

# Shared aperture reflector antenna

Final Presentation  
7<sup>th</sup> November 2013  
ESTEC



UNIVERSITÀ  
DI SIENA  
1240



**TICRA**

# Shared Aperture Project Overview



Prime contractor: TICRA, Copenhagen

Sub-Contractor: The University of Siena

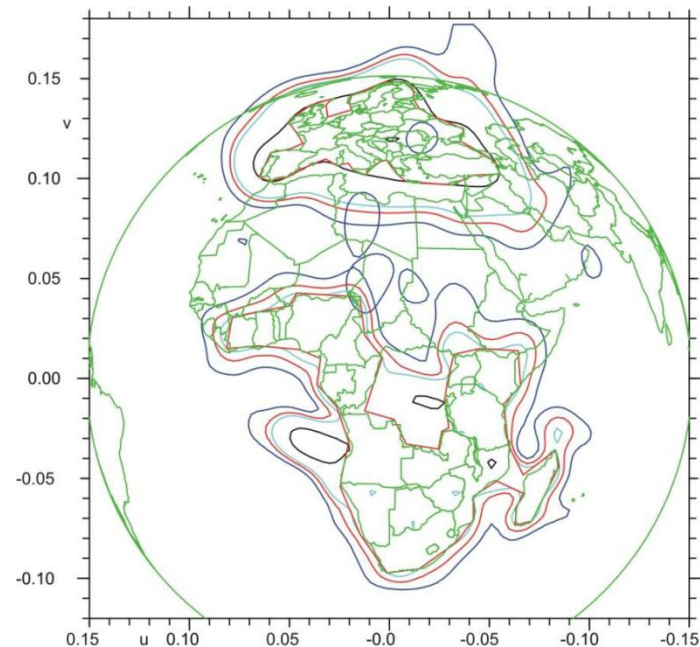
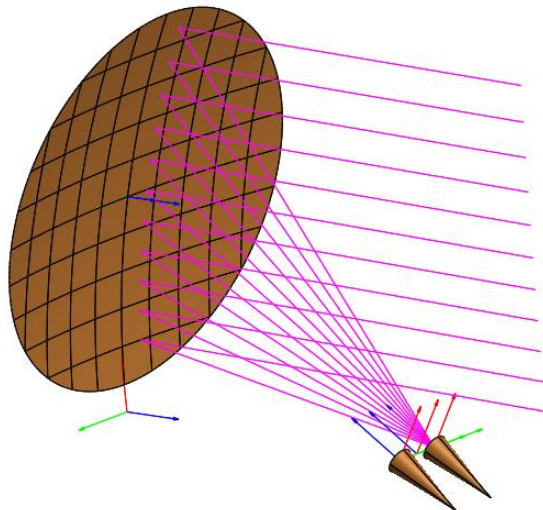
Project duration: 12 months

# Project Goal

Generate more than one contoured beam from a single aperture.

Reduce loss compared to traditional shaped reflectors.

Combine surface shaping and metasurface materials.



## Traditional shaped reflectors:

Very efficient for one feed and one contoured beam.  
Performance degradation if several beams are optimized.

## Planar reflectarray:

Performance similar to the shaped reflector for one beam.  
Severe degradation for multiple contoured beams.

## Metasurface shaped reflector:

Metasurface: Very small metallic elements ( $\lambda/10$ ) on substrate with high dielectric constant ( $\epsilon=9$ ).  
Continuous equivalent current (J,M) distribution assumed.

More than one contoured beam from one aperture.

One or two frequency bands.

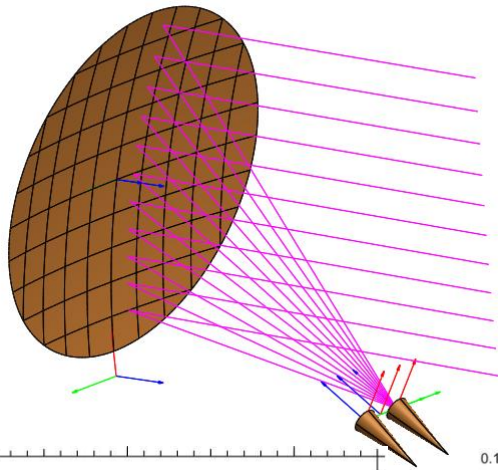
Cx-polar level comparable to shaped metallic reflector.

Loss due to multiple beams  $< 0.5$  dB, compared to separate metallic shaped reflectors.

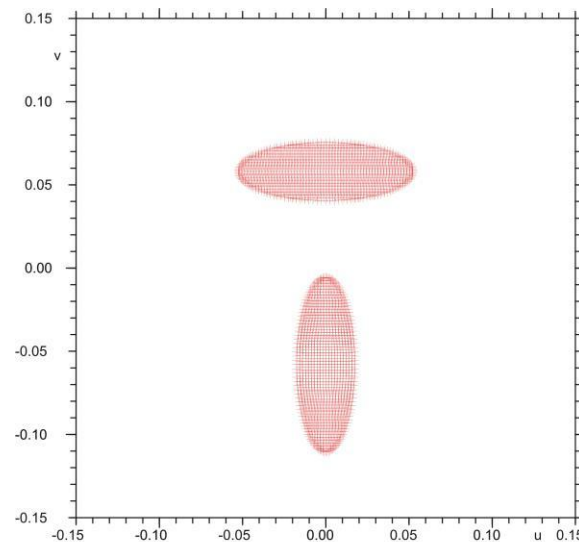
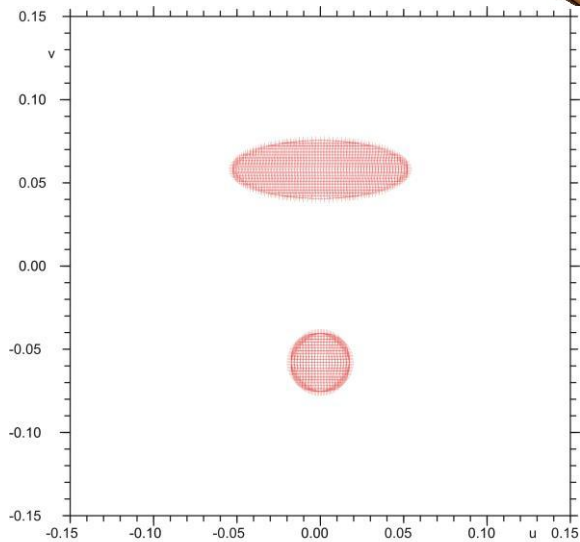
Metasurface material compatible with space environment.

# Benchmark Solution

## Metallic shaped reflector



2 feeds, 2 elliptical coverages.  
Ellipse sizes from  $1^\circ \times 1^\circ$  to  $1^\circ \times 5^\circ$ .  
Scan:  $\pm 3.3^\circ$  and  $\pm 6.6^\circ$   
Frequencies: 10.7 and 14.5 GHz.  
Comparison to two separate reflectors.



# Benchmark Solution

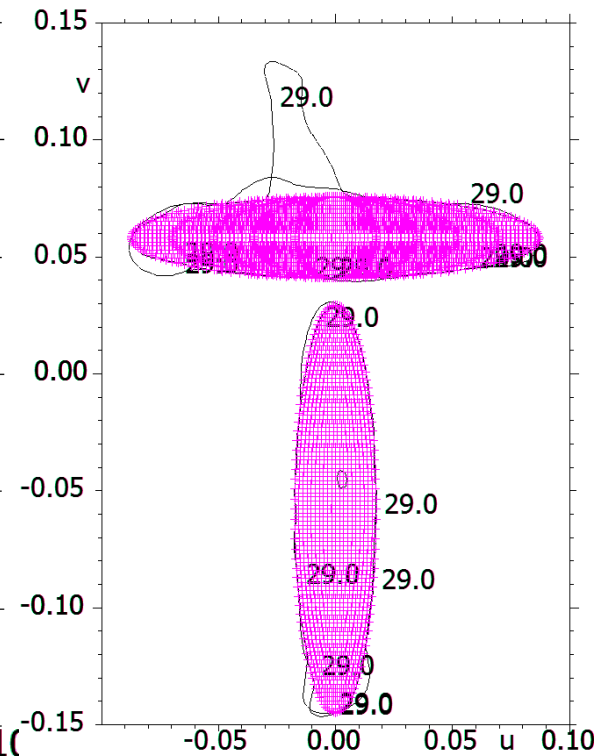
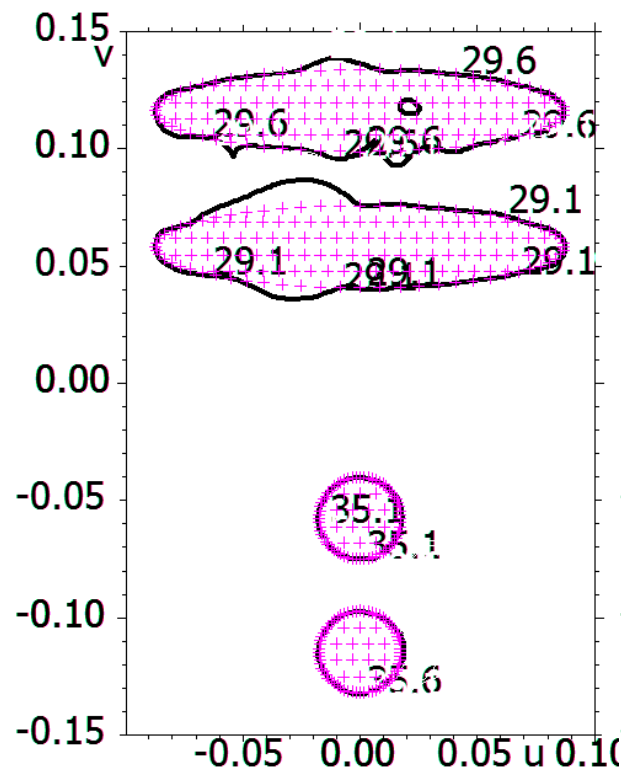
## Metallic shaped reflector



Two beams from one reflector.

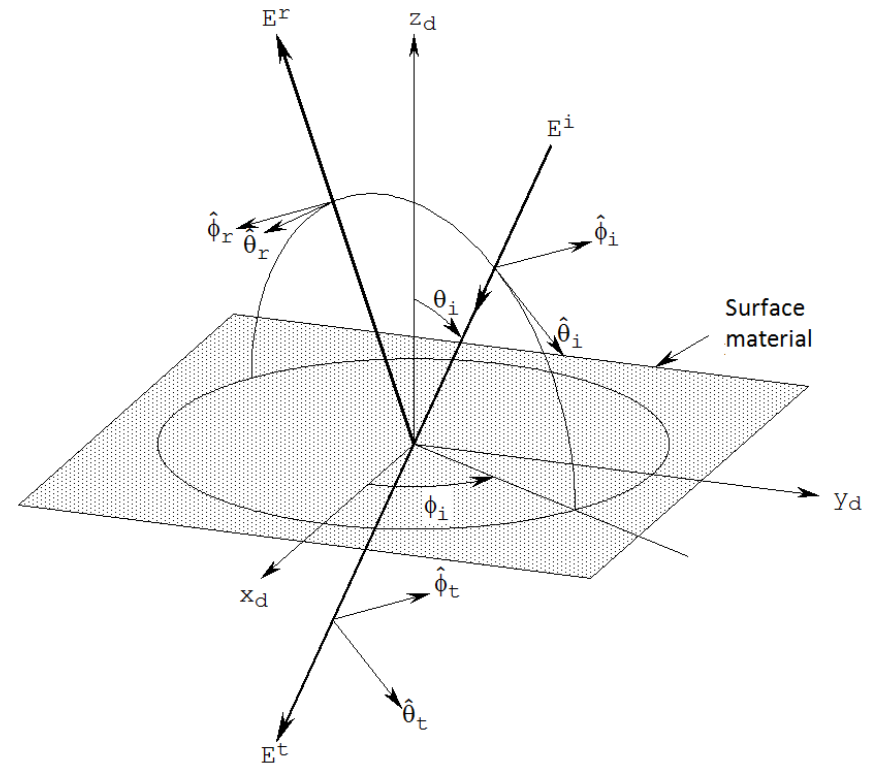
Comparison to two separate metallic reflector.

Penalty varies from 0.4 dB to 1.7 dB in minimum coverage gain.



The S-matrix relates the reflected to the incident field.

$$\begin{pmatrix} E_{\theta}^r \\ E_{\phi}^r \end{pmatrix} = \begin{pmatrix} S_{\theta\theta} & S_{\theta\phi} \\ S_{\phi\theta} & S_{\phi\phi} \end{pmatrix} \begin{pmatrix} E_{\theta}^i \\ E_{\phi}^i \end{pmatrix}$$





# S-Matrix Database



The S-matrix has been tabulated by UNISI as a function of:

Frequency :	10.7 and 14.5 GHz
Patch diameter:	50 values
Slot-length/width:	15 values
$\theta$ -angle:	5 values
$\phi$ -angle:	72 values

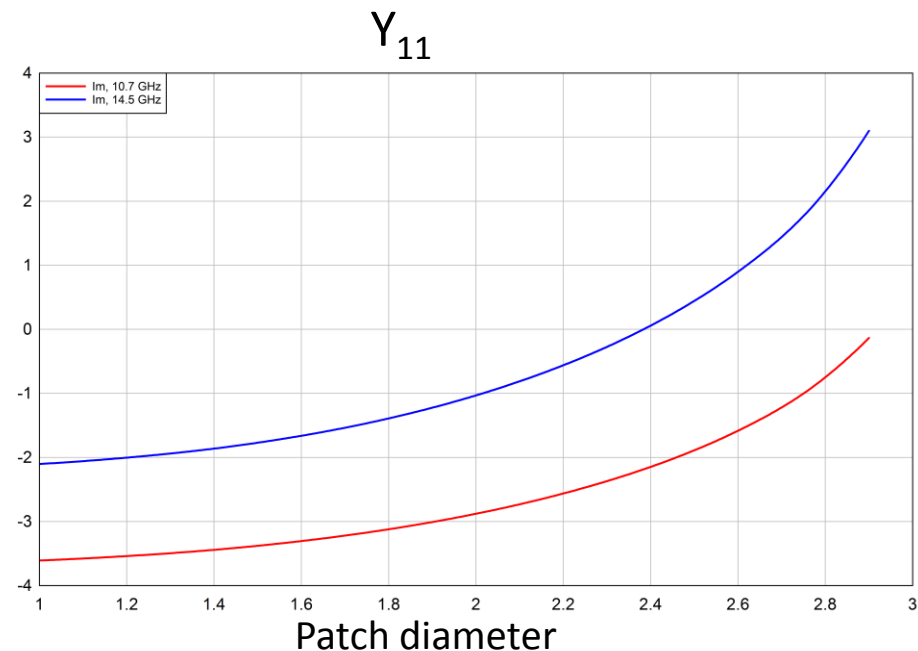
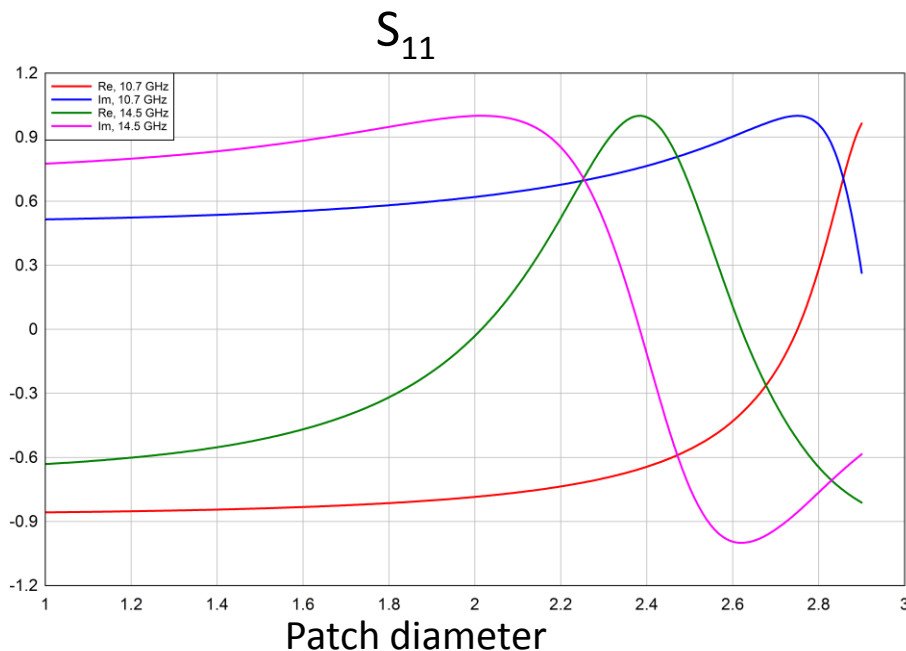
Intermediate values obtained by:

Cubic Lagrange interpolation in geometrical variables and in  $\theta$ .  
Trigonometric interpolation in  $\phi$ .

# S-Matrix Database



Interpolation in Y-matrix (Admittance matrix) much easier than in S-matrix.  
Conversion:  $Y = (U - S)(U + S)^{-1}$  ,  $S = (U - Y)(U + Y)^{-1}$



# S-Matrix Database



The S-matrix is a function of 4 variables:  $\mathbf{S}(a,b,\theta,\phi)$

a: patch diameter

b: slot-length/diameter

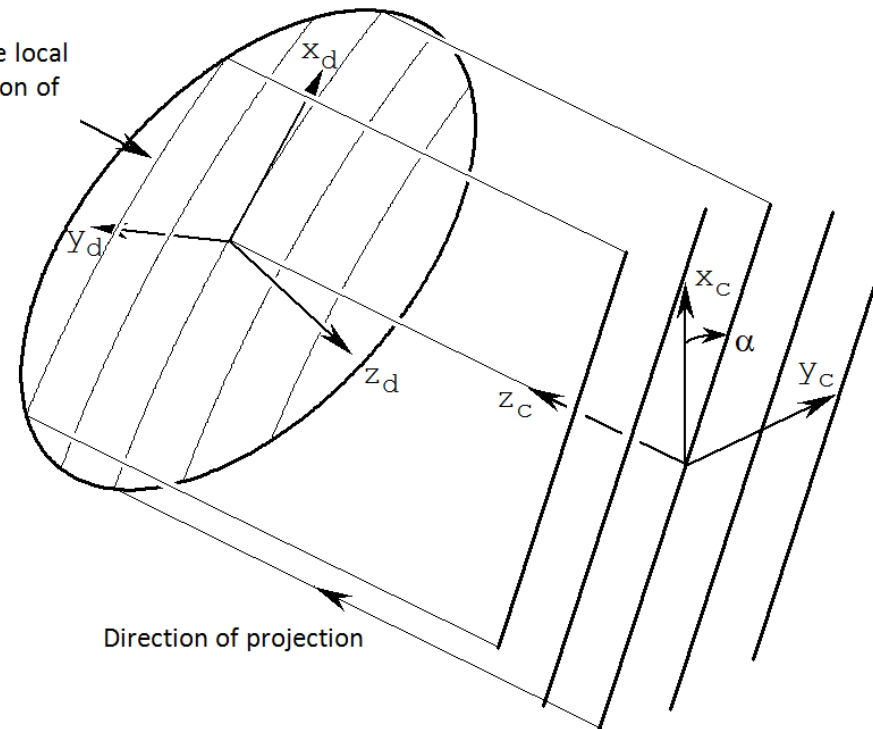
From the Lagrange and trigonometric interpolation derivatives are computed analytically:  $d\mathbf{S}/da$ ,  $d\mathbf{S}/db$ ,  $d\mathbf{S}/d\theta$ ,  $d\mathbf{S}/d\phi$ .

Derivatives needed in optimization.

# Reference direction on curved surface

Patch orientation defined by projection of a set of parallel lines onto the surface

Curves defining the local reference orientation of the S-matrix



# Reflector Currents

## PO approximation



A continuous metasurface distribution is assumed.

Equivalent currents (**J**, **M**) are computed from the S-matrix database.

Standard integration of the currents are performed to obtain the far field.

Fast optimization due to analytic calculation of derivatives of the far field with respect to the metasurface geometrical parameters.

$$d\mathbf{E}_{\text{far-field}}/da, d\mathbf{E}_{\text{far-field}}/db, d\mathbf{E}_{\text{far-field}}/d\theta, d\mathbf{E}_{\text{far-field}}/d\phi$$

Analytic derivatives with respect to surface shape variables is standard in the POS software.

# Optimization Variables



Surface shape spline expansion:  $z(x,y) = \sum_s c_s B_s(x,y)$

Patch size variable:  $a(x,y) = \sum_r d_r B_r(x,y)$

Problems with discontinuities, use instead complex representation.

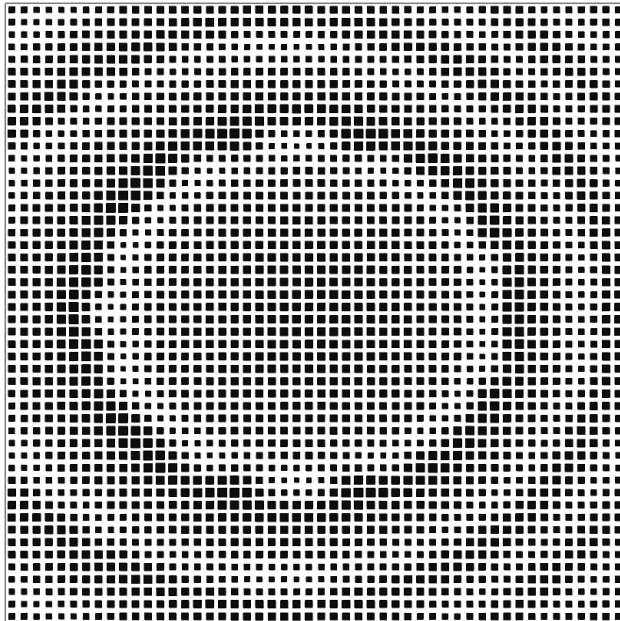
Complex expansion coefficients  $\gamma_r$ :  $F(x,y) = \sum_r \gamma_r B_r(x,y)$

$a(x,y) = \arg(F(x,y)), \quad a(x,y) \in ]-\pi; \pi]$

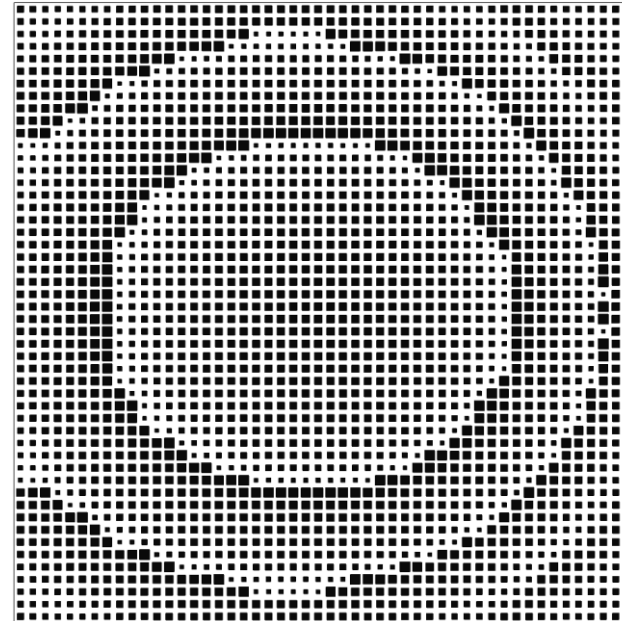
Linear transformation used to bring  $a(x,y)$  into an appropriate interval.

# Optimization Variables

Direct spline expansion  
optimization

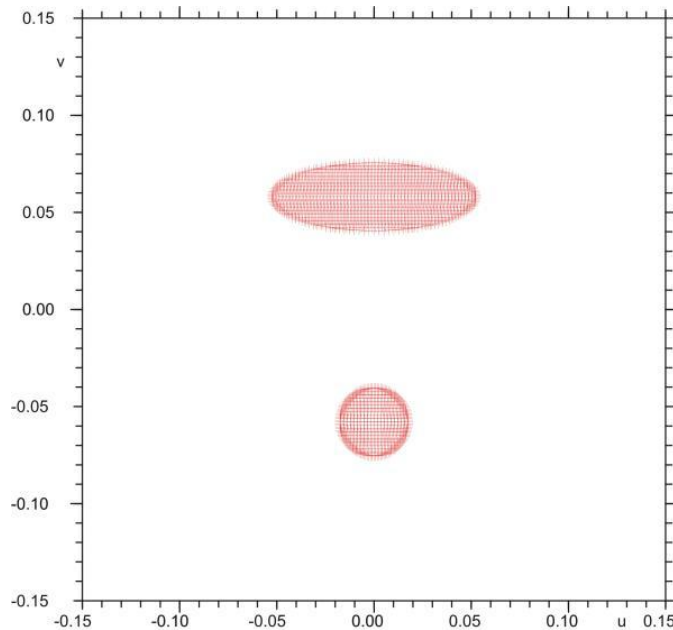


Complex spline expansion  
optimization

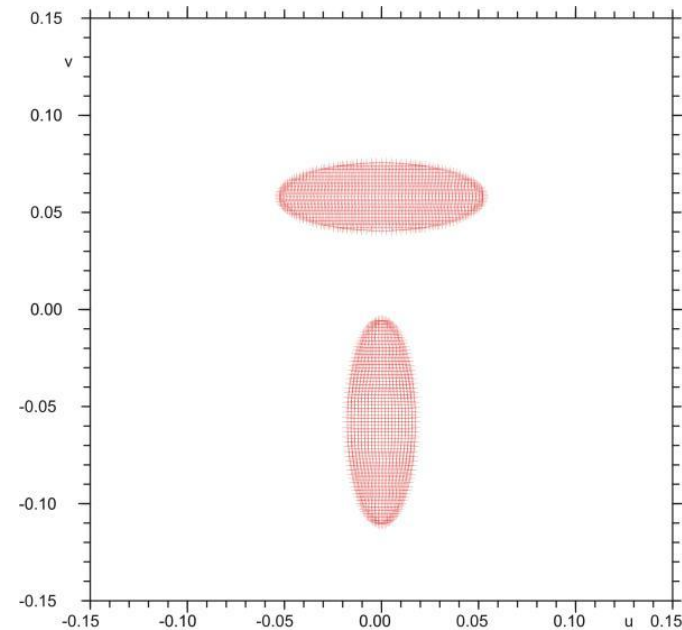


# Combined Metasurface and surface shaping

Comparison with benchmark cases



$1^\circ \times 1^\circ + 1^\circ \times 3^\circ$



$1^\circ \times 3^\circ + 3^\circ \times 1^\circ$



# Combined Metasurface and surface shaping



Penalty of using one shaped reflector instead of two.  
The penalty can be reduced by combining metasurface and surface shaping.

## **One frequency, two beams:**

No improvement. Metasurface and surface shaping provides identical degrees of freedom.

## **Two frequencies, two beams, different frequency for each beam:**

Penalty typically reduced from 1.5 dB to 0.5 dB.

## **Two frequencies, two beams, two frequencies for each beam:**

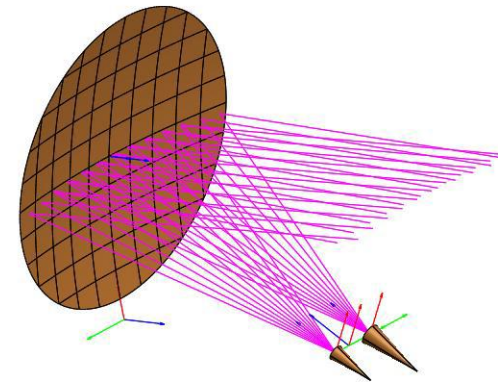
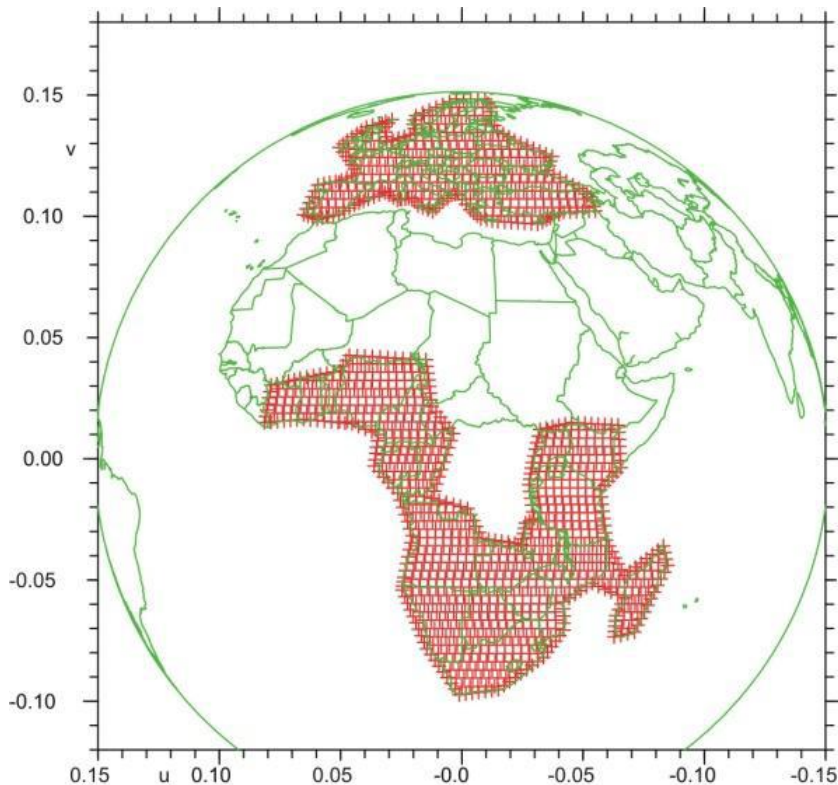
Penalty typically reduced from 2 dB to 1.6 dB.

## **Two frequencies, one beam:**

Penalty typically reduced from 1.5 dB to 0.8 dB.

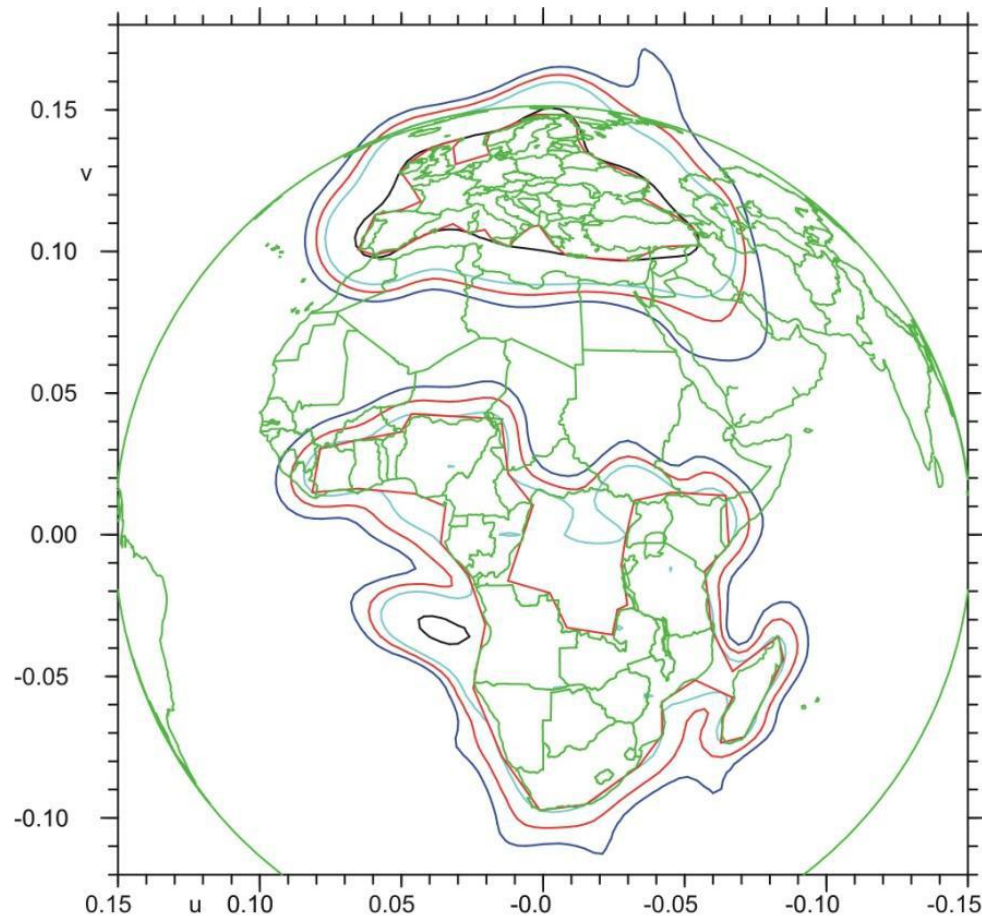
# Applicational example

European and African contoured beam generated by one reflector.



Diameter: 1400 mm  
Focal length: 1400 mm  
10.7 GHz and 14.5 GHz

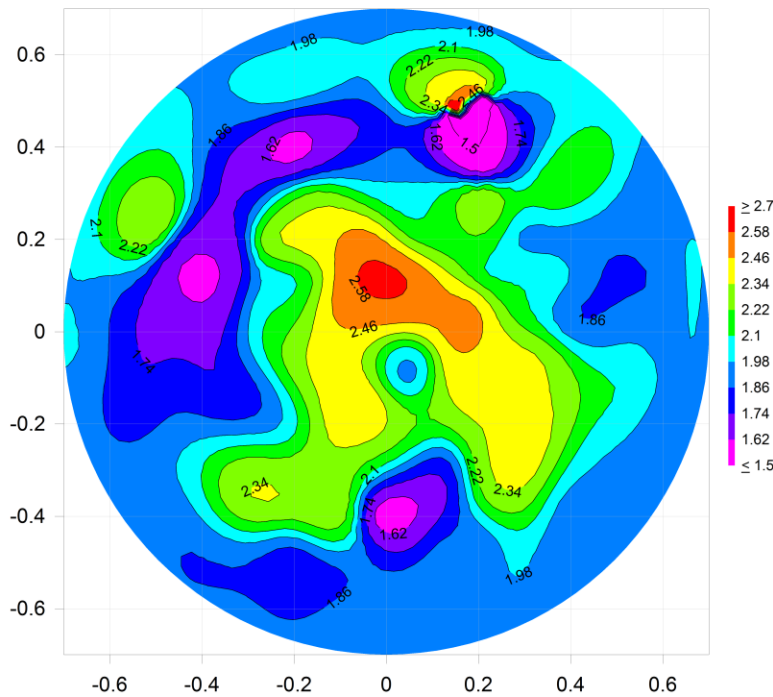
# Applicational example



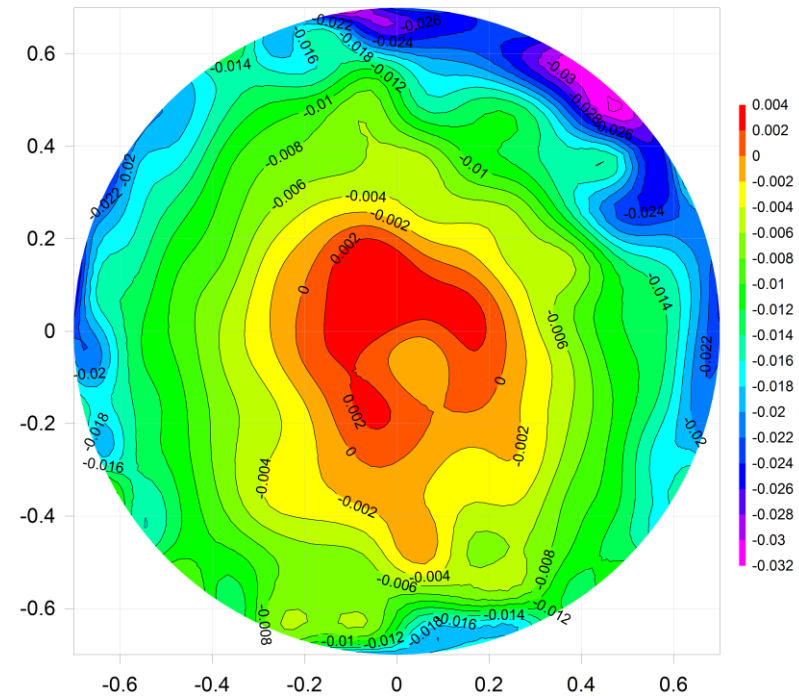
Europe: 14.5 GHz, min. cov.  
directivity 31.09 dBi

Africa: 10.7 GHz, min. cov.  
directivity 27.02 dBi

# Applicational example



Element size distribution  
(mm) on reflector.



Surface shaping (m). Initial  
paraboloid subtracted.

# Result Summary



The metasurface reflector appears to be a natural further development of the shaped reflector.

Penalty of generating two beams from one reflector can be reduced to 0.6-0.7 dB.

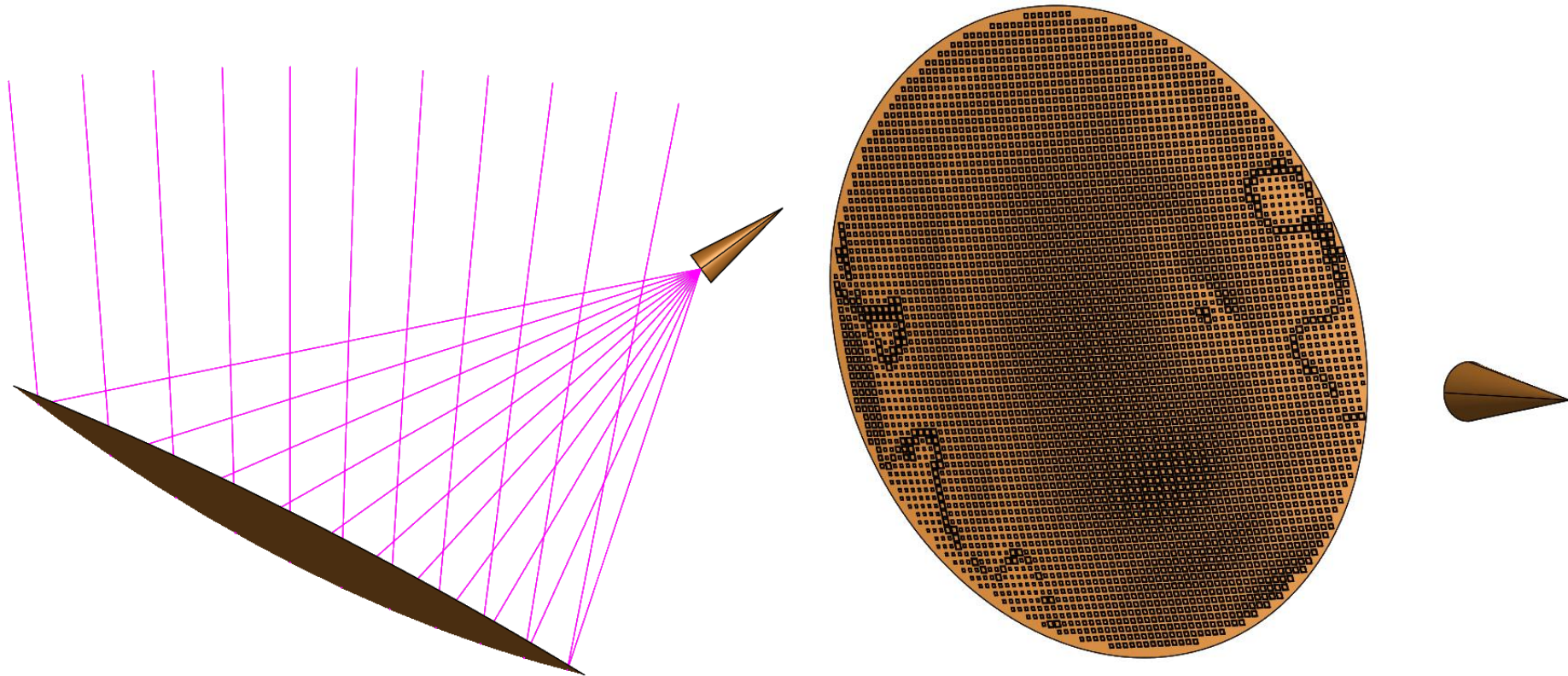
Improvement due to metasurface: 0.6-1.0 dB.

Further research needed in:

- Patch design for large bandwidth.

- Optimization methods, due to discontinuities and the large number of variables.

# Curved reflectarray for Rx-Tx bands



# Comparison with MLFMM

Very good agreement between Periodic MoM-PO and full-wave MLFMM.

The periodic MoM-PO approach is expected to be perfectly applicable for optimization of curved metasurface reflectors.

Limitations may appear for large angles of incidence and high surface curvature.

