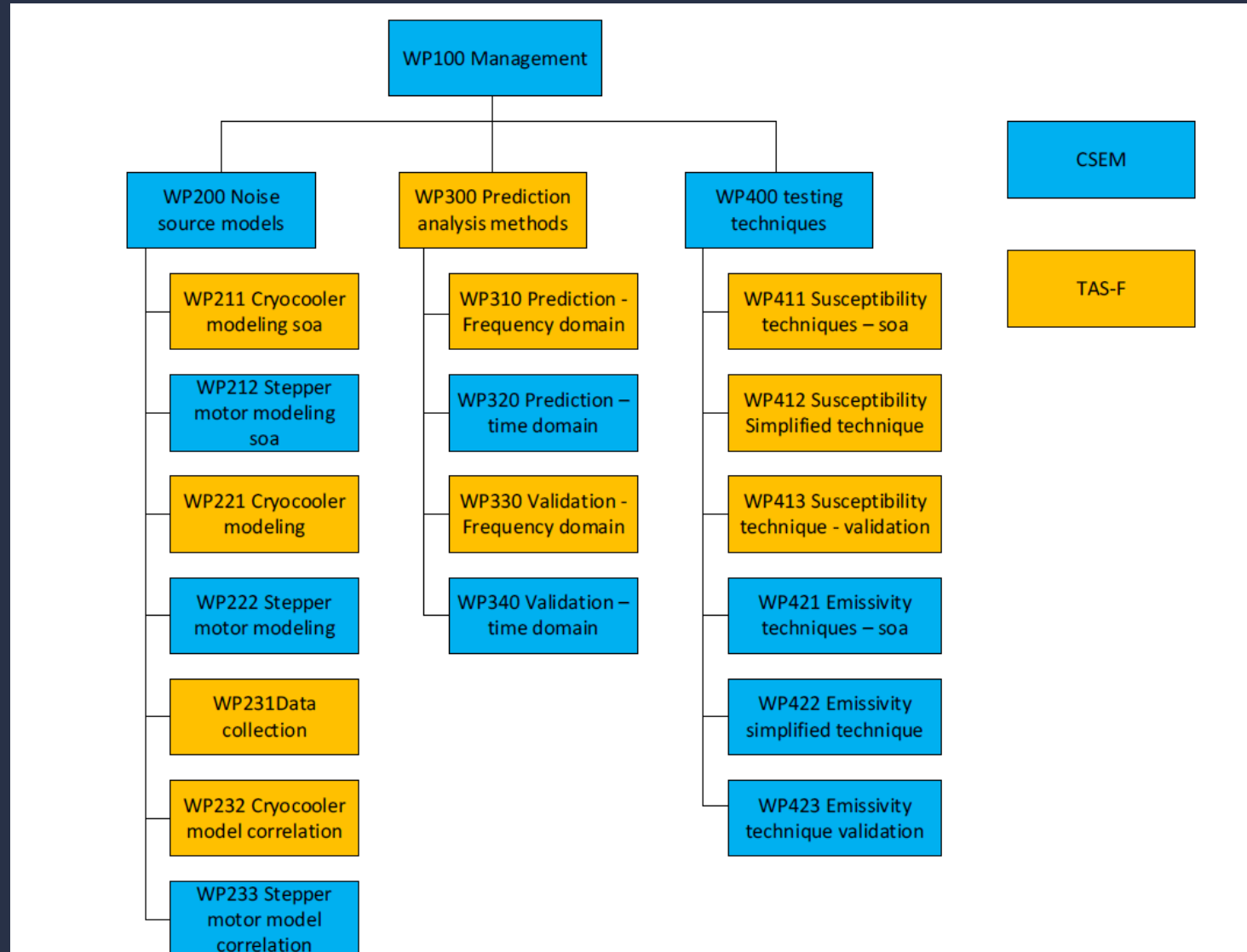
Conclusions

# Overview

- Space missions, especially Science and Earth Observation, have more and more stringent micro vibration requirements. Reaction Wheels, Cryocoolers, Stepper Motors, are among the main sources of micro vibration aboard the satellite.
- Stepper motors are widely employed for motorization in space applications, including deployment, orientation, and accurate pointing positioning mechanisms (e.g., SADM, APM, HDRM)
- Large Pulse Tube Coolers (LPTC) for Infrared focal planes are used in several missions such as the MeteoSat Third Generation (MTG) program.
- Better understand the effect of stepper motor and cryocooler w.r.t micro vibrations

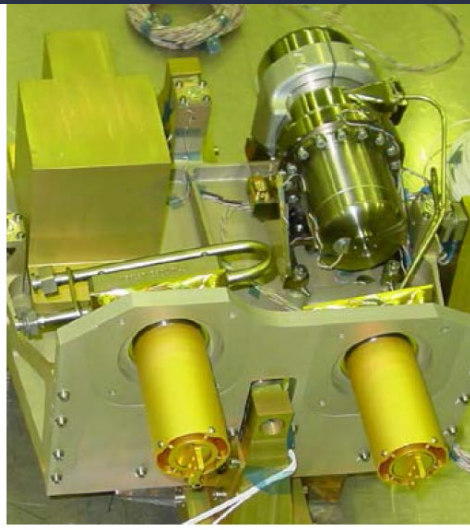


# WBS



## Elements to be modelled – Stepper motor

- Phytron stepper motor with performances close to a Sagem 35 PP
  - Load: solar array (flexible appendage)
- Large Pulse Tube Cooler, EM03Cd, incl cold finger





## Mechanism for prediction method validation

- DSS mechanism developed by TAS-FR
- Diameter:
  - external diameter of the cylinder 302 mm.
- Height: The overall height of the structure is 585.8 mm.
- Resulting output will be considered at mirror level.



## Original planning

- 18 months activity
- KO on 01/2019
- Planned end date 06/2020
- Final end date 02/2022
- 18 months delay

## Delay root cause

- Second stepper test campaign for model development / correlation
- Complexity of cryo cooler / stepper modelling & correlation
- Development and commissioning of CSEM uvib test facility
- Lack of resources on TAS-FR side



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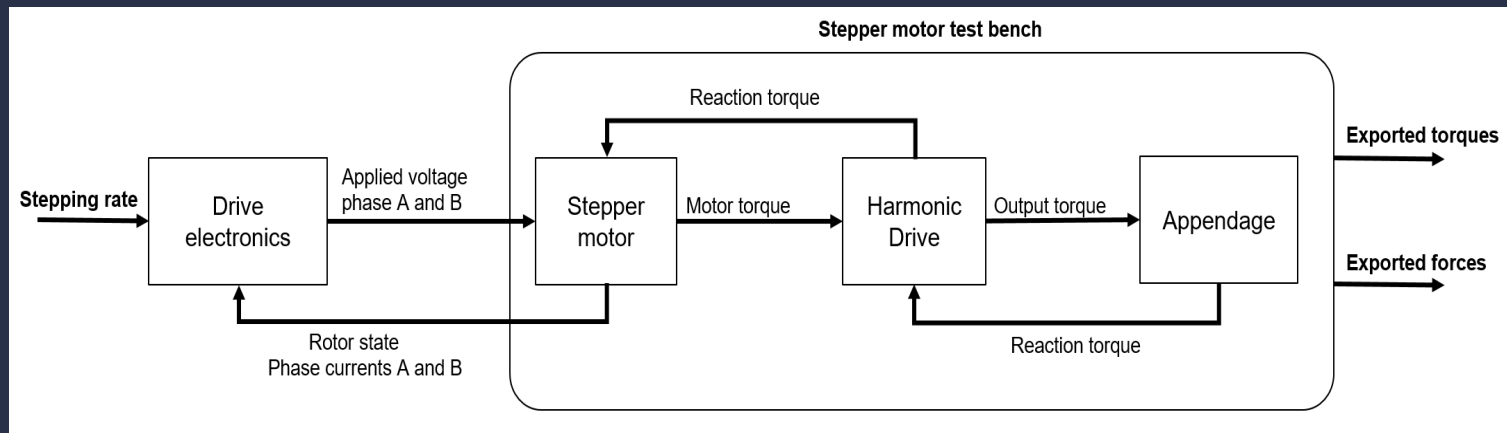
Frequency domain summation methodology– TAS

Test results - CSEM / TAS

Conclusions

# Model architecture

- Model of:
  - The drive electronics
  - Stepper motor
  - Harmonic drive
  - Inertia

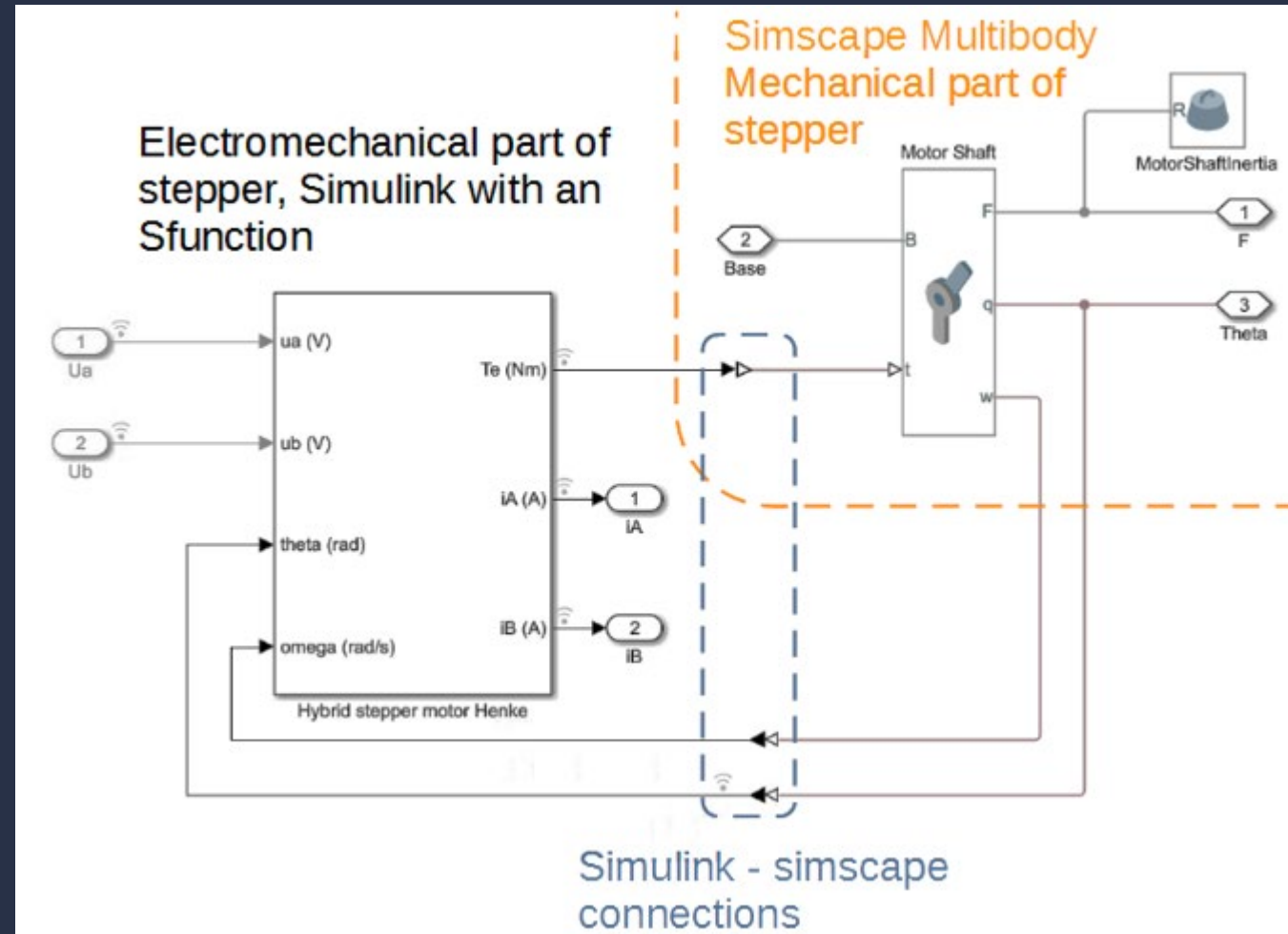


# Model architecture: stepper motor – Henke model

- $\frac{d\omega}{dt} = \frac{1}{J} (T_{el} - T_{det}(\varphi) - T_{load})$
- $\frac{d\theta}{dt} = \omega$
- $\theta = \frac{\varphi}{p_p} = \frac{2}{P} \varphi$
- $\varphi$  is the electrical angle and is related to  $\theta$  /  $p_p$  is the number of pole pairs and  $P$  the number of poles
- The electromagnetic torque comprises two components:
  - the Lorentz force between the permanent magnet in the rotor and the electromagnetic stator windings;
  - the reluctance force between the electromagnetic stator windings and the salient iron end caps of the rotor.
  - $\Psi_M$  is the flux constant resulting from the permanent magnetic flux caused by the permanent magnet in the rotor,  $i_a$  and  $i_b$  are the currents flowing in the phases, and  $L$  is the 2x2 inductance matrix.
- $T_{el} = p\Psi_M \begin{bmatrix} i_a \\ i_b \end{bmatrix}^T \begin{bmatrix} -\sin \varphi \\ \cos \varphi \end{bmatrix} + \frac{1}{2} p_p \begin{bmatrix} i_a \\ i_b \end{bmatrix}^T \frac{\partial L(\varphi)}{\partial \varphi} \begin{bmatrix} i_a \\ i_b \end{bmatrix}$
- $L(\varphi) = L_0 \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} + L_1 \begin{bmatrix} \cos 2\varphi & \sin 2\varphi \\ -\sin 2\varphi & -\cos 2\varphi \end{bmatrix}$
- $\begin{bmatrix} \frac{di_a}{dt} \\ \frac{di_b}{dt} \end{bmatrix} = L(\varphi)^{-1} \left( \begin{bmatrix} u_a \\ u_b \end{bmatrix} - R \begin{bmatrix} i_a \\ i_b \end{bmatrix} - \varphi \frac{\partial L(\varphi)}{\partial \varphi} \begin{bmatrix} i_a \\ i_b \end{bmatrix} - \Psi_M \varphi \begin{bmatrix} -\sin \varphi \\ \cos \varphi \end{bmatrix} \right)$
- $T_{det} = \sum_{k=1}^n a_k \sin k\varphi$

# Model architecture: stepper motor

- Implementation in Simulink / Simscape



## Model architecture: harmonic drive

- $J_{Gear} \frac{d\omega_{Gear}}{dt} = K_{Gear} \left( \frac{\theta}{N_{red}} - \theta_{Gear} \right) - B_{st_{Gear}} \text{sign}(\omega_{Gear}) - B_{dyn_{Gear}} \omega_{Gear}$
- Reaction torque produced by the HD:  $T_{GearRot} = -K_{Gear} \frac{1}{N_{red}} \left( \frac{\theta}{N_{red}} - \theta_{Gear} \right)$
- Implemented in Simulink

$J_{Gear}$  gearbox inertia

$\theta_{Gear}$   $\omega_{Gear}$  outer shaft position / speed of gearbox

$K_{Gear}$  stiffness associated to the connection between the rotor and the outer shaft

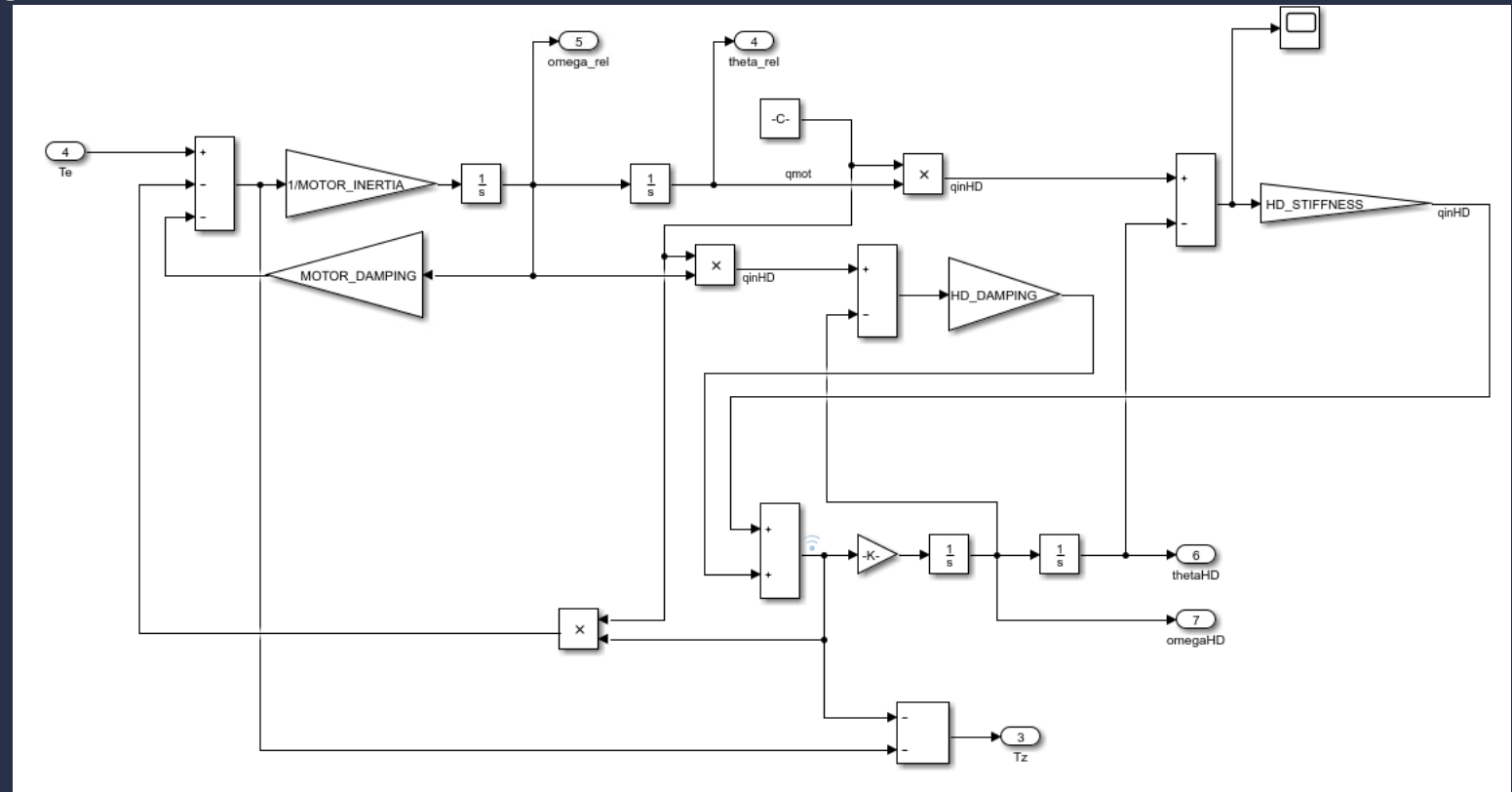
$B_{st_{Gear}}$  and  $B_{dyn_{Gear}}$  are the static / viscous friction coefficients

## Model architecture: harmonic drive

- $J_{HD}\ddot{\theta} = K_{HD}\left(\frac{\theta}{N_{red}} - \theta_{HD}\right) + B_{HD}\left(\frac{\dot{\theta}_{mot}}{N_{red}} - \dot{\theta}_{HD}\right)$
- Reaction torque produced by the HD:  $T_{HD} = -J_{HD}\ddot{\theta}$
- Implemented in Simulink

For forces:

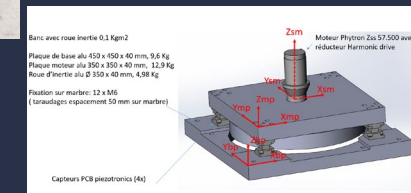
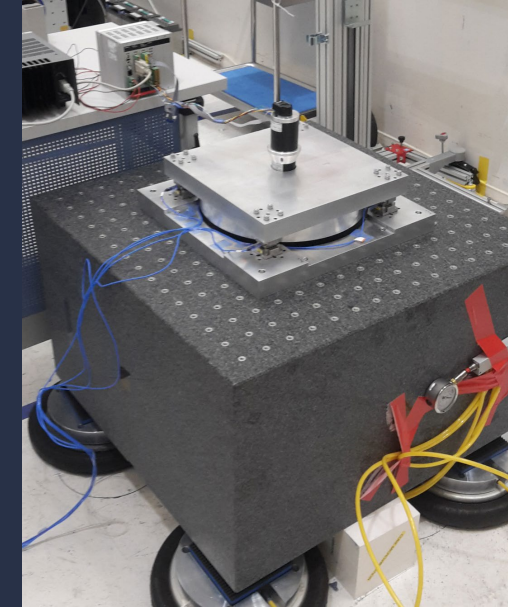
Similarly a second unbalance is added to the HD output inertia



# Stepper motor Configuration

- Phytron ZSS 57.500

Parameters	Value
Motor pole pairs $p_p$	125
Harmonic drive reduction ratio $N_{red}$	100
Motor inertia $J_{Mot}$	Motor: 2.4e-5 kgm <sup>2</sup> Harmonic drive 3.3e-6 kgm <sup>2</sup> Total 2.7e-5 kgm <sup>2</sup>
Motor constant (equal to $p\Psi_M$ )	0.338 Nm/A
Motor detent torque coefficients $a_k$ , with k from 1 to 4.	[30 mNm 0 0 1 mNm ]
Current amplifier closed-loop bandwidth	1000 Hz



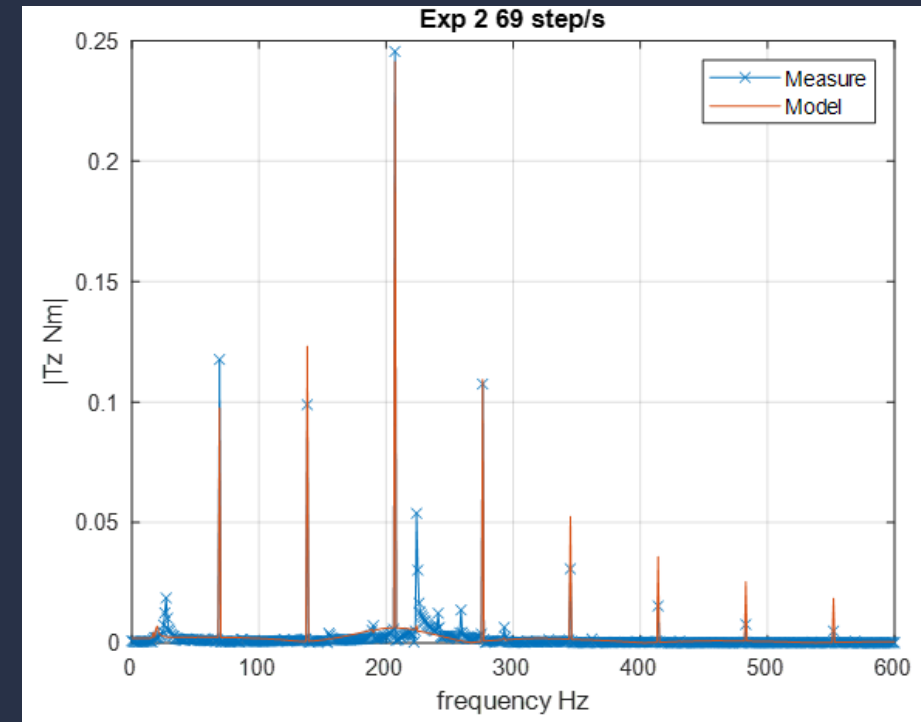
Associated with an harmonic drive from the CSG-CH family with a 100-reduction factor to drive a flexible appendage.



# First campaign results - Exported torque

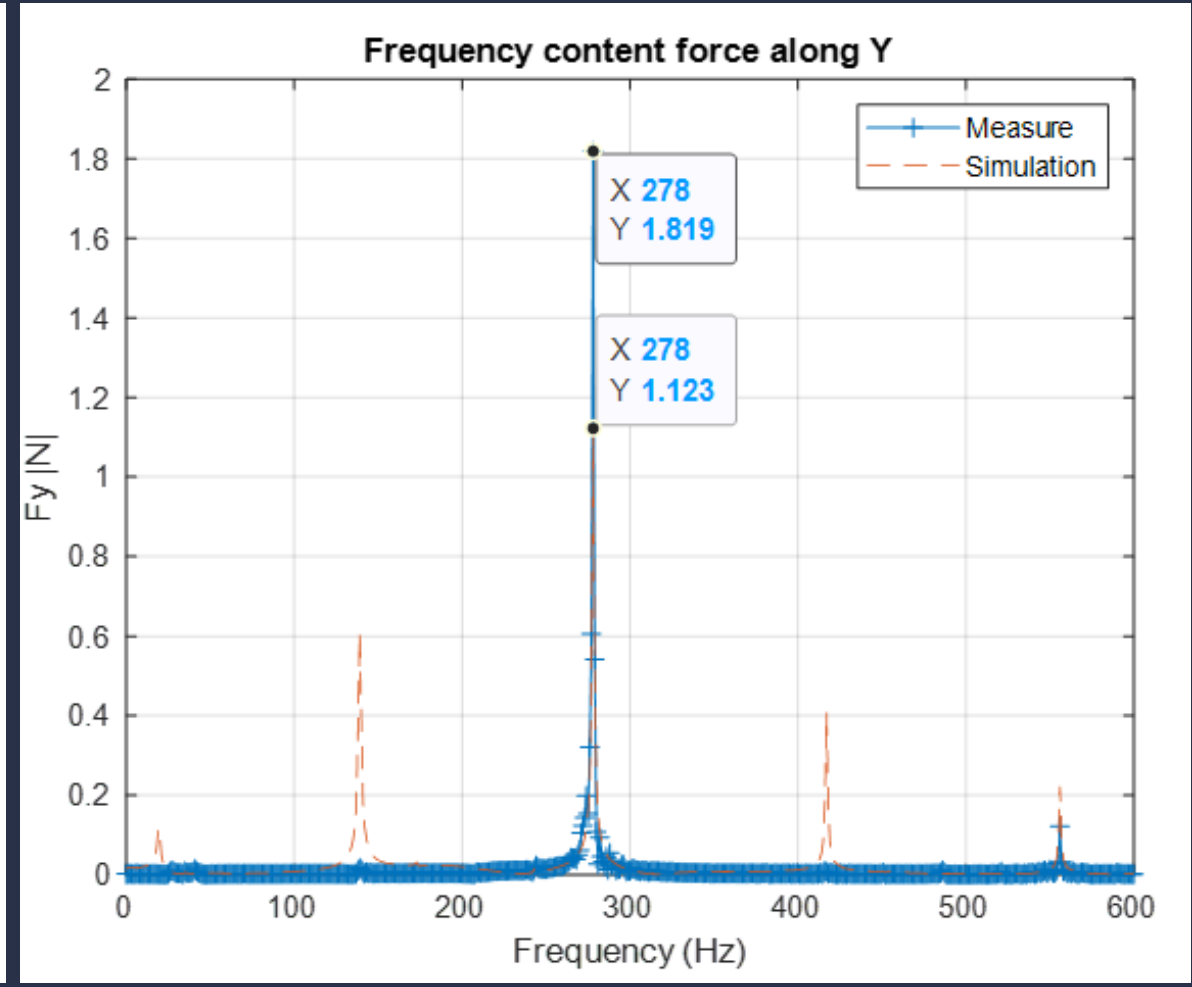
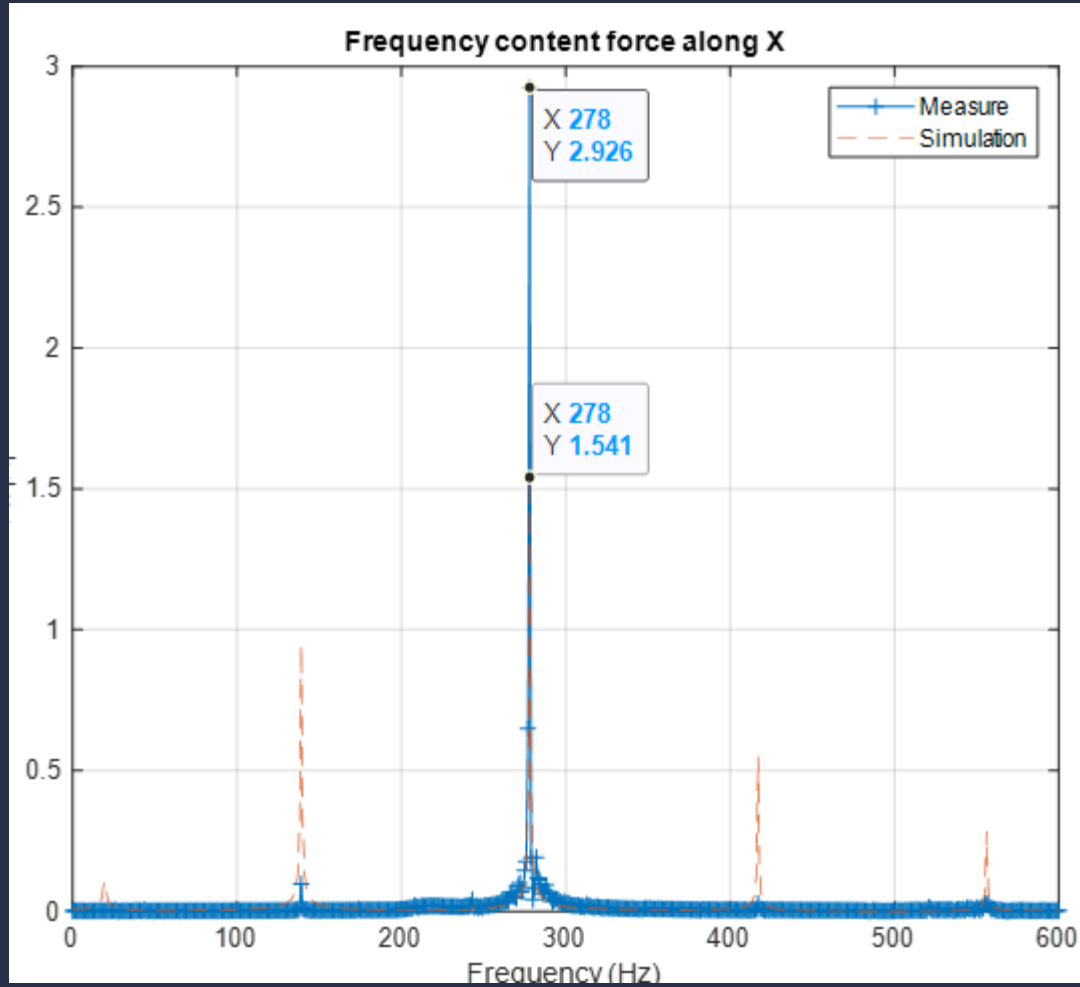
- Full system measurement at TAS-FR

Parameters	Range	Optimized value
Harmonic drive viscous friction $B_{dynGear}$ (Nms/rad)	[0.5 3]	0.90894
Harmonic drive output stiffness $K_{Gear}$ (Nm/rad)	[1500 2900]	1501.1
Motor viscous damping $B_{dynMot}$ (Nms/rad)	[1e-2 0.1]	0.014265
Motor inertia $J_{Mot}$ (kgm2)	2.7e-5 3.5e-5	3.145e-05
Cost function (estimated 0-600 Hz)	N.A.	271.3



Stepper motor

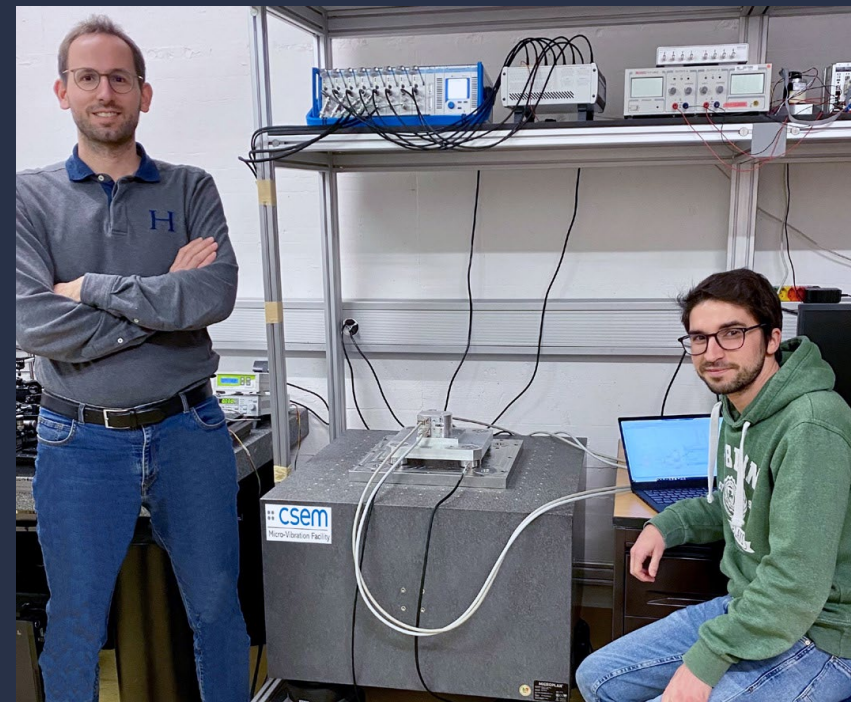
## First campaign results -. Exported forces



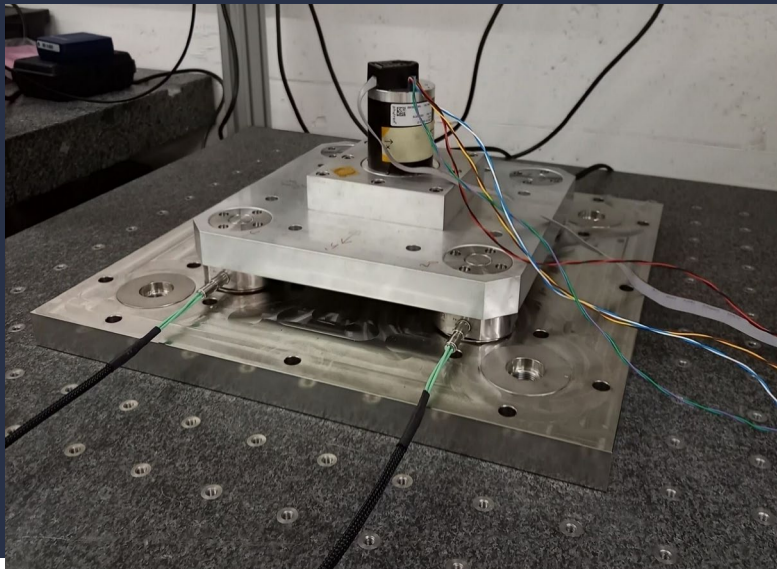
Stepper motor

## Second test campaign

- Dedicated test campaign element per element
- Development of a dedicated micro-vibration facility
- Support of HEIG-VD for HD characterization



Vibration characterization facility



4x Kistler 9067 triaxial force sensors

1x topplate, ad-hoc design by CSEM

1x bottom plate, ad-hoc design by CSEM

1x Granite table, ad-hoc design by CSEM

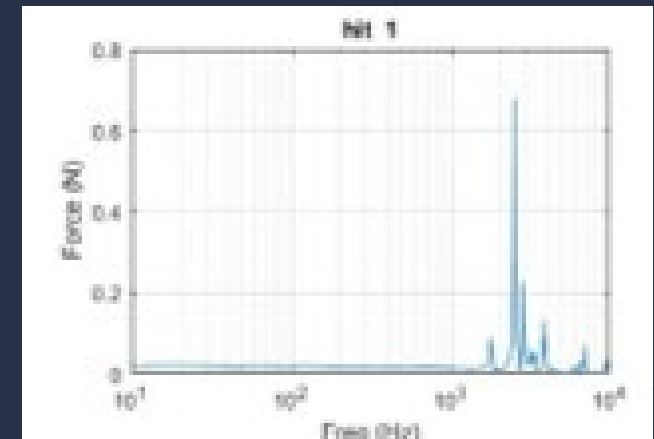
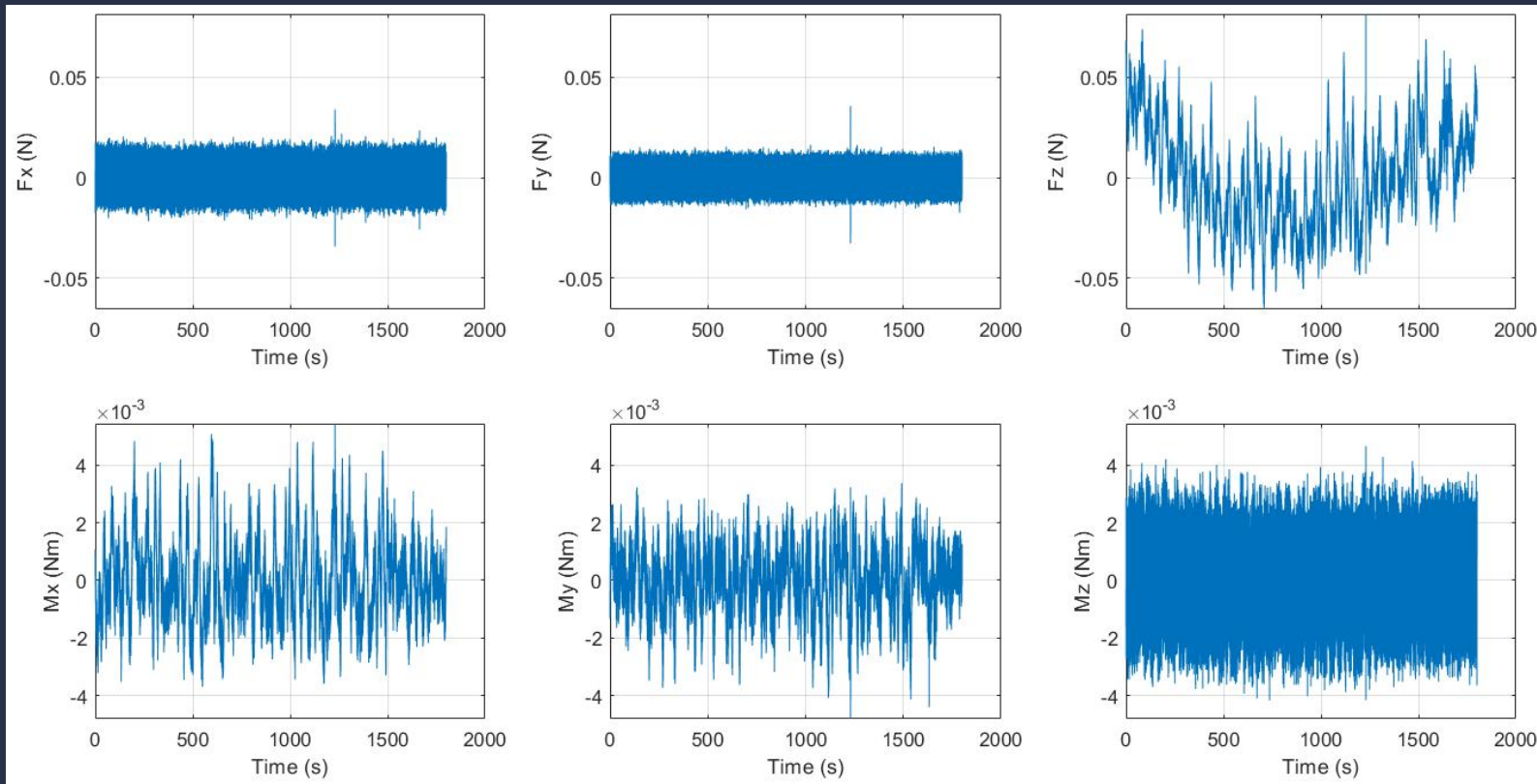
4x Passive pneumatic Isolators Newport SL-1200-410

Kistler 5080 charge amplifier

:: csem

## Second test campaign

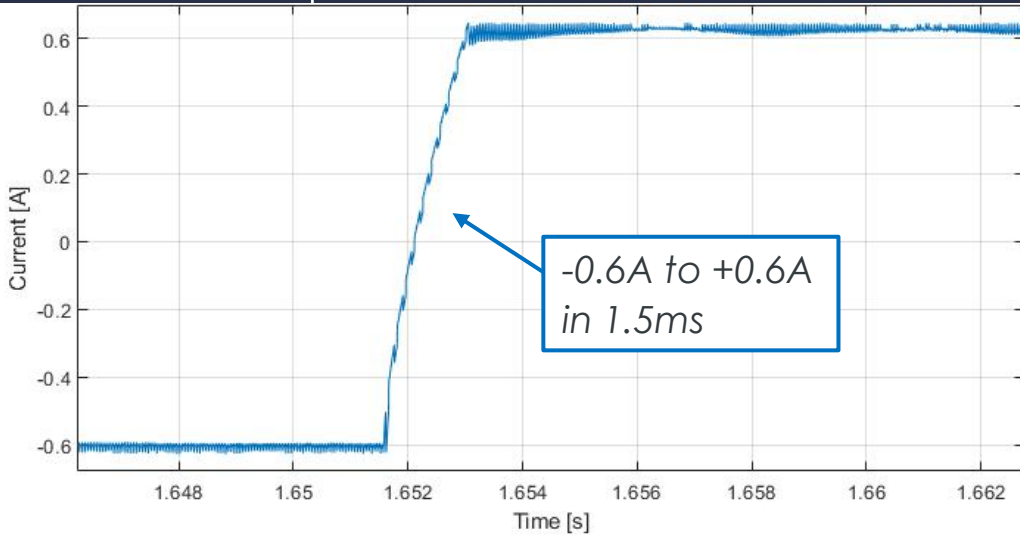
- Noise 50 mN in force / 4 mNm in torque
- Hammer tests to see mechanical modes: above 2 kHz



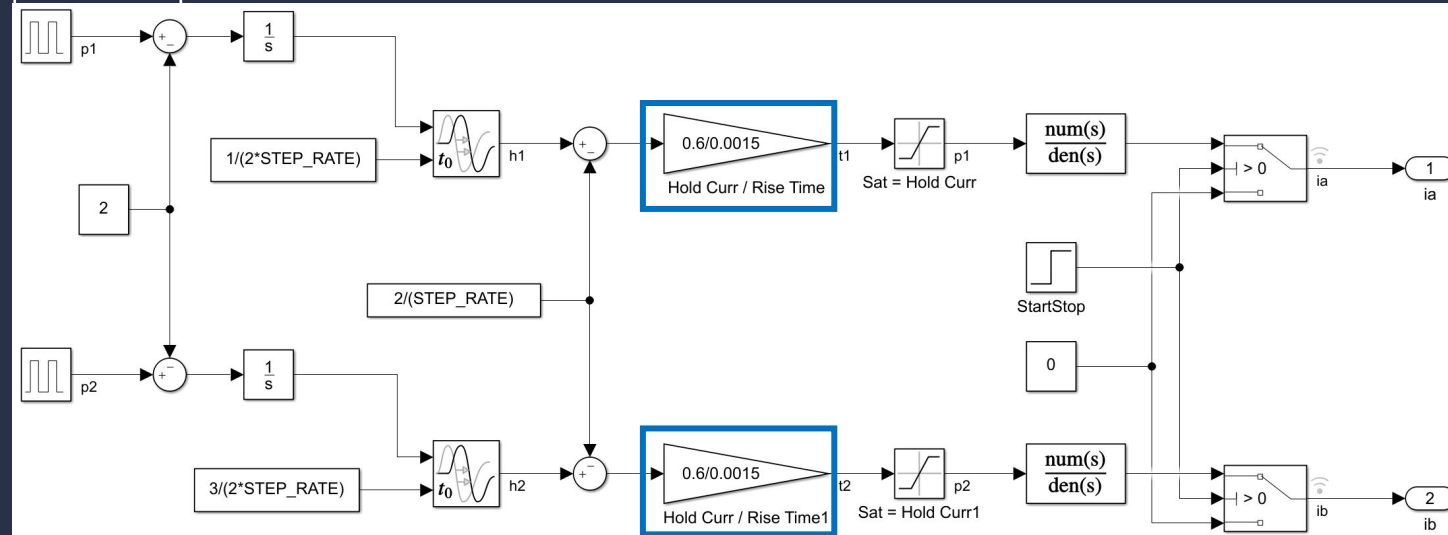
# Model adaptation - *Electrical*

- Phase current was measured and ramp behavior observed
- Modeled as a clipped triangular wave

measurement



model



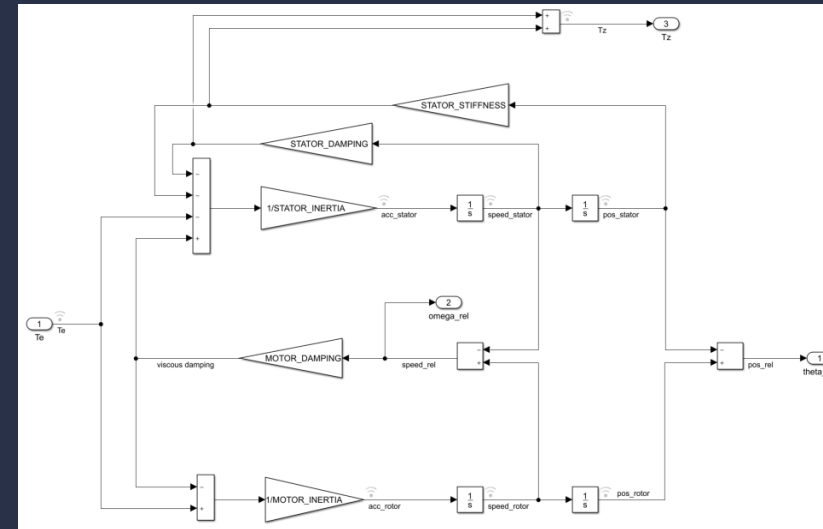


## Model adaptation - Mechanical

- Introduction of stator dynamics (in addition to rotor dynamics)

$$J_S \ddot{\theta}_S = -T_e + C_R(\dot{\theta}_R - \dot{\theta}_S) - K_S \theta_S - C_S \dot{\theta}_S$$

$$J_R \ddot{\theta}_R = T_e - C_R(\dot{\theta}_R - \dot{\theta}_S)$$



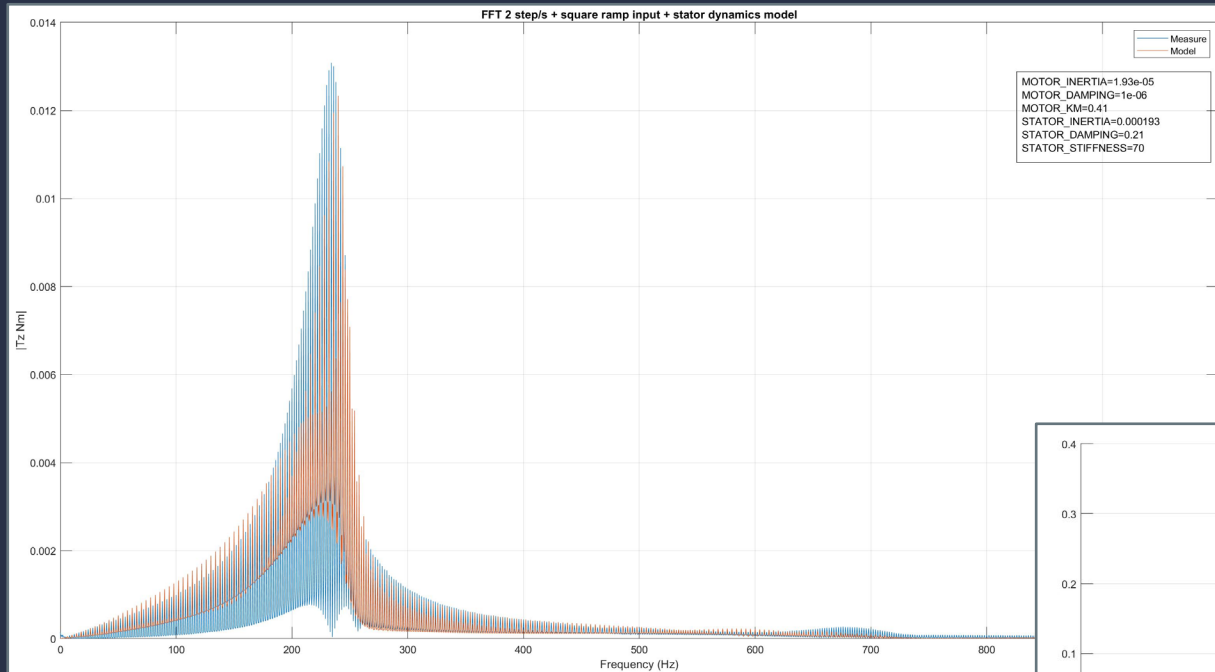
- Introduction of exported forces model (rotating unbalance)

$$F_x = M_R(\dot{\theta}_R^2 \cos(x + \varphi) + \ddot{\theta}_R \sin(x + \varphi))$$

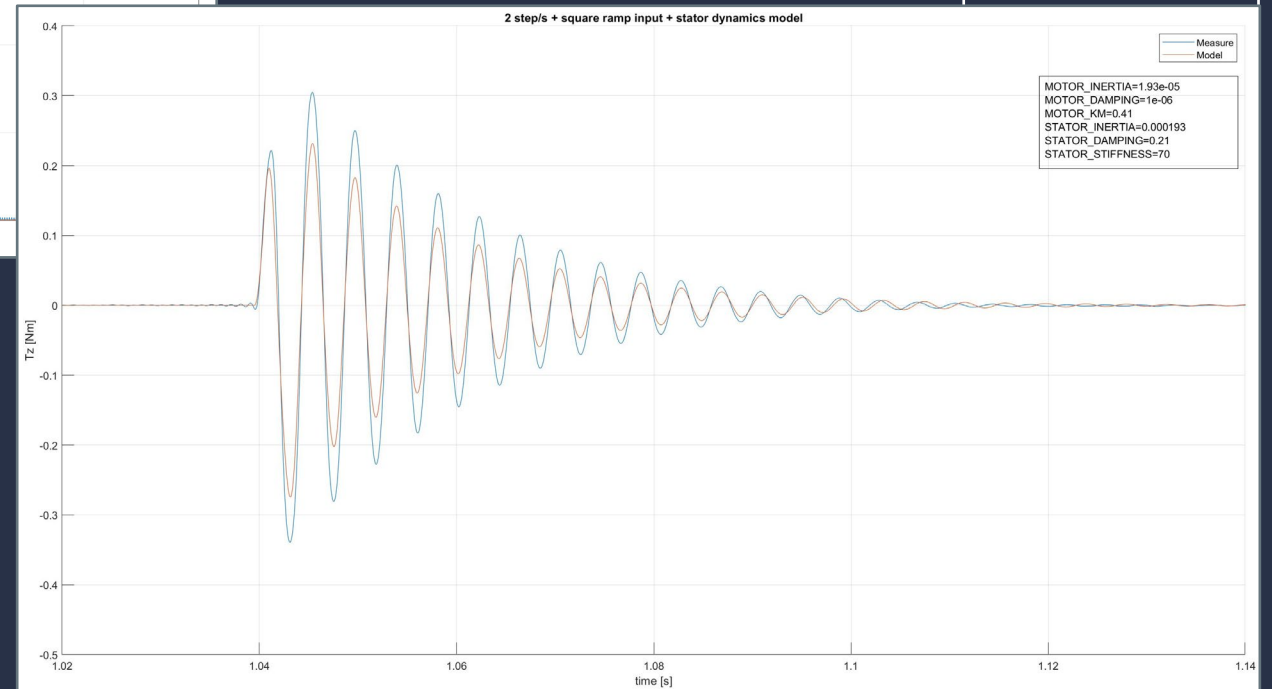
$$F_y = M_R(\dot{\theta}_R^2 \sin(x + \varphi) + \ddot{\theta}_R \cos(x + \varphi))$$

# Stepper motor

## Results – Torque



Frequency domain

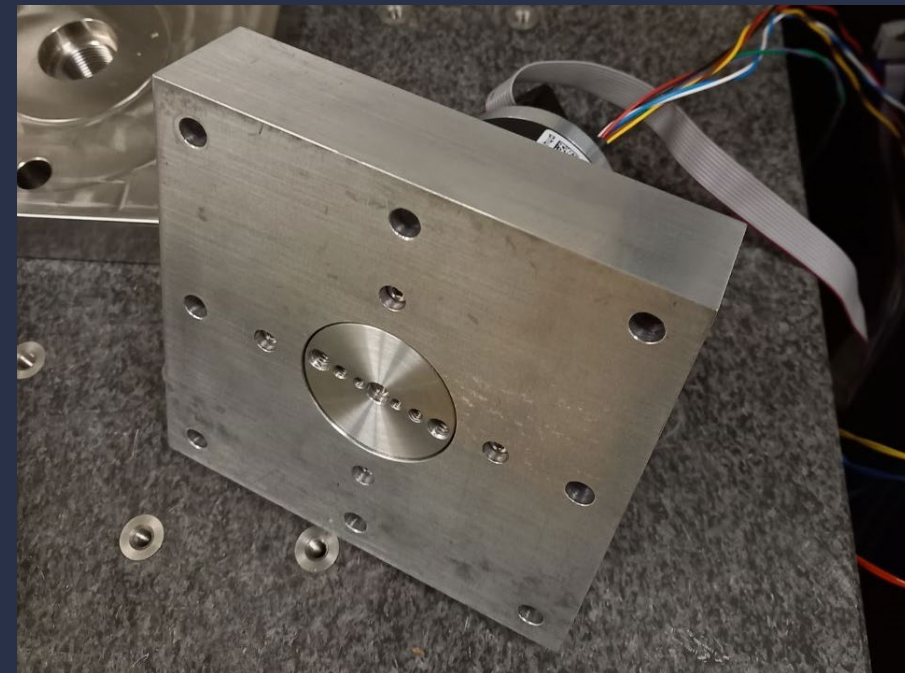
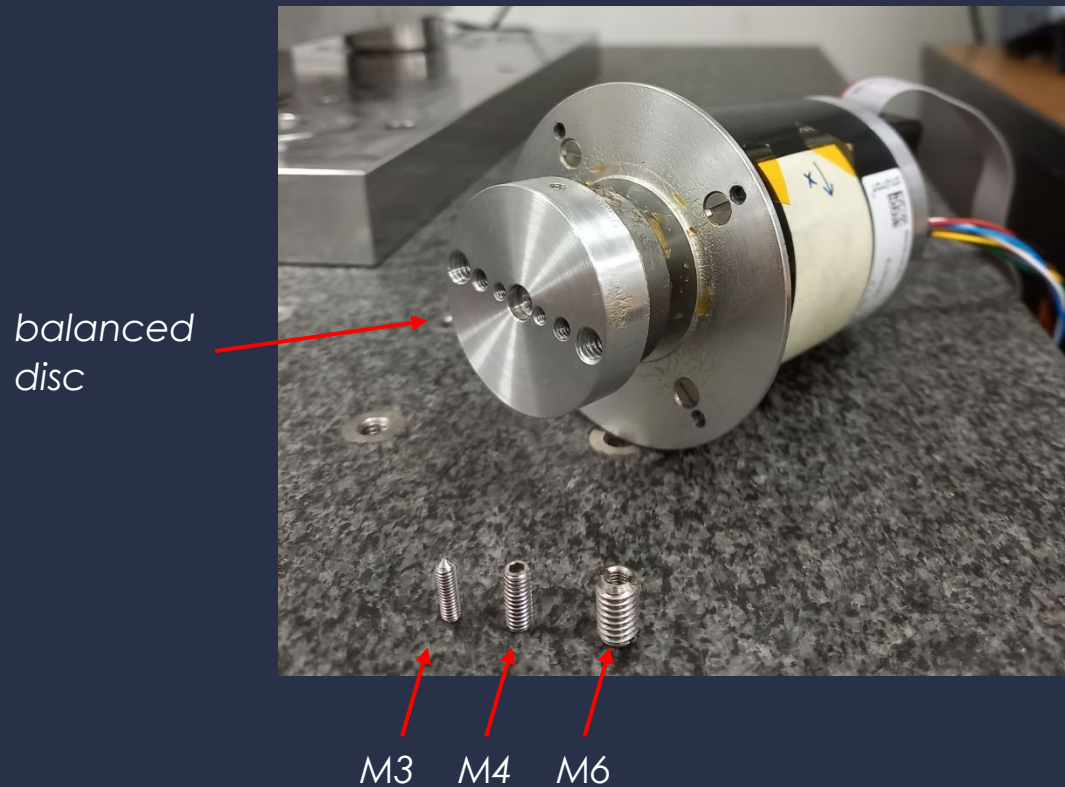


Time domain



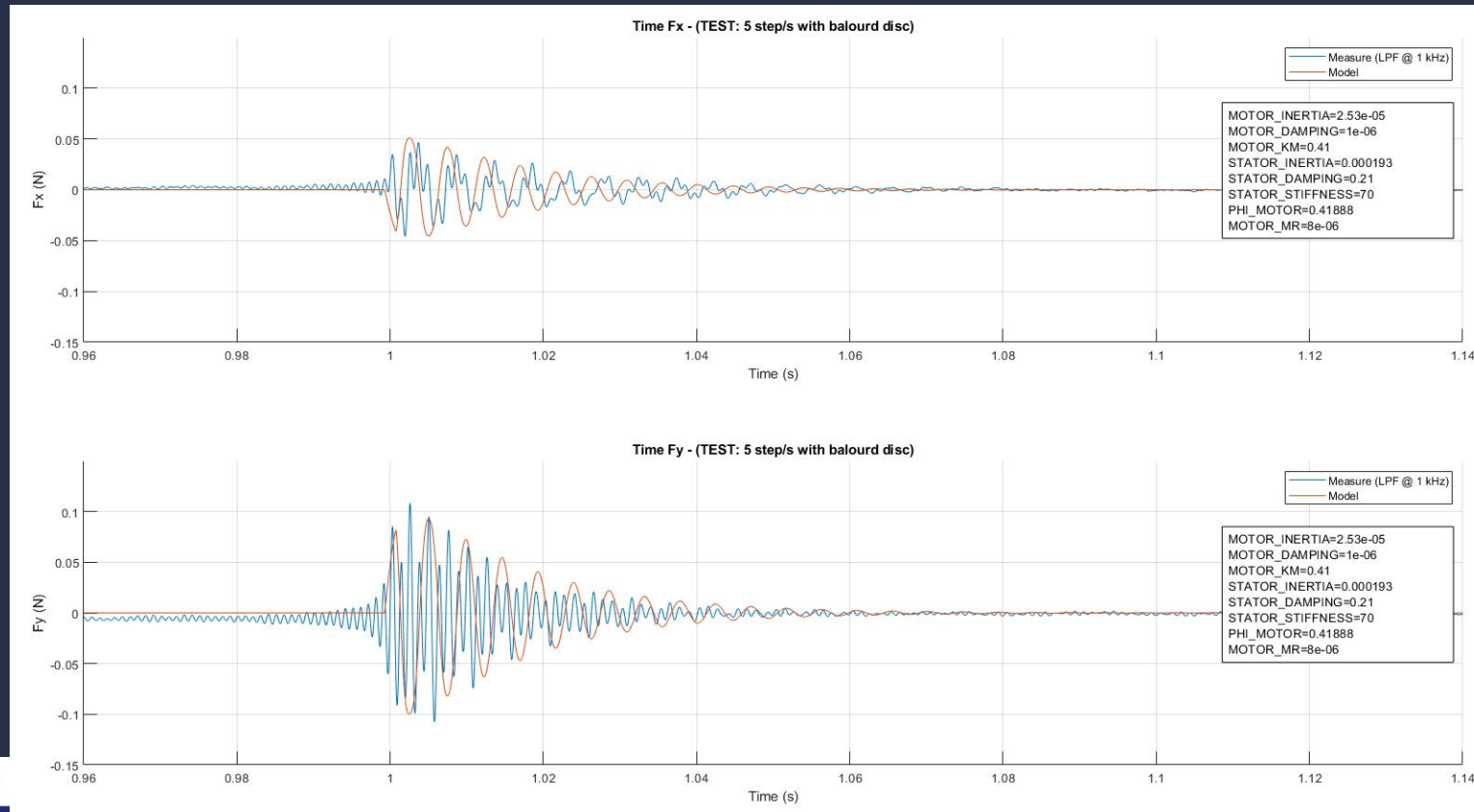
## Results – Forces

- Measurement of controlled rotating unbalance (using screws of varying mass at varying distances from SM axis)



## Results – Forces

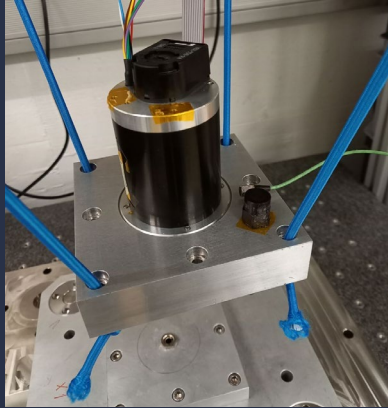
- As the higher modes are unaccounted for in the model, correlation of the model to the measured data is imprecise
- Parameters optimised for torque were kept unchanged and parameters related to rotating unbalance ( $\phi_{\text{motor}}$  and  $\text{motor}_{\text{mr}}$ ) were optimised



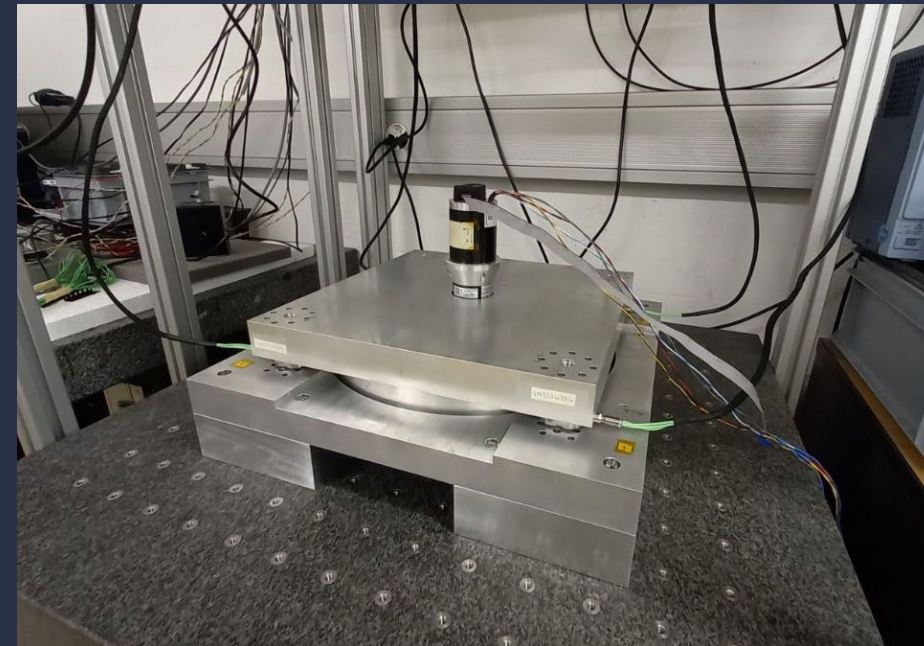
# Summary of Tests

- *Torque model*: in both time and frequency (up to 1 kHz) domains, correlates well
- *Forces model*: in time domain, envelope correlates well
- *Forces model*: in frequency domain, correlates well at low frequencies

*suspension test*



*full system with small inertia*



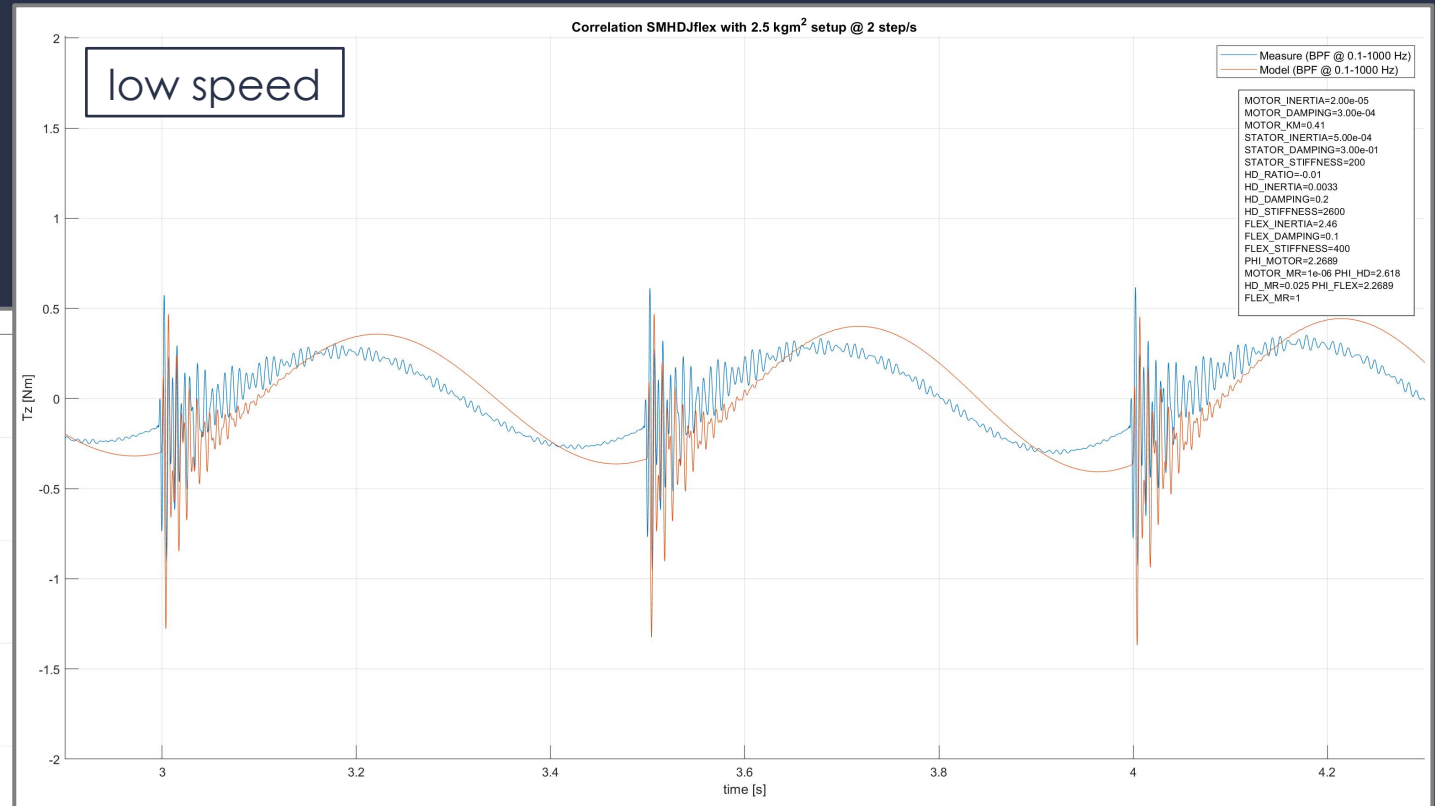
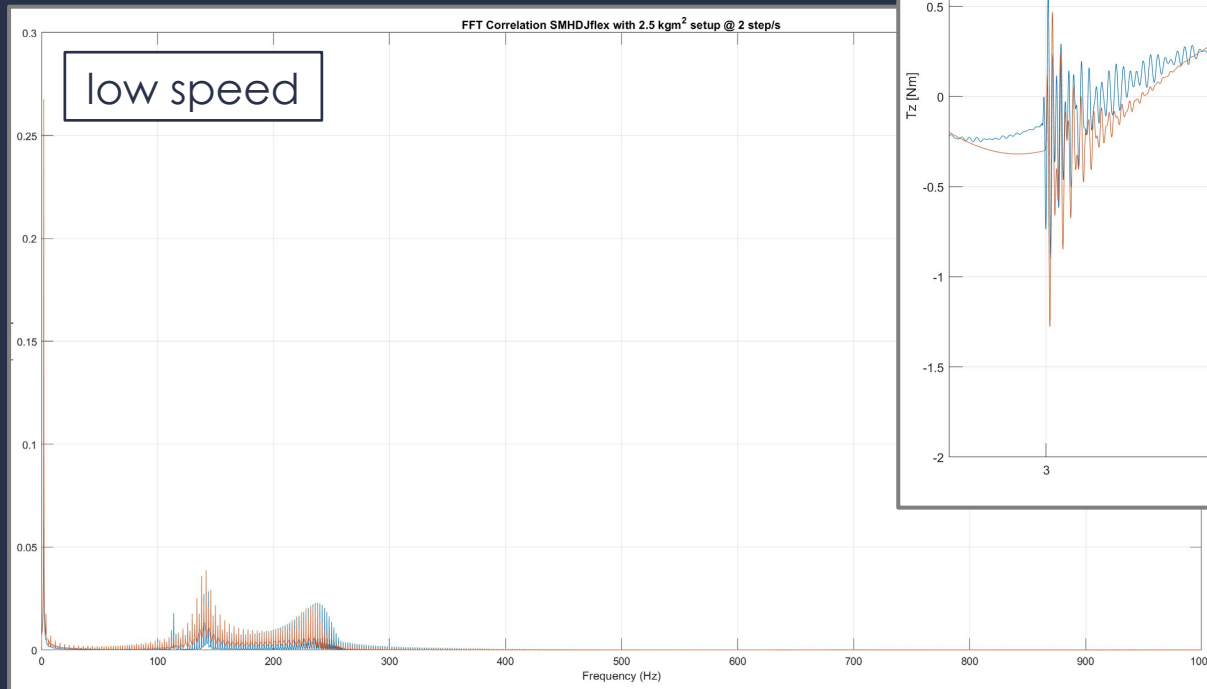
# Stepper motor Correlation:

primary torque  $T_z$  (test bench #3) →

FULL SYSTEM:

- with harmonic drive
- with load (large)

- Measurement in **blue**
- Model in **orange**





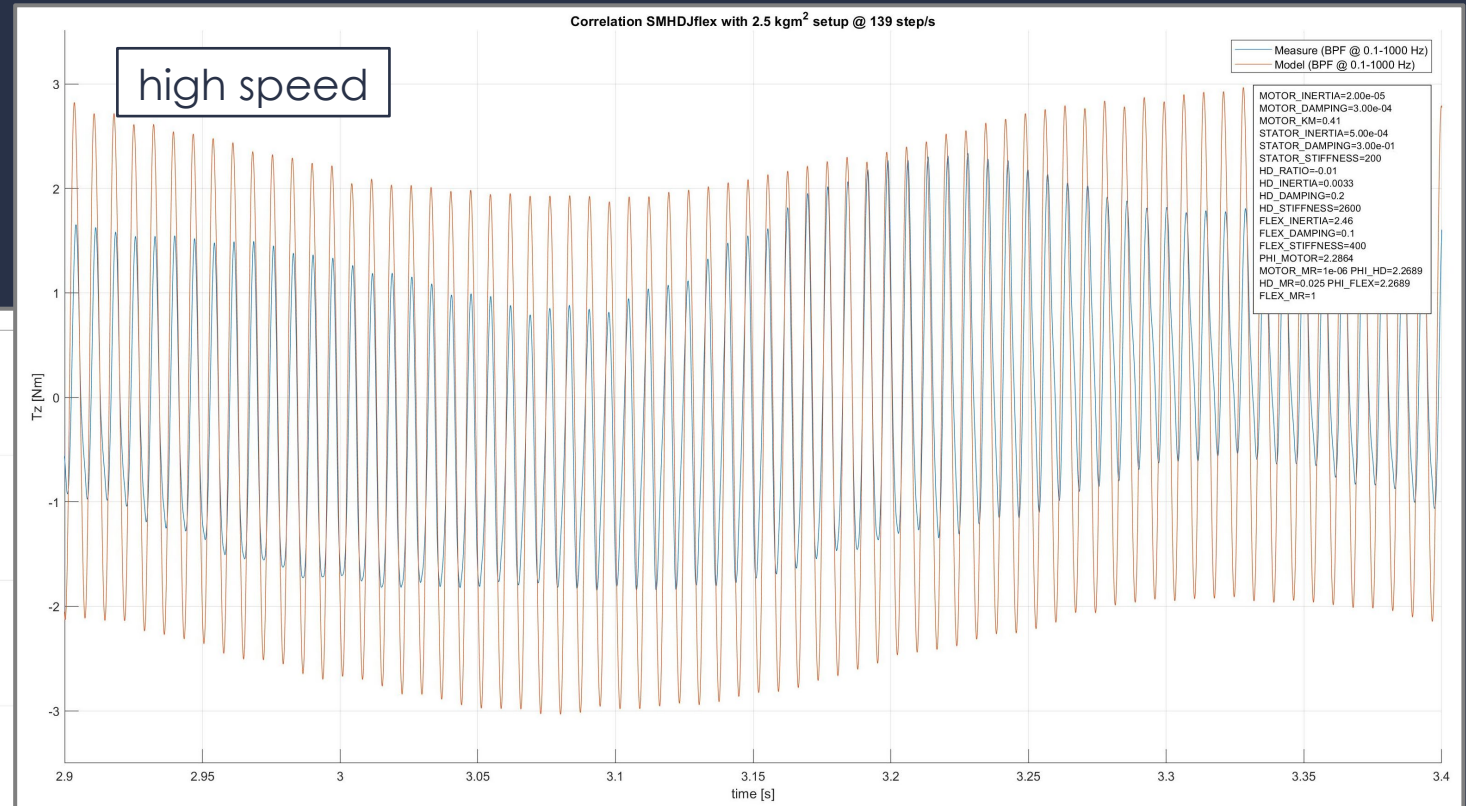
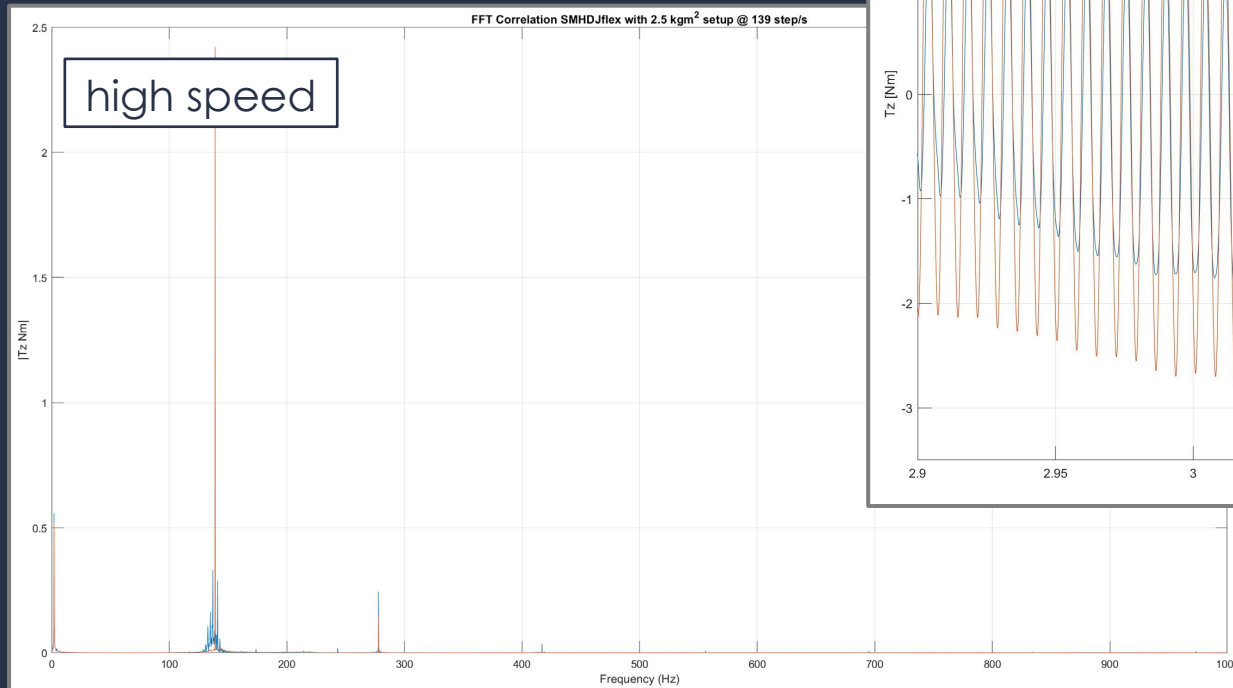
# Correlation:

primary torque  $T_z$  (test bench #3) →

FULL SYSTEM:

- with harmonic drive
- with load (large)

- Measurement in **blue**
- Model in **orange**



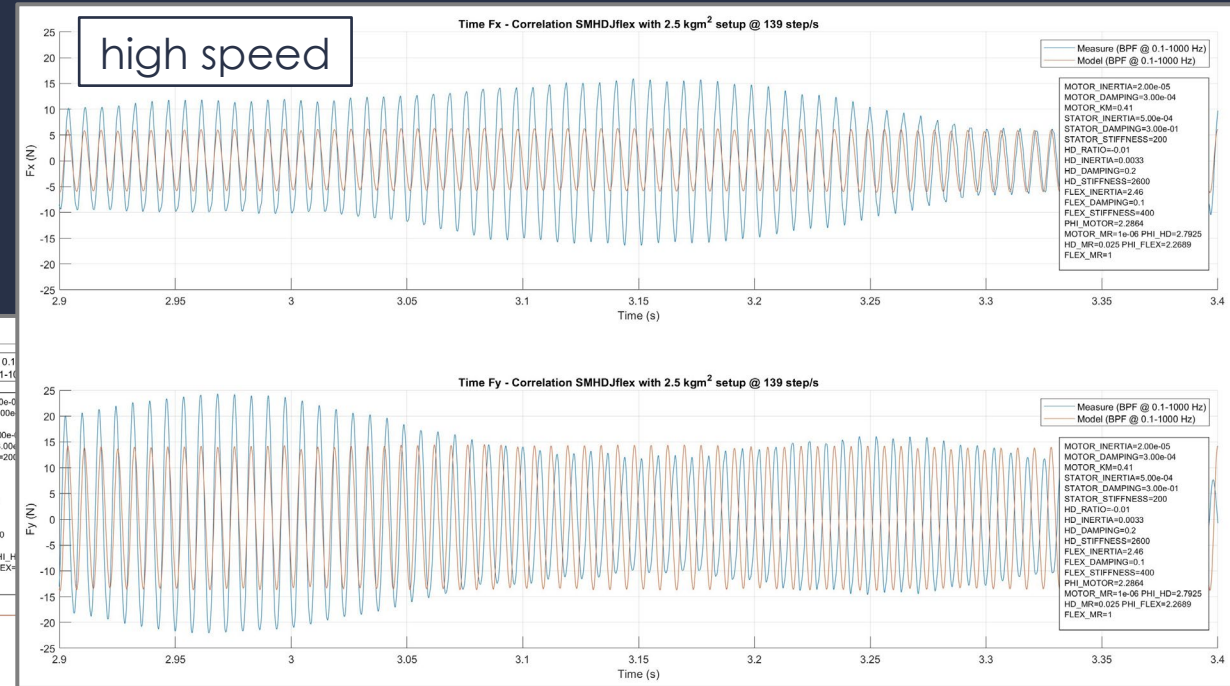
## Correlation:

lateral forces  $F_x$  &  $F_y$  (test bench #3) →

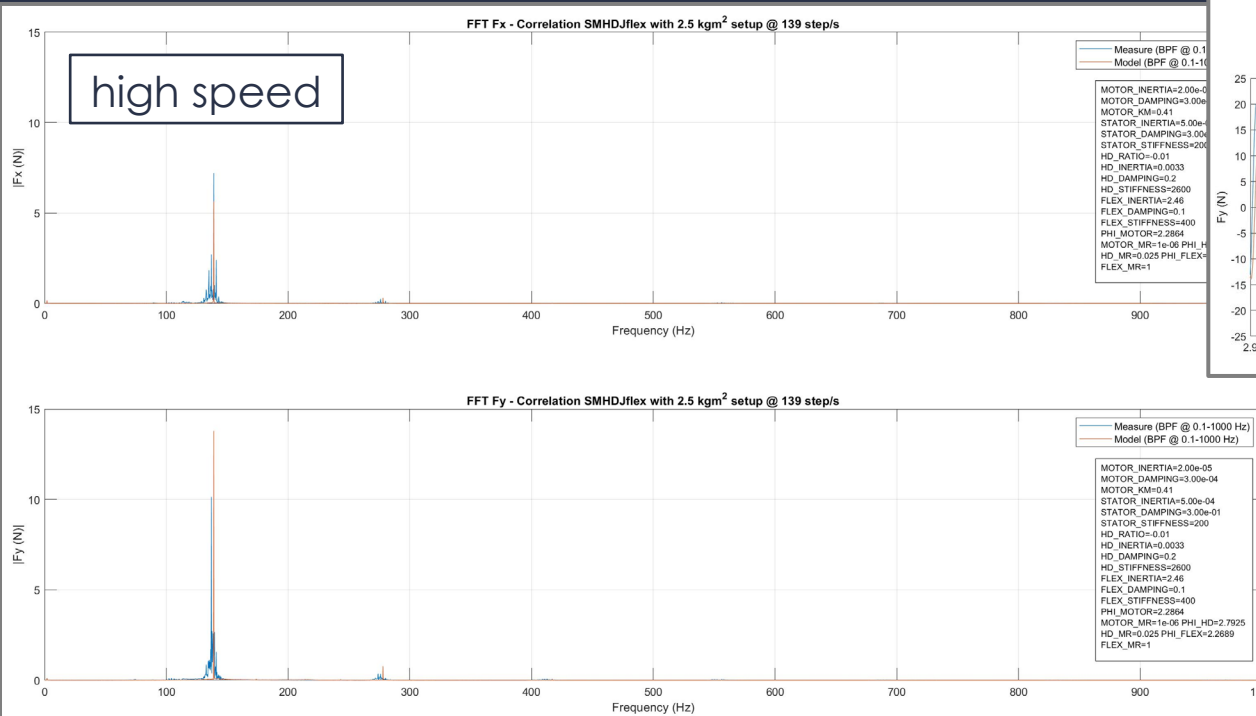
FULL SYSTEM:

- with harmonic drive
- with load (large)

- Measurement in **blue**
- Model in **orange**



28



# Summary of Correlation Results

	Low speeds (<10 step/s)		High speeds (>60 step/s)	
	Torque	Forces	Torque	Forces
Test Bench #1 (only SM)	Good	OK	Good	OK
Test Bench #2 (SM+HD+J <sub>small</sub> )	Good	OK	OK	Unsatisfactory
Test Bench #3 (SM+HD+J <sub>large</sub> )	Good	OK	OK	Unsatisfactory

- Torque correlation generally good, degrading with increasing speed and system complexity
- Force correlation generally OK degrading with increasing speed and system complexity



## Conclusion & lessons learnt 1/2

- Extensive test campaign has been carried out to better understand sources of microvibration from stepper motor + harmonic drive + inertia system, whose dynamics are akin to those of a SADM
- Detailed development of multi-DoF Simulink model to predict exported microvibrations, specifically primary torque  $T_z$  and lateral forces  $F_x$  &  $F_y$
- Correlation of model to measurements has been challenging, with error in results generally growing with increasing system complexity and step rate
- Seemingly simple system much more complex beneath the surface

## Stepper motor Conclusion 2/2

- In the frame of micro vibration predictions, the key element is to be able to simulate acceleration and displacement of sensitive elements like telescope.
- **Globally the results match the overall tendency, but details are not captured**
- Results are generally better along Z axis
  - The structure of the telescope and the iridium case are "simpler" in the Z direction, meaning less poles and more accurate FEM explaining the slightly better prediction.
- Results show that uncorrelated FEM (not in the scope of the activity) gives only a first valid idea of micro vibration prediction with resonance frequencies most of the time off by more than 100 Hz.
- **The general idea seems promising but shall be restricted to simpler structure where a FEM correlation can be performed or used only for rough estimates.**

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# Prediction in the time domain

- Task : to develop a methodology to reduce considered structure FEM model
  - Use of the CBN method of NASTRAN, subcontract to Almatech
- There is two different foreseen strategies (see Perez, J. A et al. "Flexible Multibody System Linear Modeling for Control Using Component Modes Synthesis and Double-Port Approach ", 2016):

## All in one model

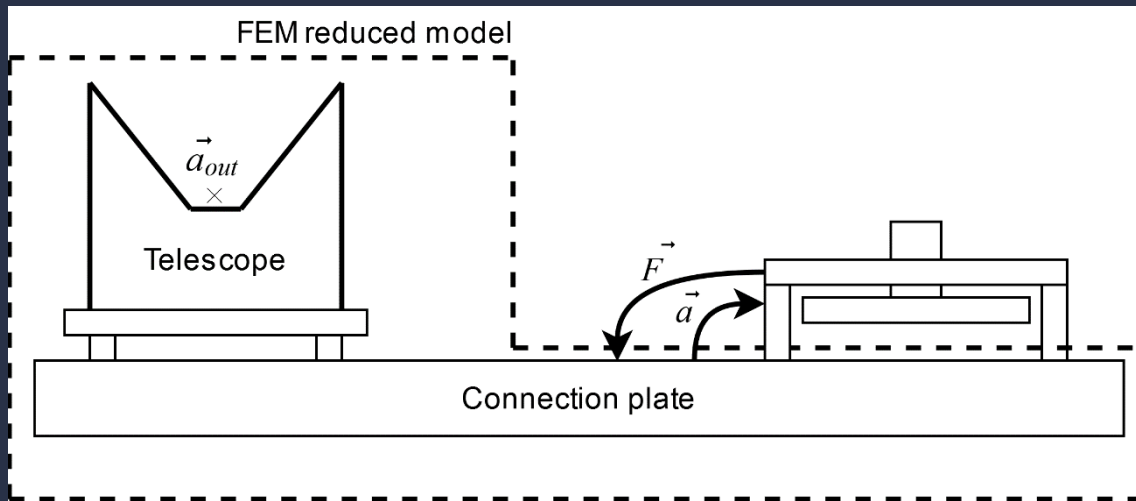
- Adding the connection plate to the telescope FEM, then performing modal reduction.
- Attachment (fixed boundary) point is the stepper and cryo cooler interfaces
- Inputs are forces
- Output point is the telescope mirror
- The output is acceleration

## Dual part model

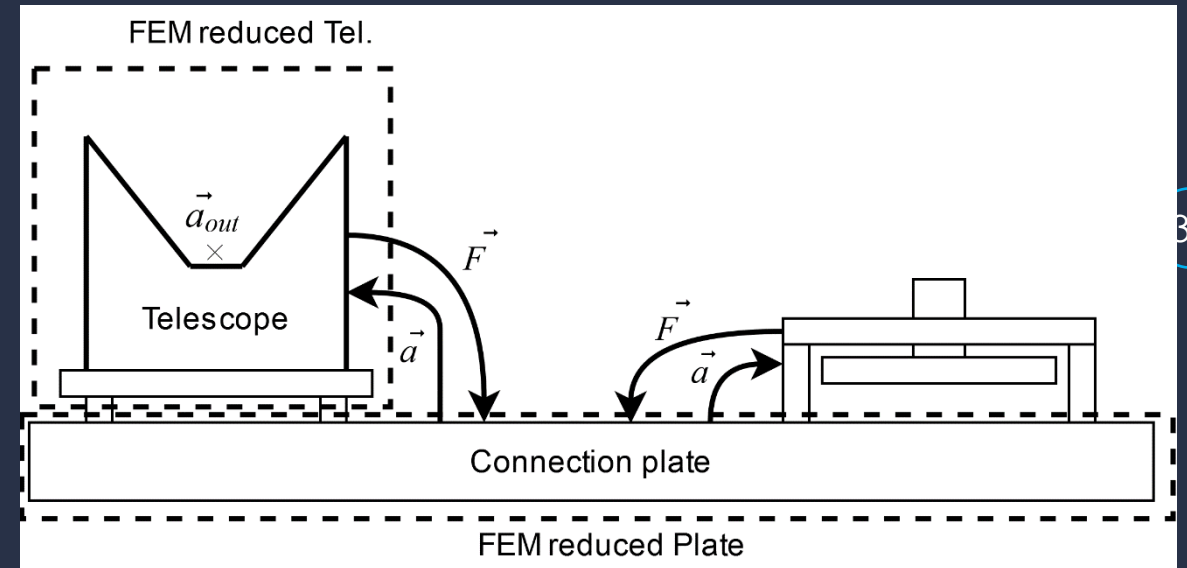
- Allows concatenating multiple elements.
- Telescope FEM is reduced alone with its defined attachments (fixed boundary). Input is acceleration at attach points, output is forces at attachment point and acceleration at mirror.
- The plate is reduced. Input is forces at attach (fixed boundary) points of stepper motor, cryo cooler and telescope, output is acceleration at attachment points.
- Full model is obtaining by connecting related I/O

# Prediction in the time domain

- All in one model



- Dual part model



## Prediction in the time domain– from FEM to state-space

- From reduced model:

$$\underbrace{\begin{bmatrix} I_{n \times n} & M_{qa} & M_{qb} \\ M_{aq} & M_{aa} & M_{ab} \\ M_{bq} & M_{ba} & M_{bb} \end{bmatrix}}_M \cdot \begin{bmatrix} \ddot{q} \\ \ddot{a} \\ \ddot{b} \end{bmatrix} + \underbrace{\begin{bmatrix} \omega^2 & 0 & 0 \\ 0 & K_{aa} & K_{ab} \\ 0 & K_{ba} & K_{bb} \end{bmatrix}}_K \cdot \begin{bmatrix} q \\ a \\ b \end{bmatrix} + \underbrace{\begin{bmatrix} 2\xi\omega & D_{qa} & D_{qb} \\ D_{aq} & D_{aa} & D_{ab} \\ D_{bq} & D_{ba} & D_{bb} \end{bmatrix}}_{KD} \cdot \begin{bmatrix} \dot{q} \\ \dot{a} \\ \dot{b} \end{bmatrix} = \begin{bmatrix} 0 \\ F_a \\ F_b \end{bmatrix}$$

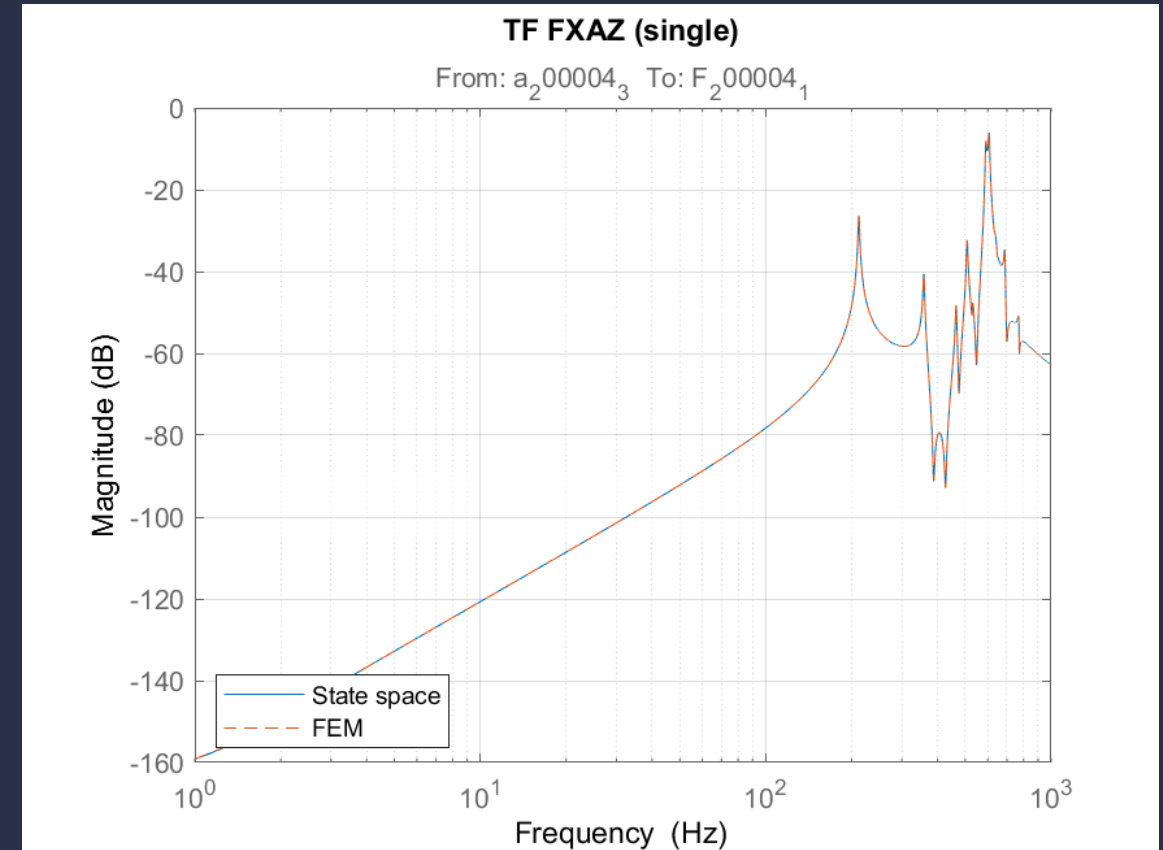
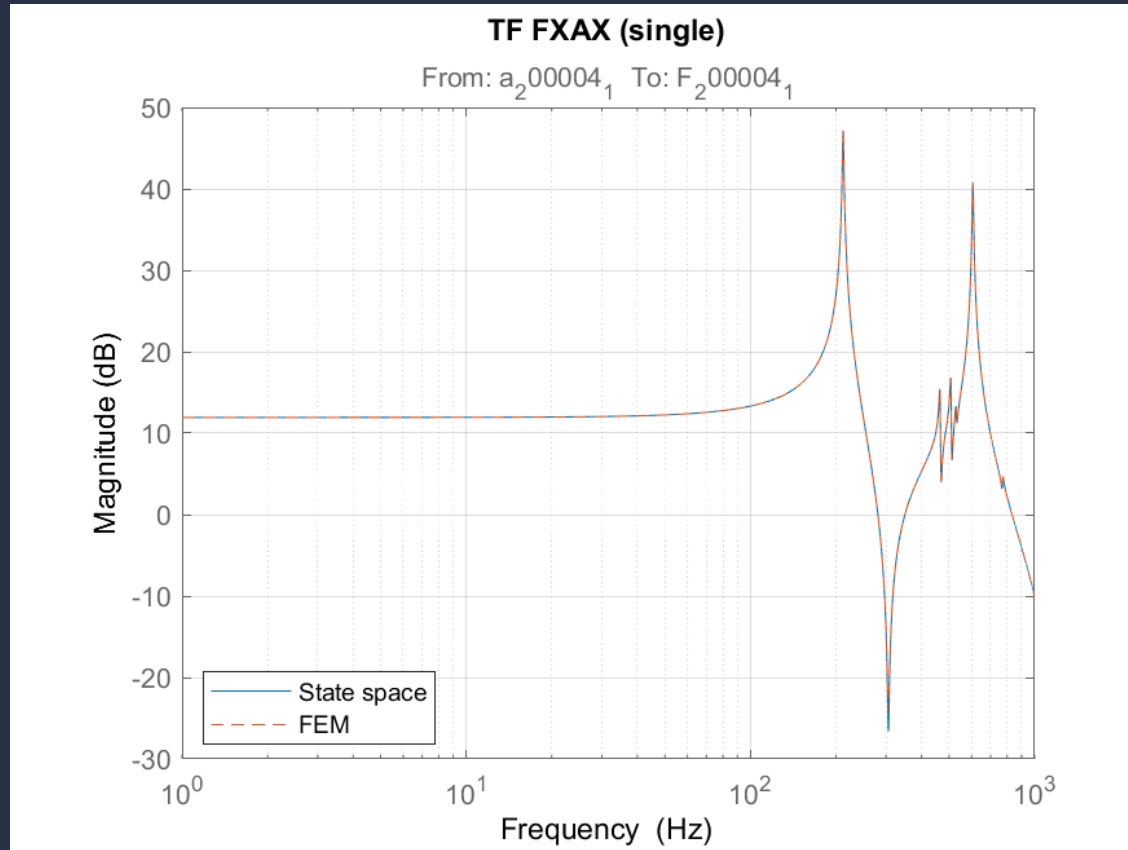
- A state space is derived . Methodolgy summarized in TN3.2. 3 options studied
  - Single point – input acceleration at pt a, output forces at pt a
  - Dual port model Substructure connected to 2 structures via 1 connection point each
  - Fixed free
- To check the state space model, transfer function are compared with transfer function obtained from the full FEM model.
- The eigenvalues of the obtained state space A matrix shall be negative.



# Time domain prediction method approach

## Single point model forces

From feet acceleration to feet exported forces



## Prediction in the time domain– from FEM to state-space (PM16)

- To Implement the effect of the source (stepper and cryo cooler), two terms are needed the forces & torques from the model and a set of forces and torques due to the imported acceleration ( $F$  is used as a vector of forces and torques):
  - $F = F_{model} + F_{acc}(a)$
  - If modeling ran into problems it is also possible to directly use measurements
  - $F = F_{meas} + F_{acc}(a)$
  - As no specific modeling of  $F_{acc}(a)$  is foreseen, the following model is used:

$$F_{acc}(a) = \begin{bmatrix} 1 & 0 & 0 & 0 & ao_z & -ao_y \\ 0 & 1 & 0 & -ao_z & 0 & ao_x \\ 0 & 0 & 1 & ao_y & -ao_x & 0 \end{bmatrix} \cdot \vec{a}$$

with  $\vec{ao}$  being the vector from attachment point to COG of the stepper or cryo cooler.

## Prediction in the time domain damping (PM17)

- Difference between structural and viscous damping

Structural	Viscous
$F_{D \text{ Struct.}} = G \cdot K \cdot \cos(\omega \cdot t)$	$F_{D \text{ Visc.}} = D \cdot \omega \cdot \cos(\omega \cdot t)$

- Usually FEM states damping as structural damping as (i stands for imaginary part):

$$\begin{bmatrix} \dot{a} \\ \ddot{a} \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ \frac{-K(1+iG)}{M} & 0 \end{bmatrix} \begin{bmatrix} a \\ \dot{a} \end{bmatrix} + \begin{bmatrix} 0 \\ \frac{F_a}{M} \end{bmatrix}$$

- $M \cdot \ddot{x} = -K(1 + i \cdot G) \cdot x + F$

- With this formulation it leads to a state space of the form:

Whose eigenvalues are:

- $s_1 = -a + ib$

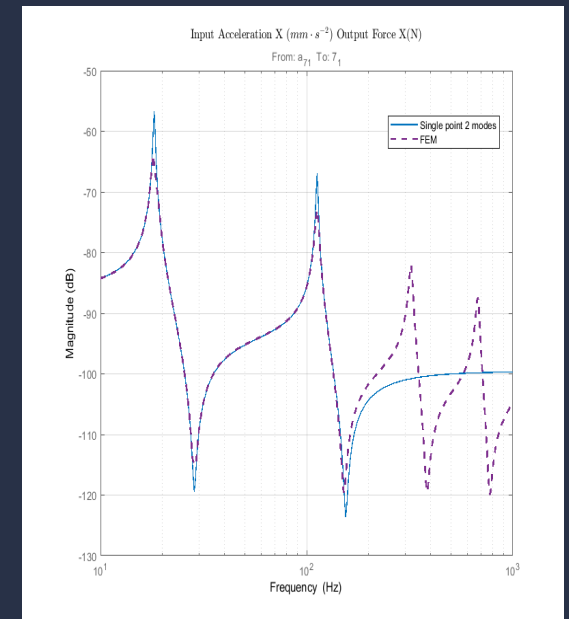
- $s_2 = a - ib$

## Prediction in the time domain damping

- As one of the eigen values has a positive real part, the time domain response is unbounded
- A solution is needed
  - If the damping matrix is diagonal ie with a single point reduced Newton:

$$\underbrace{\begin{bmatrix} E_{n \times n} & M_{qa} \\ M_{aq} & M_{aa} \end{bmatrix}}_M \cdot \begin{bmatrix} \ddot{q} \\ \ddot{a} \end{bmatrix} + \underbrace{\begin{bmatrix} \omega^2 & 0 \\ 0 & 0 \end{bmatrix}}_K \cdot \begin{bmatrix} q \\ a \end{bmatrix} + \underbrace{\begin{bmatrix} G\omega^2 & 0 \\ 0 & 0 \end{bmatrix}}_D \begin{bmatrix} \dot{q} \\ \dot{a} \end{bmatrix} = \begin{bmatrix} 0 \\ F_a \end{bmatrix}$$

- D matrix is replaced by:  $\underbrace{\begin{bmatrix} G \cdot \omega & 0 \\ 0 & 0 \end{bmatrix}}_D$  for viscous damping



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## Improve

- Final test:
  - Main goal, validate the whole chain:
    - (Source model) replaced by shaker
    - Propagation model
    - Telescope model
- 3 step experiment consisting of:
  - Structure Only, iridium case
  - Structure + sensitive load (iridium case + DSS)
  - Structure + sensitive load (iridium case + DSS) with several perturbation sources in parallel
    - Mounting two shakers one at stepper location the other @ cryo location
    - A sum of sinuses was be injected on each shaker

## Simplified testing techniques

- Literature search has been performed on testing techniques
  - Almost everybody uses rigid mounting of setup on Kistler table
  - Whole setup being decoupled from ground through heavy marble and pneumatic dampers
  - There is one facility at Estec that uses active decoupling
    - Rising performance in the low frequency range
  - For more realistic reconstruction of exported forces a suspended test configuration is able to recover the dynamic mass contribution
    - Dynamic mass improve the computation of exported forces when couples to a structure.

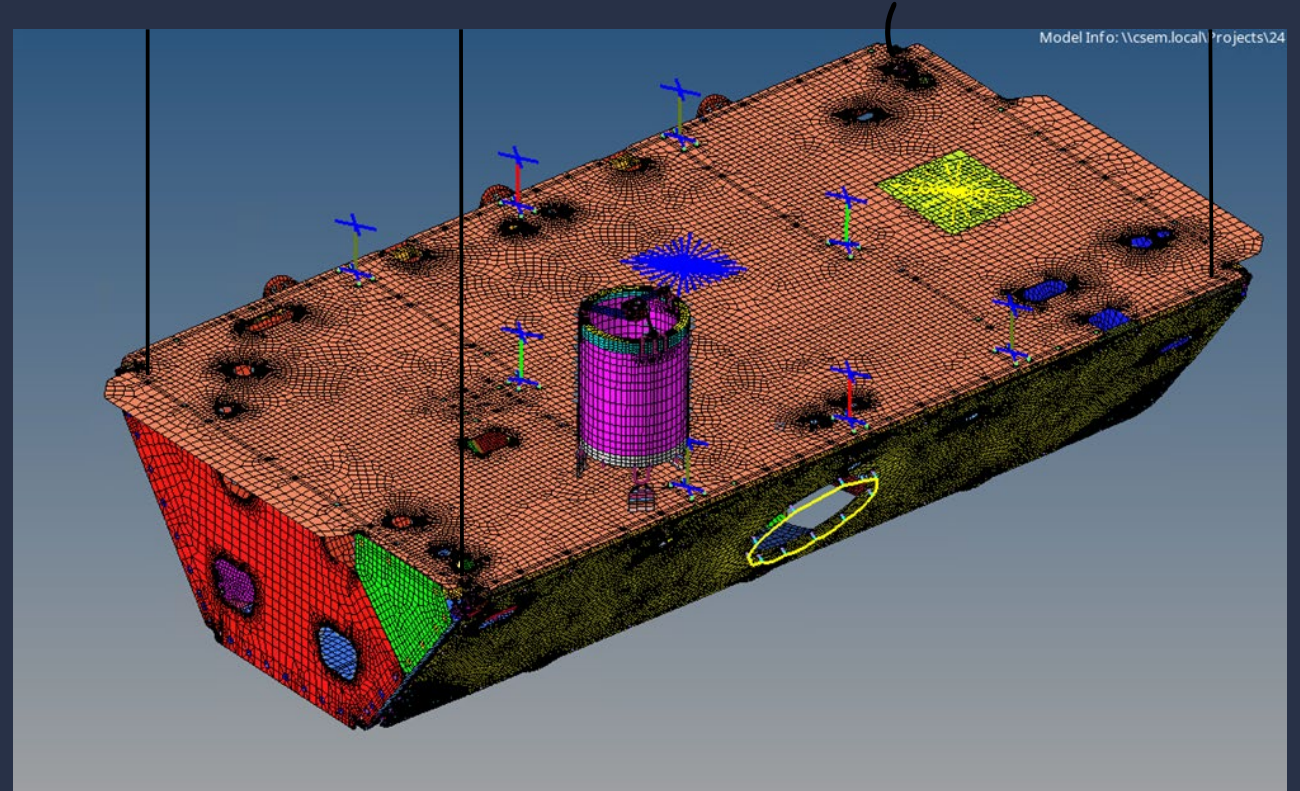


## Example of instrumentation

- Structure + DSS tests
  - Mounting a known perturbation source on stepper and cryo cooler location. (shaker)
  - Mounting force sensor between shaker and structure (TBC)
  - Mounting accelerometer @ Telescope primary and secondary mirrors
  - Measuring transfer function from source to telescope primary and secondary mirrors
    - Compare it with FEM reduced model
    - Transfer function measured will be from X,Y,Z to X,Y,Z (9 TF)
    - Transfer function involving rotation and torques won't be measured

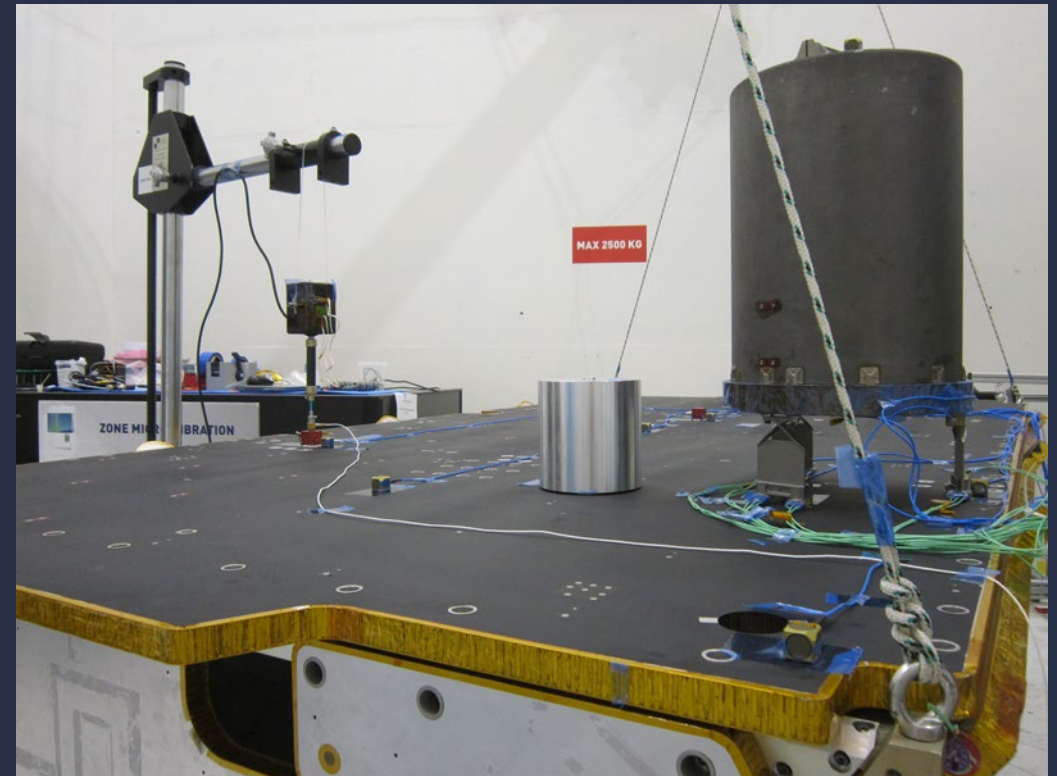
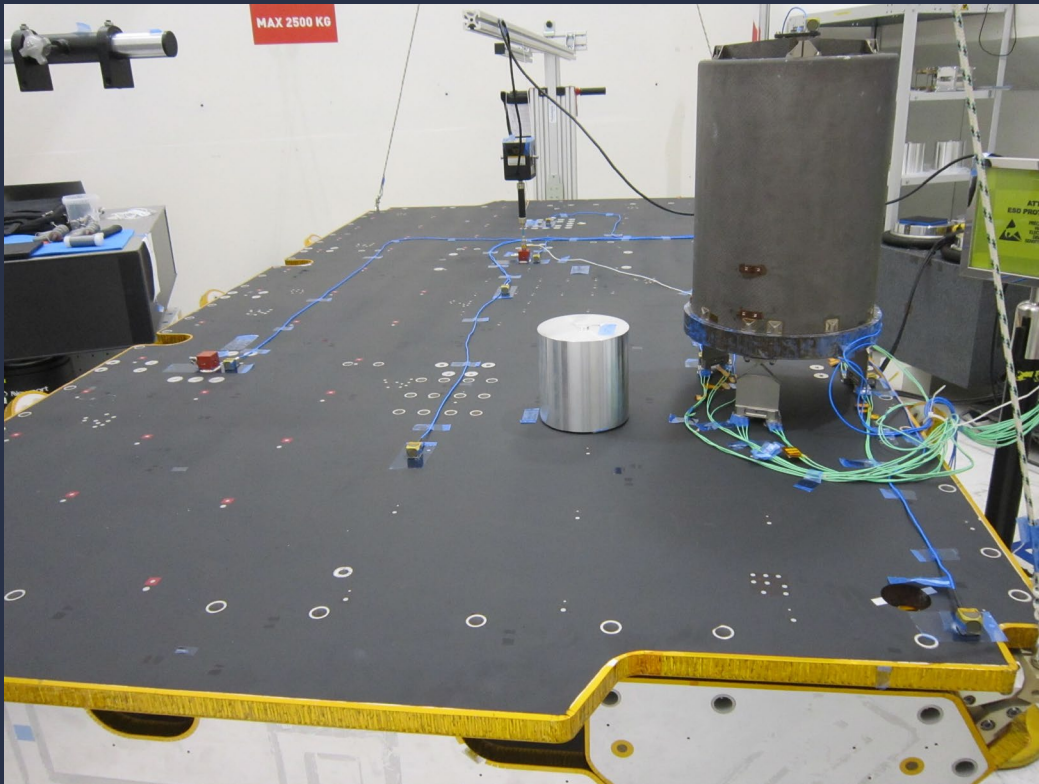
## Setup

- Iridium case suspended on hoisting lines to recreate a free free behaviour
- Acquisition system:
  - Accelerometers PCB 356
  - Force sensors Kistler
  - LMS acquisition platform



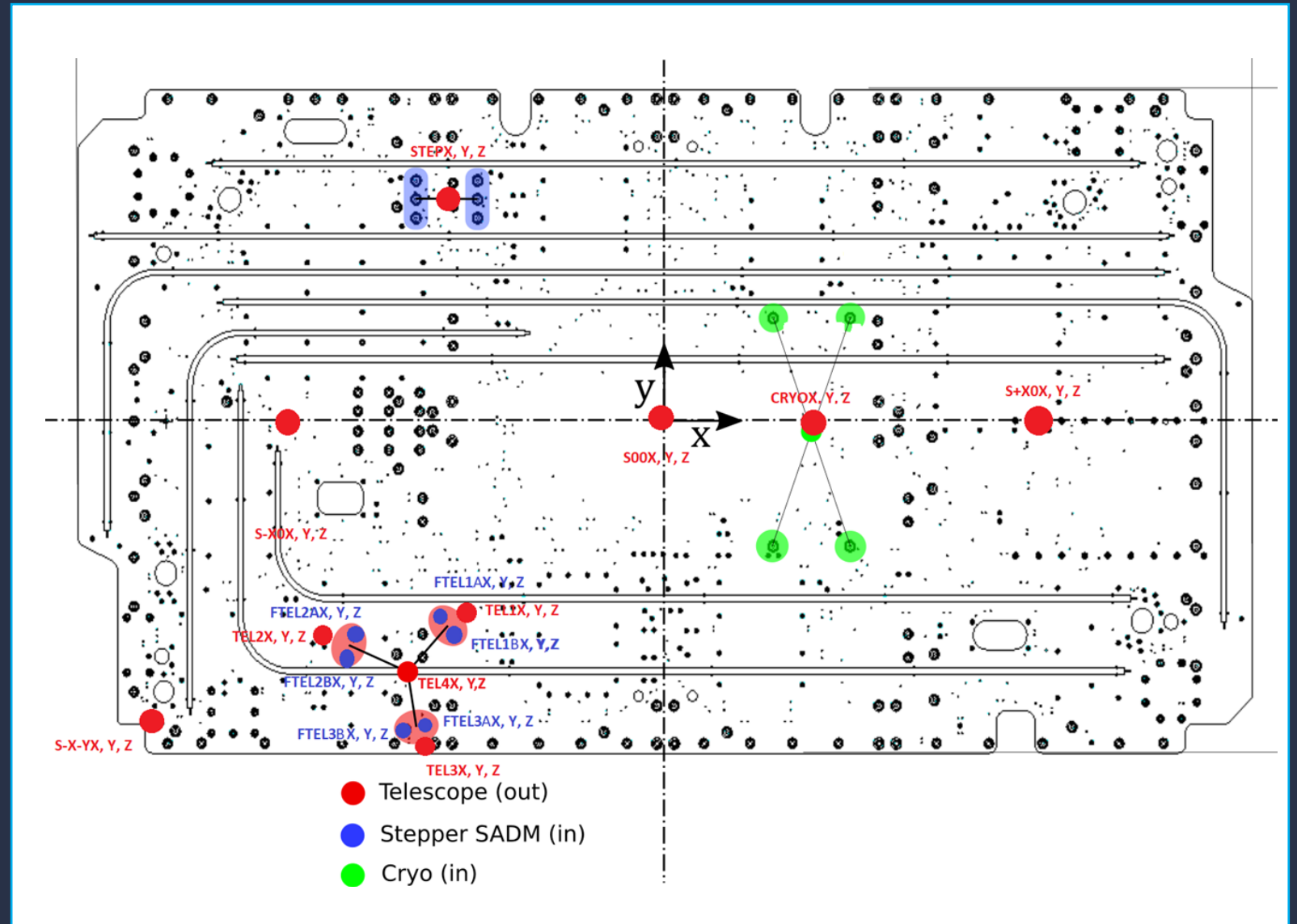
# Final tests Setup

- Final tests



# Accelerometers locations

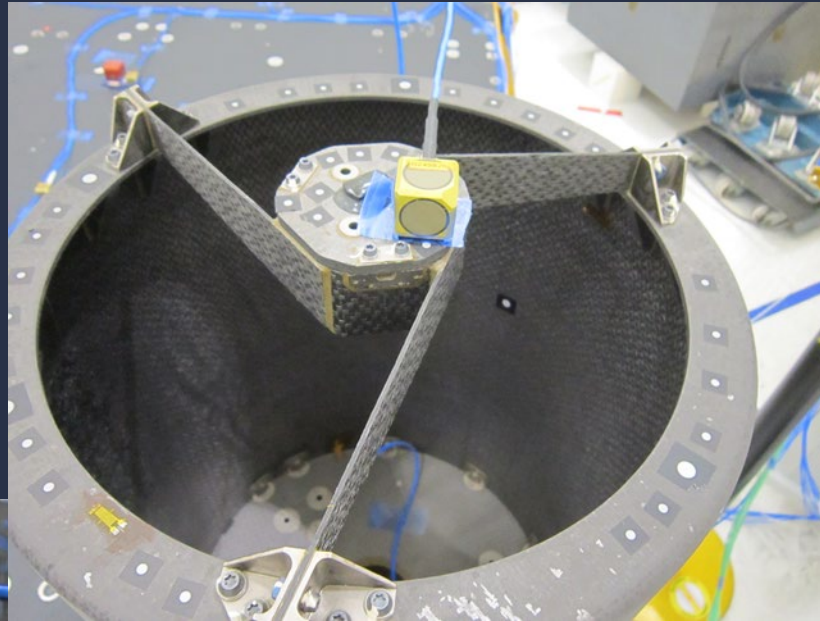
- Blue = Stepper (SADM)
- Green = cryocooler
- Red = DSS
- Telescope mounted with force sensor at interface with top panel



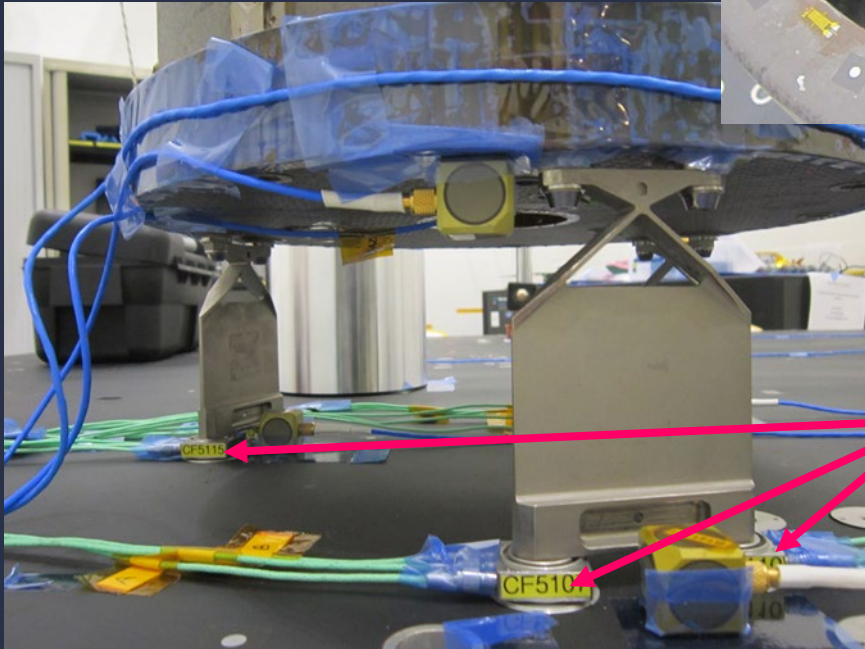


# Accelerometers location telescope details

TEL4

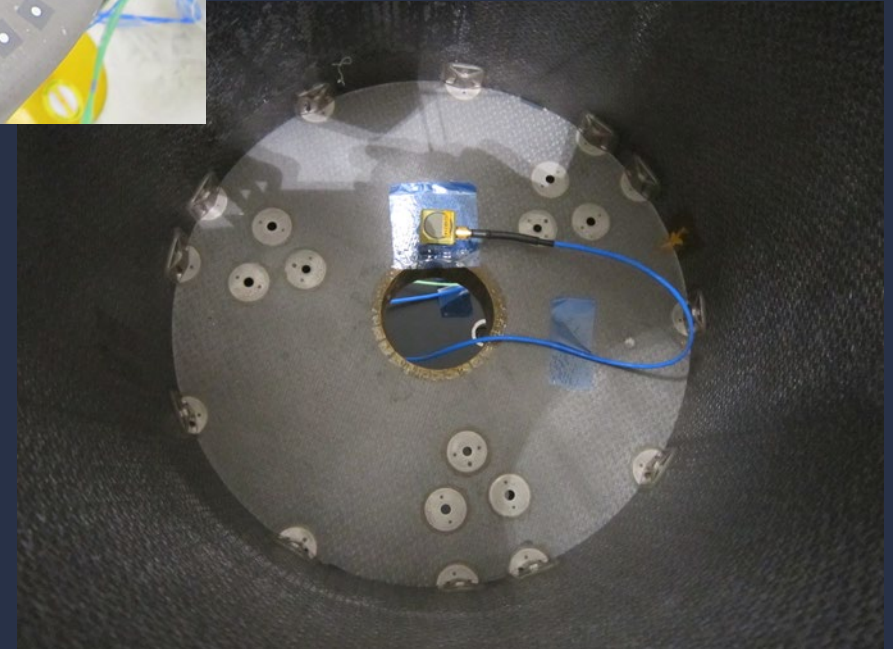


TEL6



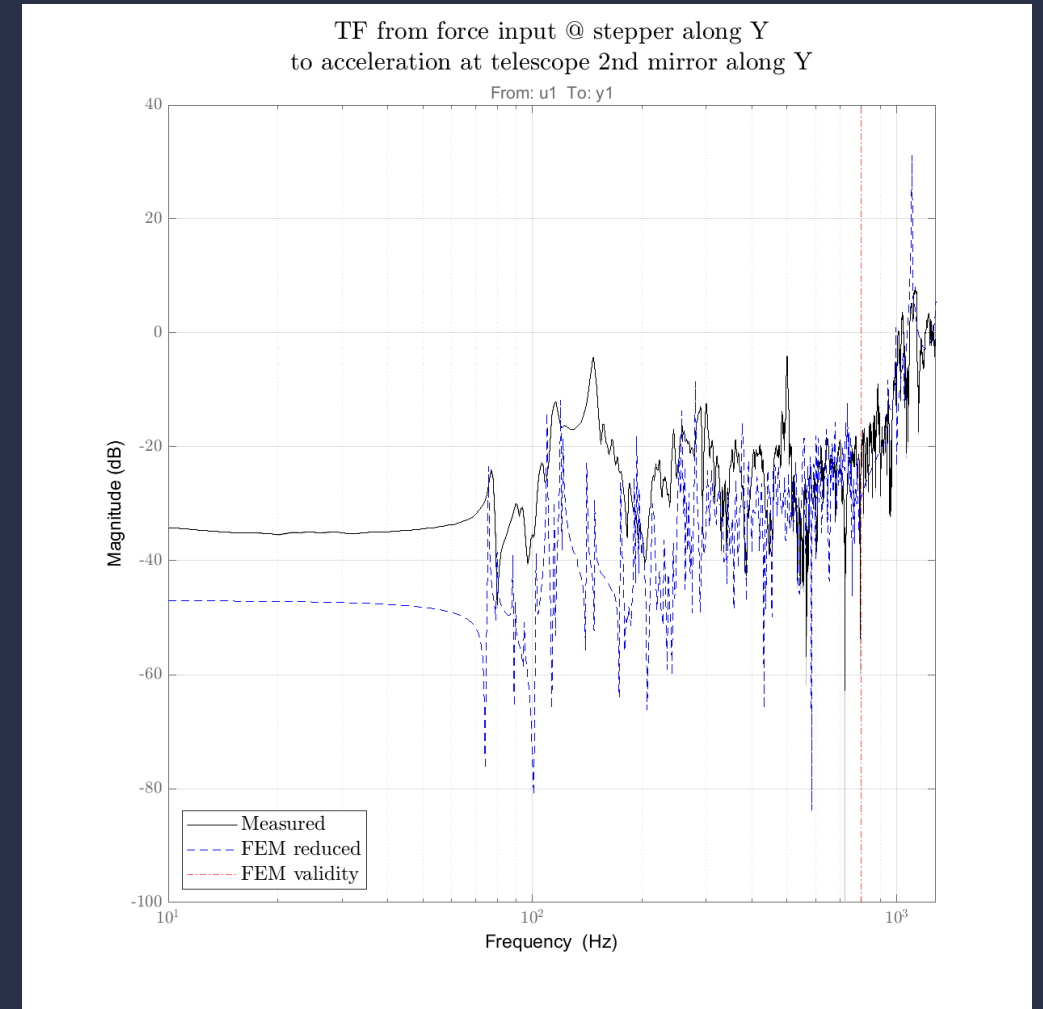
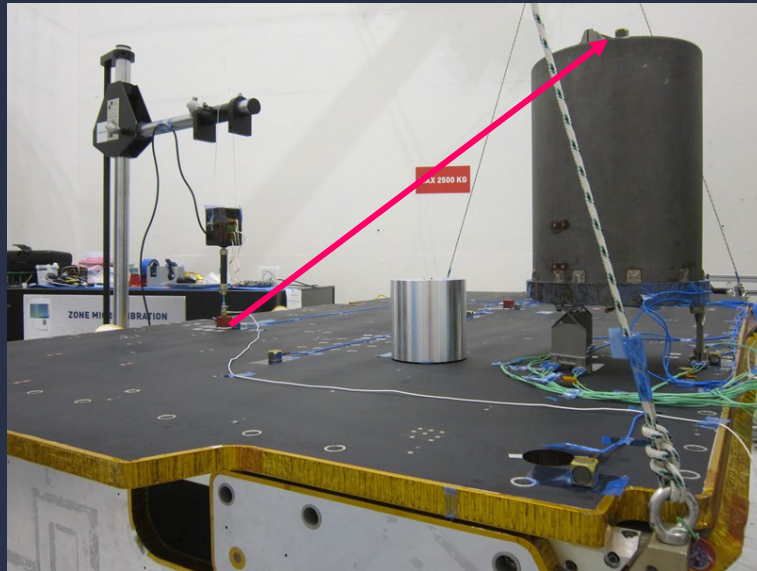
6\*Force sensors

TEL5



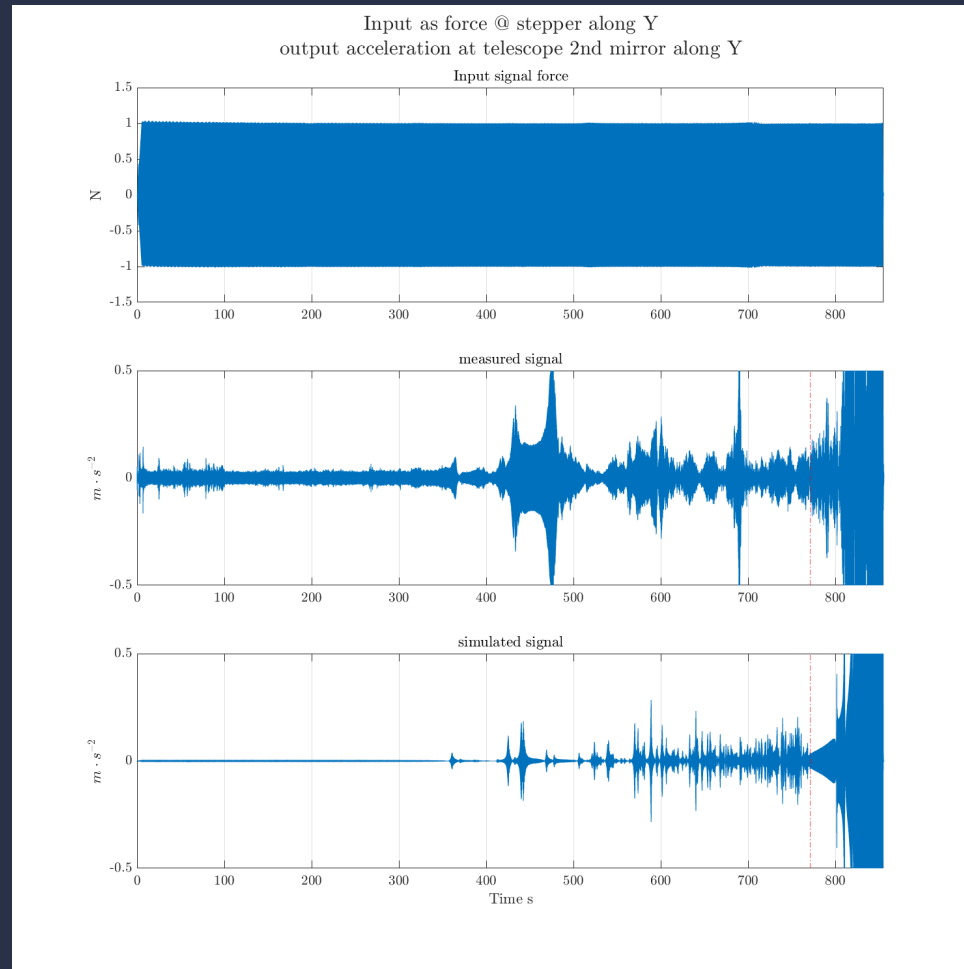
## Example: Structure + DSS

- From force at stepper location to acceleration at telescope 2nd mirror along Y
- Axis Y



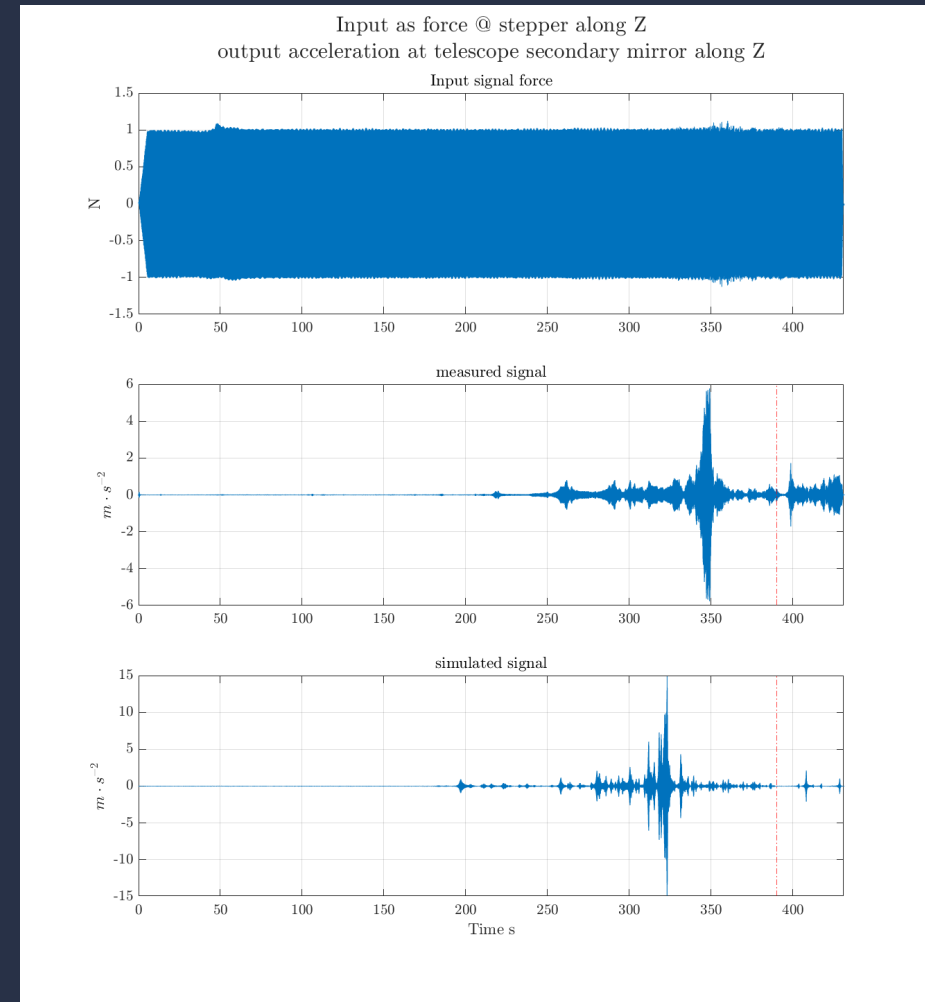
# Example: Temporal domain with structure + DSS

- From stepper force to 2<sup>nd</sup> ary mirror (input 1 N sinesweep 10 → 1280 Hz)



Measure

Simulation



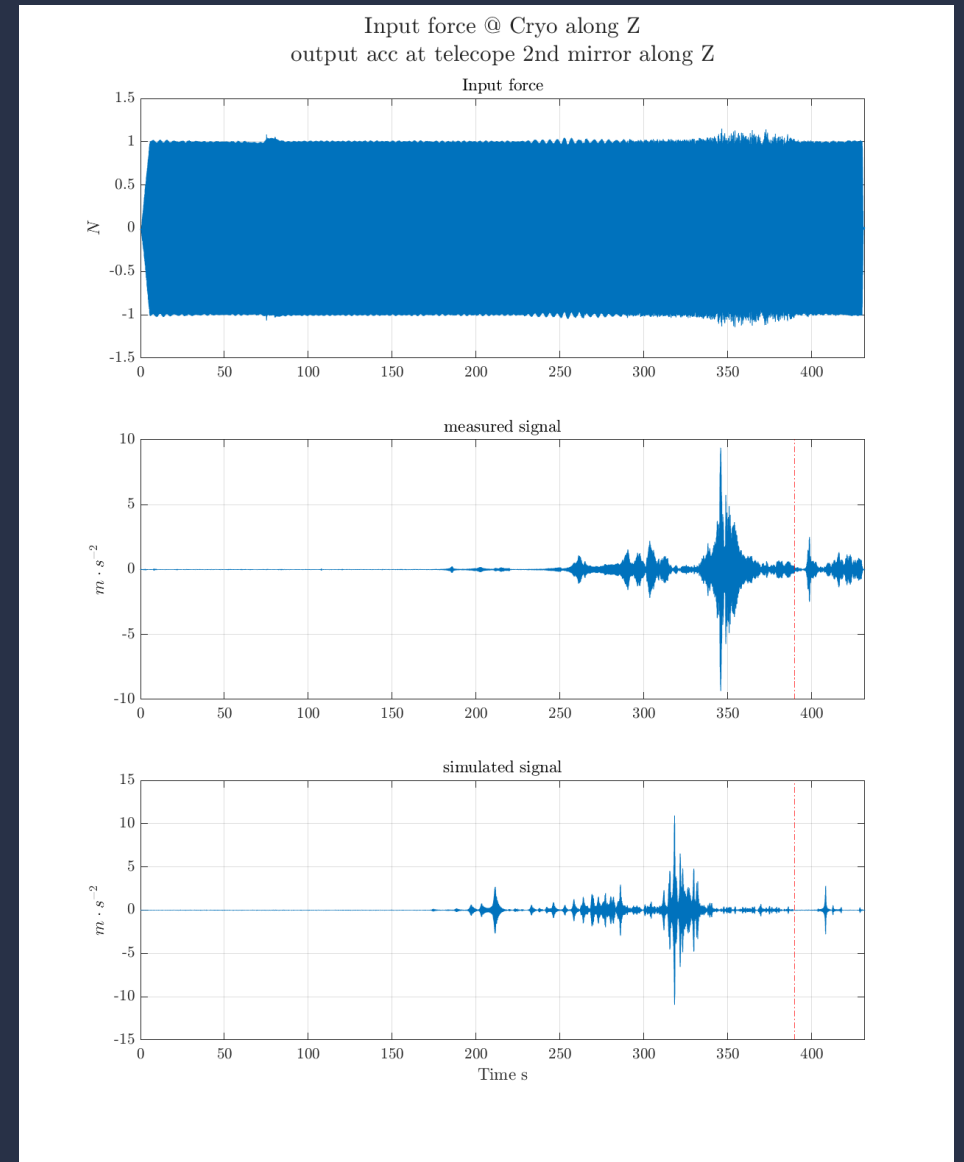


# Temporal domain with DSS (input 1 N sinesweep 10 → 1280 Hz)

- From Cryo force to 2<sup>nd</sup> ary mirror
- Z axis

Measure

Simulation



# Agenda

Project introduction, structure and organization – CSEM

Stepper motor modelling and correlation – CSEM

Cryo cooler motor modelling and correlation – TAS

Time domain summation methodology – CSEM

Frequency domain summation methodology– TAS

Test results - CSEM / TAS

Conclusions

# Conclusion

- In the frame of micro vibration predictions, the key element is to be able to simulate acceleration and displacement of sensitive elements like telescope.
- **Globally the results match the overall tendency, but details are not captured**
- Results are generally better along Z axis
  - The structure of the telescope and the iridium case are “simpler” in the Z direction, meaning less poles and more accurate FEM explaining the slightly better prediction.
- Results show that uncorrelated FEM (not in the scope of the activity) gives only a first valid idea of micro vibration prediction with resonance frequencies most of the time off by more than 100 Hz.
- **The general idea seems promising but shall be restricted to simpler structure where a FEM correlation can be performed or used only for rough estimates.**

Thank you for your attention!

